## 3. Pair of Linear Equations in Two Variables

## Exercise 3.1

## 1. Question

Akhila went to a fair in her village. She wanted to enjoy rides on the Giant Wheel and play Hoopla (a game in which you throw a rig on the items kept in the stall, and if the ring covers any object completely you get it). The number of times she played Hoopla is half the number of rides she had on the Giant Wheel. Each ride costs Rs 3, and a game of Hoopla costs Rs 4. If she spent Rs 20 in the fair, represent this situation algebraically and graphically.

## Answer

Let the number of times Akhila played Hoopla be $x$ and number of times she played Giant wheel be $y$.
Given, number of times she played Hoopla is half the number of rides she had on the Giant Wheel.
$\Rightarrow x=2 y$
$\Rightarrow x-2 y=0$ For above equation, we have following table

| $x$ | 0 | 2 | 4 |
| :--- | :--- | :--- | :--- |
| $y$ | 0 | 1 | 2 |

Each ride costs Rs 3, and a game of Hoopla costs Rs 4 and she spent Rs 20 in the fair.
$\Rightarrow 4 x+3 y=20$

| x | 5 | 2 | 8 |
| :--- | :--- | :--- | :--- |
| y | 0 | 4 | -4 |

Thus, algebraically it is represented by :
$x-2 y=0$ and $4 x+3 y=0$
Geometrically, it can be graphed as,


## 2. Question

Aftab tells his daughter, 'Seven years ago, I was seven times as old as you were then. Also, three years from now, I shall be three times as old as you will be." Is not this interesting? Represent this situation algebraically and graphically.

## Answer

Let the present age of father be $x$ and present age of daughter be $y$.
Aftab tells his daughter, 'Seven years ago, I was seven times as old as you were then. Also, three years from now, I shall be three times as old as you will be."
$\therefore x-7=7(y-7) \Rightarrow x-7=7 y-49 \Rightarrow x-7 y+42=0 \Rightarrow x=7 y-42 \Rightarrow x=7(y-6)$
[1]The coordinates satisfying above equation are

| x | 7 | 14 | 21 |
| :---: | :---: | :---: | :---: |
| y | 7 | 8 | 9 |

Also, $x+3=3(y+3) \Rightarrow x+3=3 y+9 \Rightarrow x-3 y-6=0 \Rightarrow x=3 y+6 \Rightarrow x=3(y+2)$

two required algebraic representations.


## 3. Question

The path of a train $A$ is given by the equation $3 x+4 y-12=0$ and the path of another train $B$ is given by the equation $6 x$ $+8 y-48=0$. Represent this situation graphically.

## Answer

Given equations are $3 x+4 y-12=0$ and $6 x+8 y-48=0$
Let us plot the given equations. For this we will need some points to plot for the equation.
$3 x+4 y-12=0$
$4 y=12-3 x$ Now let us take random values of $x$ and obtain the corresponding values of $y$ by putting in the equation.at $x$ $=0,4 y=12-3 x 04 y=12 y=3$ Now at $y=0,3 x+4 x 0=123 x=12 x=4$ So we have two points for the equation $3 x$ $+4 y-12=0$ and those are $(0,3)$ and $(4,0) 6 x+8 y-48=0$ Now let us find points for this equationat $x=0,6 x 0+8 y$
$=488 y=48 y=6$ at $y=0,6 x+8 x 0=486 x=48 x=8$ So we have two points for the equation $6 x+8 y-48=0$ and those are $(8,0)$ and $(0,6) 3 x+4 y-12=0$ passes through $(4,0)$ and $(0,3)$
$6 x+8 y-48=0$ passes through $(8,0)$ and $(0,6)$


## 4. Question

Gloria is walking along the path joining $(-2,3)$ and $(2,-2)$, while Suresh is walking along the path joining $(0,5)$ and $(4,0)$. Represent this situation graphically.

## Answer

Given, Gloria is walking along the path joining $(-2,3)$ and $(2,-2)$, while Suresh is walking along the path joining $(0,5)$ and $(4,0)$.


## 5. Question

On comparing the ratios $\frac{a_{1}}{a_{2}}, \frac{b_{1}}{b_{2}}$ and $\frac{c_{1}}{c_{2}}$, and without drawing them, find out whether the lines representing the following pairs of linear equations intersect at a point, are parallel or coincide:
(i) $5 x-4 y+8=0$
$7 x+6 y-9=0$
(ii) $9 x+3 y+12=0$
$18 x+6 y+24=0$
(iii) $6 x-3 y+10=0$
$2 x-y+9=0$

## Answer

Two lines, $a 1 x+b 1 y+c 1=0$ and $a 2 x+b 2 y+c 2=0$
If $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, then the lines coincide
If $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines are parallel
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines intersect
(i) $5 x-4 y+8=0$
$7 x+6 y-9=0$
$\Rightarrow \frac{a 1}{a 2}=\frac{5}{7}, \frac{b 1}{b 2}=-\frac{4}{6}, \frac{c 1}{c 2}=\frac{8}{-9}$
Thus, $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$.
The lines intersect.
(ii) $9 x+3 y+12=0$
$18 x+6 y+24=0$
$\Rightarrow \frac{a 1}{a 2}=\frac{9}{18}=\frac{1}{2}, \frac{b 1}{b 2}=\frac{3}{6}=\frac{1}{2}, \frac{c 1}{c 2}=\frac{12}{24}=\frac{1}{2}$
Thus, $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
The lines are coincident.
(iii) $6 x-3 y+10=0$
$2 x-y+9=0$
$\Rightarrow \frac{a 1}{a 2}=\frac{6}{2}=3, \frac{b 1}{b 2}=-\frac{3}{-1}=3, \frac{c 1}{c 2}=\frac{10}{9}$
Thus, $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
The lines are parallel.

## 6. Question

Given the linear equation $2 x+3 y-8=0$, write another linear equation in two variables such that the geometrical representation of the pair so formed is:
(i) intersecting lines (ii) parallel lines
(iii) coincident lines.

## Answer

Two lines, $a 1 x+b 1 y+c 1=0$ and $a 2 x+b 2 y+c 2=0$

If $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, then the lines coincide
If $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines are parallel
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines intersect
Given the linear equation $2 x+3 y-8=0$.
An intersecting line is $x+2 y-4=0$
A parallel line is $4 x+6 y-12=0$
A coincident line is $4 x+6 y-16=0$

## 7. Question

The cost of 2 kg of apples and I kg of grapes on a day was found to be Rs 160 . After a month, the cost of 4 kg of apples and 2 kg of grapes is Rs 300. Represent the situation algebraically and geometrically.

## Answer

Let the cost of 1 kg of apple be $x$ and cost of 1 kg of grape be y .
Given, cost of 2 kg of apples and I kg of grapes on a day was found to be Rs 160.
$\therefore 2 x+y=160$
Also, after a month, the cost of 4 kg of apples and 2 kg of grapes is Rs 300 .
$\therefore 4 x+2 y=300$ Now to present these equations graphically plot the points of respective lines,For $2 x+y=160, y=160-$ $2 x$ When $x=50, y=60$ When $x=60, y=40$ Table is :

| x | 50 | 60 |
| :--- | :--- | :--- |
| y | 60 | 40 |

Plot the points $A(50,60)$ and $B(60,40)$
For $4 \mathrm{x}+2 \mathrm{y}=300, y=\frac{300-4 x}{2}$
$\Rightarrow y=150-2 x$ When $x=40, y=70$ When $x=60, y=30$ Table is :

| x | 40 | 60 |
| :--- | :--- | :--- |
| y | 70 | 30 |

Plot the points $C(40,-30)$ and $D(60,30)$


## Exercise 3.2

## 1. Question

Solve the following systems of equations graphically:
$x+y=3$
$2 x+5 y=12$

## Answer

For the solutions first we make graph for the equations.
For $x+y=3$,

| $x$ | 0 | 3 |
| :--- | :--- | :--- |
| $y$ | 3 | 0 |

$x+y=3$ passes through $(3,0)$ and $(0,3)$ For $2 x+5 y=12$,

| $x$ | 6 | 0 |
| :--- | :--- | :--- |
| $y$ | 0 | 2.4 |

$2 x+5 y=12$ passes through $(6,0)$ and $(0,2.4)$ Now we plot the points and join them to make graph.Wherever, they intersect that is common solution to both equations.


They meet at point $x=1$ and $y=2$.So $(1,2)$ is solution.

## 2. Question

Solve the following systems of equations graphically:
$x-2 y=5$
$2 x+3 y=10$
Answer
Given: The system of equations: $\begin{aligned} & x-2 y=5 \\ & 2 x+3 y=10\end{aligned}$
To find: The solution of above system.

## Solution:

For $x-2 y=5$,Put $x=5$, we get $y=0$ Put $x=1$, we get $y=-2$ Table for $x-2 y=5$

| x | 5 | 1 |
| :--- | :--- | :--- |
| y | 0 | -2 |

$x-2 y=5$, passes through $(0,5)$ and $(1,-2)$
For $2 x+3 y=10$ Put $x=-1$, we get $y=4$ Put $x=2$, we get $y=2$ Table for $2 x+3 y=10$

| x | -1 | 2 |
| :--- | :--- | :--- |
| y | 4 | 2 |

$2 x+3 y=10$ passes through $(0,5)$ and $(2,2)$ Plot the points in the graph,


The lines meet at the point $(5,0)$ So $x=5$ and $y=0$.

## 3. Question

Solve the following systems of equations graphically:
$3 x+y+1=0$
$2 x-3 y+8=0$

## Answer

$3 x+y+1=0$ passes through $(-1 / 3,0)$ and $(0,-1)$
$2 x-3 y+8=0$ passes through $(-4,0)$ and $(0,8 / 3)$
They meet at point $x=-1$ and $y=2$


## 4. Question

Solve the following systems of equations graphically:
$2 x+y-3=0$
$2 x-3 y-7=0$
Answer
$2 x+y-3=0$ passes through $(3 / 2,0)$ and $(0,3)$
$2 x-3 y-7=0$ passes through $(7 / 2,0)$ and $(0,-7 / 3)$


They meet at point $x=2, y=-1$

## 5. Question

Solve the following systems of equations graphically:
$x+y=6$
$x-y=2$

Answer
Given: $\begin{aligned} & x+y=6 \\ & x-y=2\end{aligned}$
To show: The given pair of equations graphically.
Solution:For $x+y=6$,Put $y=0$, we get $x=6$
Put $x=0$, we get $y=6$
Table for $x+y=6$

| $x$ | 6 | 0 |
| :--- | :--- | :--- |
| $y$ | 0 | 6 |

$x+y=6$ passes through $(6,0)$ and $(0,6)$
For $x-y=2$ Put $y=0$, we get $x=2$
Put $x=0$, we get $y=-2$
Table for $x-y=2$

| $x$ | 2 | 0 |
| :--- | :--- | :--- |
| $y$ | 0 | -2 |

$x-y=2$ passes through $(2,0)$ and $(0,-2)$ Plot the points in the graph,


They meet at point $x=4, y=2$

## 6. Question

Solve the following systems of equations graphically:
$x-2 y=6$
$3 x-6 y=0$

## Answer

$x-2 y=6$ passes through $(6,0)$ and $(0,-3)$
$3 x-6 y=0$ passes through origin
Both lines are parallel, thus it has no solution.


## 7. Question

Solve the following systems of equations graphically:
$x+y=4$
$2 x-3 y=3$

## Answer

For $x+y=4$,Put $y=0$, we get $x=4$
Put $x=0$, we get $y=4$
Table for $x+y=4$

| $x$ | 4 | 0 |
| :--- | :--- | :--- |
| $y$ | 0 | 4 |

$x+y=4$ passes through $(4,0)$ and $(0,4)$
For $2 \mathrm{x}-3 \mathrm{y}=3 \mathrm{y}=\frac{2 x-3}{3}$
Put $y=1$, we get $x=3$
Put $x=0$, we get $y=-1$
Table for $x-y=2$

| $x$ | 3 | 0 |
| :--- | :--- | :--- |
| $y$ | 1 | -1 |

$2 x-3 y=3$ passes through $(3,1)$ and $(0,-)$ Plot the points in the graph


They meet at point $(3,1)$ Hence $x=3, y=1$.

## 8. Question

Solve the following systems of equations graphically:
$2 x+3 y=4$
$x-y+3=0$

## Answer

$2 x+3 y=4$ passes through $(2,0)$ and $(0,4 / 3)$
$x-y+3=0$ passes through $(-3,0)$ and $(0,3)$
They meet at point $x=-1, y=2$


## 9. Question

Solve the following systems of equations graphically:
$2 x-3 y+13=0$
$3 x-2 y+12=0$

## Answer

On solving graphically,
$2 x-3 y+13=0$ passes through $(-6.5,0)$ and $(0,13 / 3)$
$3 x-2 y+12=0$ passes through $(-4,0)$ and $(0,6)$
Thus the meeting point of the straight lines is, $(-2,-3)$


## 10. Question

Solve the following systems of equations graphically:
$2 x+3 y+5=0$
$3 x-2 y-12=0$

## Answer

For the equation $2 x+3 y+5=0, y=\frac{-5-2 x}{3}$
When $x=-1, y=-1$
When $x=5, y=-5$
Table is:

| $x$ | -1 | 5 |
| :--- | :--- | :--- |
| $y$ | -1 | -5 |

Plot the points $A(-1,-1) B(-5,5)$ on the graph

For the equation $3 \mathrm{x}-2 \mathrm{y}-12=0, y=\frac{3 x-12}{2}$
When $\mathrm{x}=0, \mathrm{y}=-6$
When $x=2, y=-3$
Table is :

| $x$ | 0 | 2 |
| :--- | :--- | :--- |
| $y$ | -6 | -3 |

Plot the points $C(0,-6) D(2,-3)$ on the graph



Since the two lines meet at the point $(2,-3)$ Therefore, $x=2$ and $y=-3$

## 11. Question

Show graphically that each one of the following systems of equations has infinitely many solutions:
$2 x+3 y=6$
$4 x+6 y=12$

## Answer

Given: the system of equations: $\begin{aligned} & 2 x+3 y=6 \\ & 4 x+6 y=12\end{aligned}$
To show:systems of equations has infinitely many solutions.

## Solution:

consider the equation $2 x+3 y=6$
To plot its graph, we have $y=\frac{6-2 x}{3}$
Putting $x=0$ we get $y=2$
putting $y=0$ we get $x=3$
The table for points of $2 x+3 y=6$ is:

| $x$ | 0 | 3 |
| :--- | :--- | :--- |
| $y$ | 2 | 0 |

Plot $A(0,2)$ and $B(3,0)$ in the graph
Consider the equation $4 x+6 y=12$
To plot its graph, we have $y=\frac{12-4 x}{6}$

Putting $x=6$ we get $y=-2$
Putting $y=4$ we get $x=-3$
The table for the points $4 x+6 y=12$ is:

| $x$ | 6 | -3 |
| :--- | :--- | :--- |
| $y$ | -2 | 4 |

Plot $C(6,-2)$ and $D(-3,4)$ in the graph
Now plot the graphs for these equations as:


As Both the lines pass through the same points and are coinciding. There can be infinite points lying on both the lines.Hence,systems of equations has infinitely many solutions.

## 12. Question

Show graphically that each one of the following systems of equations has infinitely many solutions:
$x-2 y=5$
$3 x-6 y=15$
Answer

Both pass through the same points and are coinciding.

## 13. Question

Show graphically that each one of the following systems of equations has infinitely many solutions:
$3 x+y=8$
$6 x+2 y=16$
Answer
Given: the system of equations: $\begin{aligned} & 3 x+y=8 \\ & 6 x+2 y=16\end{aligned}$
To show:systems of equations has infinitely many solutions.
Solution:consider the equation $3 x+y=8$
To plot its graph, we have $y=8-3 x$
Putting $x=0$ we get $y=8$
putting $y=2$ we get $x=2$
The table for points of $3 x+y=8$ is:

| x | 0 | 2 |
| :--- | :--- | :--- |
| y | 8 | 2 |

Plot $A(0,8)$ and $B(2,2)$ in the graph
Consider the equation $6 x+2 y=16$
To plot its graph, we have $y=\frac{16-2}{6}$
Putting $x=2$ we get $y=2$
Putting $y=0$ we get $x=8$
The table for the points $6 x+2 y=16$ is:

| $x$ | 1 | 3 |
| :--- | :--- | :--- |
| $y$ | 5 | -1 |

Plot $C(1,5)$ and $D(3,-1)$ in the graph
Now plot the graphs for these equations as:


As Both the lines pass through the same points and are coinciding. There can be infinite points lying on both the lines. Hence,systems of equations has infinitely many solutions.

## 14. Question

Show graphically that each one of the following systems of equations has infinitely many solutions:
$x-2 y+11=0$
$3 x-6 y+33=0$
Answer


Both pass through the same points and are coinciding.

## 15. Question

Show graphically that each one of the following systems of equations is in-consistent (i.e. has no solution):
$3 x-5 y=20$
$6 x-10 y=-40$

## Answer


$3 x-5 y=20$ passes through $(20 / 3,0)$ and $(0,-4)$
$6 x-10 y=-40$ passes through $(-20 / 3,0)$ and $(0,4)$
Both are parallel lines, thus system of equations is in-consistent.

## 16. Question

Show graphically that each one of the following systems of equations is in-consistent (i.e. has no solution):
$x-2 y=6$
$3 x-6 y=0$

## Answer


$x-2 y=6$ passes through $(6,0)$ and $(0,-3)$
$3 x-6 y=0$ passes through origin
Both are parallel lines, thus system of equations is in-consistent.

## 17. Question

Show graphically that each one of the following systems of equations is in-consistent (i.e. has no solution):
$2 y-x=9$
$6 y-3 x=21$

## Answer


$2 y-x=9$ passes through $(-9,0)$ and $(0,9 / 2)$
$6 y-3 x=21$ passes through $(-7,0)$ and $(0,7 / 2)$
Both are parallel lines, thus system of equations is in-consistent.

## 18. Question

Show graphically that each one of the following systems of equations is in-consistent (i.e. has no solution):
$3 x-4 y-1=0$
$2 x-\frac{8}{3} y+5=0$
Answer

$3 x-4 y-1=0$ passes through $(1 / 3,0)$ and $(0,-1 / 4)$
$2 x-8 y / 3+5=0$ passes through $(-5 / 2,0)$ and $(0,15 / 8)$
Both are parallel lines, thus system of equations is in-consistent.

## 19. Question

Determine graphically the vertices of the triangle, the equations of whose sides are given below:
(i) $2 y-x=8,5 y-x=14$ and $y-2 x=1$
(ii) $y=x, y=0$, and $3 x+3 y=10$

Answer

(i) $2 y-x=8,5 y-x=14$ and $y-2 x=1$
$2 y-x=8$ passes through $(-8,0)$ and $(0,4)$
$5 y-x=14$ passes through $(-14,0)$ and $(0,14 / 5)$
$Y-2 x=1$ passes through $(0,1)$ and $(-1 / 2,0)$
Vertices of the triangle are $(-4,2),(1,3)$ and $(2,5)$
(ii) $y=x, y=0$, and $3 x+3 y=10$

$3 x+3 y=10$ passes through $(10 / 3,0)$ and $(0,10 / 3)$
Vertices of the triangle are $(0,0),(10 / 3,0)$ and $(5 / 3,5 / 3)$

## 20. Question

Determine, graphically whether the system of equations is consistent or in-consistent.
$x-2 y=2,4 x-2 y=5$
Answer
$x-2 y=2$ passes through $(2,0)$ and $(0,-1)$
$4 x-2 y=5$ passes through $(5 / 4,0)$ and $(0,-5 / 2)$


Thus the system of equations is consistent and it has a unique solution.

## 21. Question

Determine, by drawing graphs, whether the following system of linear equations has a unique solution or not:
(i) $2 x-3 y=6, x+y=1$
(ii) $2 y=4 x-6,2 x=y+3$

Answer
(i) $2 x-3 y=6$ passes through $(3,0)$ and $(0,-2)$
$X+y=1$ passes through $(0,1)$ and $(1,0)$


Thus it has unique solution
(ii) $2 y=4 x-6$ passes through $(3 / 2,0)$ and $(0,-3)$
$2 x=y+3$ passes through $(3 / 2,0)$ and $(0,-3)$


$$
2 x=y+3
$$

The lines are coincident, it has infinite solutions
22. Question

Solve graphically each of the following systems of linear equations. Also find the coordinates of the points where the lines meet axis of $y$.
(i) $2 x-5 y+4=0$
$2 x+y-8=0$
(ii) $3 x+2 y=12$
$5 x-2 y=4$
(iii) $2 x+y-11=0$
$x-y-1=0$
(iv) $x+2 y-7=0$
$2 x-y-4=0$
(v) $3 x+y-5=0$
$2 x-y-5=0$
(vi) $2 x-y-5=0$
$x-y-3=0$

## Answer

(i)


It has a unique solution at $x=3$ and $y=2$

Coordinates where lines meet $y$ axis is $(0,4 / 5)$ and $(0,8)$
(ii)


Unique solution at $x=2$ and $y=3$.
Lines meet the $y$ axis at $(0,6)$ and $(0,-2)$
(iii)


Unique solution at $x=4$ and $y=3$
Lines meet the $y$ axis at $(0,11)$ and $(0,-1)$
(iv)


Unique solution at $x=3$ and $y=2$
Lines meet $y$ axis at $(0,7 / 2)$ and ( $0,-4$ )
(v)


Unique solution at $x=2$ and $y=-1$
Lines meet the $y$-axis at $(0,5)$ and $(0,-5)$
(vi)


Unique solution at $x=2$ and $y=-1$
Lines meet $y$-axis at $(0,-5)$ and ( $0,-3$ )
23. Question

Determine graphically the coordinates of the vertices of a triangle, the equations of whose sides are:
(i) $y=x, y=2 x$ and $y+x=6$
(ii) $y=x, 3 y=x, x+y=8$

Answer
(i) $y=x, y=2 x$ and $y+x=6$

The triangle formed has vertices
$(0,0),(2,4)$ and $(3,3)$

(ii) $y=x, 3 y=x, x+y=8$

The triangle formed has vertices
$(0,0),(4,4)$ and $(6,2)$


## 24. Question

Solve the following system of linear equations graphically and shade the region between the two lines and $x$-axis:
(i) $2 x+3 y=12$,
$x-y=1$
(ii) $3 x+2 y-4=0$,
$2 x-2 y-7=0$
(iii) $3 x+2 y-11=0$
$2 x-3 y+10=0$
Answer
i) $2 x+3 y=12$ passes through $(6,0)$ and $(0,4)$
$x-y=1$ passes through $(1,0)$ and ( $0,-1$ )
They meet at $x=3, y=2$

ii) $3 x+2 y-4=0$ passes through, $(4 / 3,0)$ and $(0,2)$
$2 \mathrm{x}-2 \mathrm{y}-7=0$ passes through $(7 / 2,0)$ and ( $0,-7 / 2$ )
They meet at $x=2, y=-1$

iii) $3 x+2 y-11=0$ passes through $(11 / 3,0)$ and $(0,11 / 2)$
$2 x-3 y+10=0$ passes through $(-5,0)$ and $(0,10 / 3)$
They meet at $x=1, y=4$


## 25. Question

Draw the graphs of the following equations on the same graph paper:
$2 x+3 y=12$
$x-y=1$
Find the coordinates of the vertices of the triangle formed by the two straight lines and the $y$-axis.

## Answer


$2 x+3 y=12$
$x-y=1$
Lines meet at $x=3, y=2$
Coordinates of the vertices of the triangle formed with $y$-axis
$(0,-1),(0,4)$ and $(3,2)$

## 26. Question

Draw the graphs of $x-y+1=0$ and $3 x+2 y-12=0$. Determine the coordinates of the vertices of the triangle formed by these lines and $x$-axis and shade the triangular area. Calculate the area bounded by these lines and $x$-axis.

## Answer

$x-y+1=0$ and $3 x+2 y-12=0$


Coordinates of the vertices of triangle formed with $x$-axis
$(2,3),(-1,0)$ and (4, 0)
Height of the triangle $=3$ units
Base of the triangle $=5$ units
Area $=0.5 \times$ base $\times$ height $=7.5$ sq units

## 27. Question

Solve graphically the system of linear equations:
$4 x-3 y+4=0$
$4 x+3 y-20=0$
Find the area bounded by these lines and $x$-axis.

## Answer

They meet at $x=2, y=4$
Height of the triangle formed $=4$ units
Base of the triangle formed $=5+1=6$
Area of the region bounded by these lines and $x$-axis

$=0.5 \times 4 \times 6$
$=12$ sq. units

## 28. Question

Solve the following system of linear equations graphically:
$3 x+y-11=0, x-y-1=0$
Shade the region bounded by these lines and $y$-axis. Also, find the area of the region bounded by the these lines and $y$ axis.

Answer

$3 x+y-11=0, x-y-1=0$
They meet at $x=3, y=2$
Height of the triangle formed with $y$-axis $=3$ units
Base of the triangle formed $=11+1=12$ units
Area of the bounded region $=0.5 \times 3 \times 36=18$ sq. units

## 29. Question

Solve graphically each of the following systems of linear equations. Also, find the coordinates of the points where the lines meet the axis of $x$ in each system:
(i) $2 x+y=6$
$x-2 y=-2$
(ii) $2 x-y=2$
$4 x-y=8$
(iii) $x+2 y=5$
$2 x-3 y=-4$
(iv) $2 x+3 y=8$
$x-2 y=-3$
Answer

i) $2 x+y=6 \quad x-2 y=-2$

Unique solution at $x=2, y=2$
Lines meet $x$-axis at $(3,0)$ and $(-2,0)$
ii) $2 x-y=2$
$4 x-y=8$


Unique solution at $x=3, y=3$

Lines meet $x$-axis at $(1,0)$ and $(2,0)$
iii) $x+2 y=5$
$2 x-3 y=-4$


Unique solution at $x=1, y=2$
Lines meet $x$-axis at $(5,0)$ and $(-2,0)$
iv) $2 x+3 y=8$
$x-2 y=-3$


Unique solution at $x=1, y=2$
Lines meet $x$-axis at $(4,0)$ and $(-3,0)$

## 30. Question

Draw the graphs of the following equations:
$2 x-3 y+6=0$
$2 x+3 y-18=0$
$y-2=0$
Find the vertices of the triangle so obtained. Also, find the area of the triangle.

## Answer

For equation, $2 x-3 y+6=0$
Coordinates satisfying graph are,

| x | 0 | -3 |
| :---: | :---: | :---: |
| y | 2 | 0 |

For equation, $2 x+3 y-18=0$
Coordinates satisfying graph are,

| x | 0 | 9 |
| :---: | :---: | :---: |
| y | 6 | 0 |

and $y-2=0$
$\Rightarrow y=2$, which is a straight line parallel to $x$-axis intersecting the $y$-axis at 2
On plotting all the three line on graphs, we get the graph as follows


On observing from graph,
Vertices of the triangle obtained are
$(0,2),(3,4)$ and $(6,2)$
Height of triangle $=4-2=2$
Base of the triangle $=6$
Area of the triangle
$=\frac{1}{2} \times$ Base $\times$ Height
$=\frac{1}{2} \times 6 \times 2$
$=6$ square units

## 31. Question

Solve the following system of equations graphically:
$2 x-3 y+6=0$
$2 x+3 y-18=0$
Also, find the area of the region bounded by these two lines and $y$-axis.

## Answer



Unique solution at $x=3$ and $y=4$
Vertices of triangle formed with $y$-axis are
$(0,2),(3,4)$ and $(0,6)$
Height of the triangle obtained $=3$ units
Base of the triangle obtained $=6-2=4$ units
Area of the triangle $=0.5 \times 3 \times 4=6$ sq. units

## 32. Question

Solve the following system of linear equations graphically:

Determine the vertices of the triangle formed by the lines representing the above equation and the $y$-axis.

## Answer


$4 x-5 y-20=0$
$3 x+5 y-15=0$
Unique solution at $\mathrm{x}=5$ and $\mathrm{y}=0$
Vertices of the triangle with $y$ axis are
$(0,3),(0,-4)$ and $(5,0)$

## 33. Question

Draw the graphs of the equations $5 x-y=5$
and $3 x-y=3$. Determine the coordinates of the vertices of the triangle formed by these lines and $y$-axis. Calculate the area of the triangle so formed.

## Answer


$5 x-y=5$
and $3 x-y=3$
Coordinates of the vertices of the triangle formed by these lines and $y$-axis
$(1,0),(0,-3),(0,-5)$
Height of triangle $=1$ unit
Base of triangle $=5-3=2$ unit
Area of triangle $=0.5 \times 1 \times 2=1$ sq. units

## 34. Question

Form the pair of linear equations in the following problems, and find their solution graphically:
(i) 10 students of class $X$ took part in Mathematics quiz. If the number of girls is 4 more than the number of boys, find the number of boys and girls who took part in the quiz.
(ii) 5 pencils and 7 pens together cost Rs. 50 , whereas 7 pencils and 5 pens together cost Rs. 46 . Find the cost of one pencil and a pen.
(iii) Champa went to a 'sale' to purchase some pants and skirts. When her friends asked her how many of each she had bought, she answered, "The number of skirts is two less than twice the number of pants purchased. Also, the number of
skirts is four less than four times the number of pants purchased." Help her friends to find how many pants and skirts Champa bought.

## Answer

i) Let the number of boys and girls be ' $a$ ' and ' $b$ '.

10 students of class $X$ took part in Mathematics quiz. If the number of girls is 4 more than the number of boys
$\Rightarrow \mathrm{a}+\mathrm{b}=10$ and $\mathrm{b}=\mathrm{a}+4$
Thus, $\mathrm{a}=3$ and $\mathrm{b}=7$
ii ) Let the cost of 1 pen be a and 1 pencil be $b$.
5 pencils and 7 pens together cost Rs. 50 , whereas 7 pencils and 5 pens together cost Rs. 46
$\Rightarrow 7 \mathrm{a}+5 \mathrm{~b}=50$ and $5 \mathrm{a}+7 \mathrm{~b}=46$
Solving by multiplying $1^{\text {st }}$ by 7 and $2^{\text {nd }}$ by 5 and subtracting
$\Rightarrow 24 \mathrm{a}=120$
$\Rightarrow \mathrm{a}=$ Rs. 5
Thus, $35+5 b=50$
$\Rightarrow \mathrm{b}=$ Rs. 3
iii) Let the number of pants and skirts bought be ' $a$ ' and ' $b$ '

Champa went to a 'sale' to purchase some pants and skirts. When her friends asked her how many of each she had bought, she answered, "The number of skirts is two less than twice the number of pants purchased. Also, the number of skirts is four less than four times the number of pants purchased."
$\Rightarrow \mathrm{b}=2 \mathrm{a}-2$ and $\mathrm{b}=4 \mathrm{a}-4$
$\Rightarrow 2 a-2=4 a-4$
$\Rightarrow \mathrm{a}=1$
Thus, $\mathrm{b}=2-2=0$

## 35. Question

Solve the following system of equations graphically:
Shade the region between the lines and the $y$-axis
(i) $3 x-4 y=7$
$5 x+2 y=3$
(ii) $4 x-y=4$
$3 x+2 y=14$

## Answer

i) $3 x-4 y=7$
$5 x+2 y=3$


Unique solution at $x=1, y=-1$
ii) $4 x-y=4$
$3 x+2 y=14$
Unique solution at $x=2, y=4$


## 36. Question

Represent the following pair of equations graphically and write the coordinates of points where the lines intersects $y$-axis
$x+3 y=6$
$2 x-3 y=12$
Answer
$x+3 y=6$
$2 x-3 y=12$


Lines meet $y$-axis at $(0,2)$ and $(0,-4)$

## 37. Question

Given the linear equation $2 x+3 y-8=0$, write another linear equation in two variables such that the geometrical representation of the pair so formed is
(i) intersecting lines (ii) Parallel lines
(iii) coincident lines

Answer
Two lines, $a 1 x+b 1 y+c 1=0$ and $a 2 x+b 2 y+c 2=0$
If $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, then the lines coincide
If $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines are parallel
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, then the lines intersect
Given line $2 x+3 y-8=0$
i) intersecting line : $3 x+2 y-6=0$
ii) parallel line : $4 x+6 y=15$
iii) coincident line : $4 x+6 y-16=0$

## Exercise 3.3

## 1. Question

Solve the following systems of equations:
$11 x+15 y+23=0$
$7 x-2 y-20=0$
Answer
$11 x+15 y+23=0$
$7 x-2 y-20=0$
Multiplying the $1^{\text {st }}$ equation by 2 and $2^{\text {nd }}$ equation by 15 , we get $22 x+30 y+46=0$
$[3] 105 x-30 y-300=0$ [4]Adding [3] and [4]
$\Rightarrow 22 x+30 y+46+105 x-30 y-300=0$
$\Rightarrow 127 \mathrm{x}=254$
$\Rightarrow \mathrm{x}=2$
Substituting value of $x$ in eq1.
$\Rightarrow 11(2)+15 y+23=0$
$\Rightarrow 22+15 y+23=0$
$\Rightarrow 15 y=-45$
$\Rightarrow y=-3$

## 2. Question

Solve the following systems of equations:
$3 x-7 y+10=0$
$y-2 x-3=0$
Answer
$3 x-7 y+10=0 \quad y-2 x-3=0$
Multiplying eq 1 by 2 and eq 2 by 3 and adding.
$\Rightarrow 6 x-14 y+20+3 y-6 x-9=0$
$\Rightarrow-11 y=-11$
$\Rightarrow y=1$
Substituting value of $y$ in eq1, we get $x=-1$

## 3. Question

Solve the following systems of equations:
$0.4 x+0.3 y=1.7$
$0.7 x-0.2 y=0.8$

## Answer

$0.4 x+0.3 y=1.7$
$0.7 x-0.2 y=0.8$
Multiplying eq 1 by 0.2 and eq2 by 0.3 and adding
$\Rightarrow 0.08 x+0.06 y+0.21 x-0.06 y=0.34+0.24$
$\Rightarrow 0.29 x=0.58$
$\Rightarrow x=2$
Substituting value of $x$ in eq1, $0.8 x+0.3 y=1.7$
$\Rightarrow y=3$

## 4. Question

Solve the following systems of equations:
$\frac{x}{2}+y=0.8$
$\frac{7}{x+\frac{y}{2}}=10$
Answer
$\frac{x}{2}+y=0.8$
$\frac{7}{x+\frac{y}{2}}=10$
$\Rightarrow x+y / 2=0.7$
Multiplying eq1 by 2 and subtracting eq 2 from it.
$\Rightarrow x+2 y-x-y / 2=1.6-0.7$
$\Rightarrow 3 y / 2=0.9$
$\Rightarrow y=0.6$
Thus, $x / 2+0.6=0.8$
$\Rightarrow \mathrm{x}=0.4$

## 5. Question

Solve the following systems of equations:
$7(y+3)-2(x+2)=14$
$4(y-2)+3(x-3)=2$
Answer
$7(y+3)-2(x+2)=147 y+21-2 x-4=147 y-2 x=14-21+4$
$\Rightarrow 7 y-2 x=-3--(1)$
$4(y-2)+3(x-3)=24 y-8+3 x-9=24 y+3 x=2+8+9$
$\Rightarrow 4 y+3 x=19$
Multiplying eq 1 by 3 and eq 2 by 2 and adding them
$3(7 y-2 x)+2(4 y+3 x)=-3(3)+19(2)$
$\Rightarrow 21 y-6 x+8 y+6 x=-9+38 \Rightarrow 29 y=29$
$\Rightarrow y=1$
Put the value of $y$ in (1) to get,
$7-2 x=-3-2 x=-3-7-2 x=-10$
$\Rightarrow x=5$

## 6. Question

Solve the following systems of equations:
$\frac{x}{7}+\frac{y}{3}=5$
$\frac{x}{2}-\frac{y}{9}=6$
Answer
$\frac{x}{7}+\frac{y}{3}=5$
$\Rightarrow 3 x+7 y=105$
$\frac{x}{2}-\frac{y}{9}=6$
$\Rightarrow 9 x-2 y=108$
Multiplying eq1 by 3 and subtracting eq2 from it
$\Rightarrow 9 x+21 y-9 x+2 y=315-108$
$\Rightarrow 23 y=207$
$\Rightarrow y=9$
Thus, $9 x-18=108$
$\Rightarrow x=14$

## 7. Question

Solve the following systems of equations:
$\frac{x}{3}+\frac{y}{4}=11$
$\frac{5 x}{6}-\frac{y}{3}=-7$
Answer
$\frac{x}{3}+\frac{y}{4}=11$
$\Rightarrow 4 x+3 y=132$
$\frac{5 x}{6}-\frac{y}{3}=-7$
$\Rightarrow 5 x-2 y=-42$
Multiplying eq 1 by 2 and eq 2 by 3 and adding them
$\Rightarrow 8 x+6 y+15 x-6 y=264-126$
$\Rightarrow 23 x=138$
$\Rightarrow x=6$
Thus, $24+3 y=132$
$\Rightarrow y=36$

## 8. Question

Solve the following systems of equations:
$\frac{4}{x}+3 y=8$
$\frac{6}{x}-4 y=-5$
Answer
$\frac{4}{x}+3 y=8$
$\frac{6}{x}-4 y=-5$
Multiplying eq1 by 4 and eq2 by 3 and adding
$\Rightarrow 16 / x+12 y+18 / x-12 y=32-15 \Rightarrow 34 / x=17$
$\Rightarrow \mathrm{x}=2$
Thus, $2+3 y=8 \Rightarrow 3 y=6$
$\Rightarrow y=2$
9. Question

Solve the following systems of equations:
$x+\frac{y}{2}=4$
$\frac{x}{3}+2 y=5$
Answer
$x+\frac{y}{2}=4 \Rightarrow 2 \mathrm{x}+\mathrm{y}=8$.
$\frac{x}{3}+2 y=5 \Rightarrow x+6 y=15$
Multiplying eq2 by 2 and subtracting from eq1
$\Rightarrow 2 x+y-2 x-12 y=8-30$
$\Rightarrow-11 y=-22$
$\Rightarrow y=2$
Thus, $2 x+2=8$
$\Rightarrow x=3$

## 10. Question

Solve the following systems of equations:
$x+2 y=\frac{3}{2}$
$2 x+y=\frac{3}{2}$
Answer
$x+2 y=\frac{3}{2} \Rightarrow 2 x+4 y=3$.
$2 x+y=\frac{3}{2} \Rightarrow 4 x+2 y=3$
Multiplying eq2 by 2 and subtracting from eq1
$2 x+4 y-8 x-4 y=3-6$
$\Rightarrow-6 x=-3$
$\Rightarrow x=1 / 2$
Thus, $2 \times 1 / 2+4 y=3 \Rightarrow y=1 / 2$

## 11. Question

Solve the following systems of equations:
$\sqrt{2 x}-\sqrt{3 y}=0$
$\sqrt{3 x}-\sqrt{8 y}=0$
Answer
Given: The following systems of equations:
$\sqrt{2 x}-\sqrt{3 y}=0$
$\sqrt{3 x}-\sqrt{8 y}=0$
To find: The values of $x$ and $y$.
Solution: $\sqrt{2 x}-\sqrt{3 y}=0$
$\Rightarrow \sqrt{2 x}=\sqrt{3 y}$
Squaring both sides to get,
$2 x=3 y$
$\Rightarrow x=\frac{3 y}{2}$
Now,
$\sqrt{3 x}-\sqrt{8 y}=0 \Rightarrow \sqrt{3 x}=\sqrt{8 y}$
Squaring both sides to get, $3 x=8 y \quad \ldots .$. (1)
Substitute the value of $x$ in (1),
$3\left(\frac{3 y}{2}\right)=8 y$
$\frac{9 y}{2}=8 y$
$\frac{9 y}{2}-8 y=0$
$\frac{9 y-16 y}{2}=0$
$\frac{-7 y}{2}=0$
$-7 y=0$
$y=0$
Substitute the value of $y$ in $2 x=3 y \Rightarrow 2 x=3(0) \Rightarrow 2 x=0 \Rightarrow x=0$

Solution is $x=0, y=0$.
12. Question

Solve the following systems of equations:
$3 x-\frac{Y+7}{11}+2=10$
$2 y+\frac{x+11}{7}=10$

## Answer

Consider $3 x-\frac{Y+7}{11}+2=10$,
$\Rightarrow \frac{11(3 x)-y-7+2(11)}{11}=10$
$\Rightarrow \frac{33 x-y-7+22}{11}=10$
$\Rightarrow 33 x-y-7+22=110 \Rightarrow 33 x-y-95=0 \Rightarrow 33 x-95=y$
Consider $2 y+\frac{x+11}{7}=10$,
$\Rightarrow \frac{7(2 y)+x+11}{7}=10$
$\Rightarrow \frac{14 y+x+11}{7}=10$
$\Rightarrow 14 y+x+11=70$
$\Rightarrow 14 y+x=59$
Put the value of $y$ from (1) in (2) to get, $14(33 x-95)+x=59462 x-1330+x=59463 x=1389 x=3$ Put the value of $x$ in (1) to get, $33(3)-95=y 99-95=y 4=y \Rightarrow x=3$ and $y=4$

## 13. Question

Solve the following systems of equations:
$2 x-\frac{3}{y}=9$
$3 x+\frac{7}{y}=2, y \neq 0$
Answer
$2 x-\frac{3}{y}=9$
$3 x+\frac{7}{y}=2, y \neq 0$
Multiplying eq1 by 3 and eq2 by 2 and subtracting eq1 from eq2
$\Rightarrow 6 x+21 / y-6 x+6 / y=4-27$
$\Rightarrow 23 / y=-23$
$\Rightarrow y=-1$
Thus, $2 x+3=9$
$\Rightarrow x=3$

## 14. Question

Solve the following systems of equations:
$0.5 x+0.7 y=0.74$
$0.3 x+0.5 y=0.5$
Answer
$0.5 x+0.7 y=0.74$
$0.3 x+0.5 y=0.5$
Multiplying eq 1 by 0.3 and eq2 by 0.5 and subtracting eq 1 from eq 2
$\Rightarrow 0.15 x+0.25 y-0.15 x-0.21 y=0.25-0.222$
$\Rightarrow 0.04 y=0.028$
$\Rightarrow y=0.7$
Thus, $x=0.5$

## 15. Question

Solve the following systems of equations:
$\frac{1}{7 x}+\frac{1}{6 y}=3$
$\frac{1}{2 x}-\frac{1}{3 y}=5$

## Answer

## Given:

systems of equations:
$\frac{1}{7 x}+\frac{1}{6 y}=3$
$\frac{1}{2 x}-\frac{1}{6 y}=5$
To find: The values of $x$ and $y$.
Solution:
Let's take,
$\frac{1}{x}=u, \frac{1}{y}=v$
The equations become:
$\frac{1}{7} u+\frac{1}{6} v=3$
$\frac{6 u+7 v}{42}=3$
$6 u+7 v=126$
$\frac{1}{2} u-\frac{1}{3} v=5$
$\frac{3 u-2 v}{6}=5$
$3 u-2 v=30 \ldots \ldots$ (2)Now multiply eq. (2) with 2 and subtract it from eq. (1) $\Rightarrow 6 u+7 v-2(3 u-2 v)=126-2(30) \Rightarrow 6 u+$ $7 v-6 u+4 v=126-60 \Rightarrow 11 v=66 \Rightarrow v=6$ Now put the value of $v$ in eq.
(2) to get, $\Rightarrow 3 u-2(6)=30 \Rightarrow 3 u-12=30 \Rightarrow 3 u=42 \Rightarrow u=14$

Now
$u=\frac{1}{x}=14$
$x=\frac{1}{14}$

And
$v=\frac{1}{y}=6$
$y=\frac{1}{6}$

## 16. Question

Solve the following systems of equations:
$\frac{1}{2 x}+\frac{1}{3 y}=2$
$\frac{1}{3 x}+\frac{1}{2 y}=\frac{13}{6}$
Answer
$\frac{1}{2 x}+\frac{1}{3 y}=2$
$\frac{1}{3 x}+\frac{1}{2 y}=\frac{13}{6}$
Multiplying eq 1 by $1 / 2$ and eq 2 by $1 / 3$ and subtracting
$\Rightarrow 1 / 4 \mathrm{x}-1 / 9 \mathrm{x}=1-13 / 18$
$\Rightarrow 5 / 36 x=5 / 18$
$\Rightarrow x=1 / 2$
Thus, $1+1 / 3 y=2$
$\Rightarrow y=1 / 3$

## 17. Question

Solve the following systems of equations:
$\frac{x+y}{x y}=2$
$\frac{x-y}{x y}=6$
Answer
$\frac{x+y}{x y}=2$
$\frac{x-y}{x y}=6$
Adding both equation
$\Rightarrow 2 x / x y=8$
$\Rightarrow y=1 / 4$
Thus, $\frac{\left(x+\frac{1}{4}\right)}{\frac{x}{4}}=2$
$\Rightarrow x+1 / 4=x / 2$
$\Rightarrow \mathrm{x}=-1 / 2$

## 18. Question

Solve the following systems of equations:
$\frac{15}{u}+\frac{2}{v}=17$
$\frac{1}{u}+\frac{1}{v}=\frac{36}{5}$
Answer
$\frac{15}{u}+\frac{2}{v}=17$
$\frac{1}{u}+\frac{1}{v}=\frac{36}{5}$
Multiplying eq2 by 2 and subtracting
$13 / u=17-72 / 5$
$\Rightarrow u=5$
Thus, $3+2 / v=17$
$\Rightarrow \mathrm{v}=1 / 7$

## 19. Question

Solve the following systems of equations:
$\frac{3}{x}-\frac{1}{y}=-9$
$\frac{2}{x}+\frac{3}{y}=5$
Answer
$\frac{3}{x}-\frac{1}{y}=-9$
$\frac{2}{x}+\frac{3}{y}=5$
Multiplying eq1 by 3 and adding to eq1
$\Rightarrow 11 / x=-27+5$
$\Rightarrow x=-1 / 2$
Thus, $-4+3 / y=5$
$\Rightarrow y=1 / 3$

## 20. Question

Solve the following systems of equations:
$\frac{2}{x}+\frac{5}{y}=1$
$\frac{60}{x}+\frac{40}{y}=19, x \neq 0, y \neq 0$
Answer
$\frac{2}{x}+\frac{5}{y}=1$
$\frac{60}{x}+\frac{40}{y}=19, x \neq 0, y \neq 0$
Multiplying eq1 by 8 and subtracting from eq2
$\Rightarrow 44 / x=19-8$
$\Rightarrow x=4$
Thus, $2 / 4+5 / y=1$
$\Rightarrow 5 / y=1 / 2$
$\Rightarrow y=10$

## 21. Question

Solve the following systems of equations:
$\frac{1}{5 x}+\frac{1}{6 y}=12$
$\frac{1}{3 x}-\frac{3}{7 y}=8, \quad x \neq 0, y \neq 0$
Answer
$\frac{1}{5 x}+\frac{1}{6 y}=12$
$\frac{1}{3 x}-\frac{3}{7 y}=8, \quad x \neq 0, y \neq 0$
Multiplying eq1 by $1 / 3$ and eq2 by $1 / 5$ and subtracting
$\Rightarrow 1 / 18 y+3 / 35 y=4-8 / 5$
$\Rightarrow 89 / 630 y=12 / 5$
$\Rightarrow y=89 / 1512$
Thus, $1 / 5 x+1512 / 534=12$
$\Rightarrow 1 / 5 x=816 / 89$
$\Rightarrow x=89 / 4080$

## 22. Question

Solve the following systems of equations:
$\frac{2}{x}+\frac{3}{y}=\frac{9}{x y}$
$\frac{4}{x}+\frac{9}{y}=\frac{21}{x y}$, where, $x \neq 0, y \neq 0$

## Answer

$\frac{2}{x}+\frac{3}{y}=\frac{9}{x y}$
$\Rightarrow \frac{2 y+3 x}{x y}=\frac{9}{x y}$
$\Rightarrow 2 y+3 x=9$----- (1)
$\frac{4}{x}+\frac{9}{y}=\frac{21}{x y}$, where, $x \neq 0, y \neq 0$
$\Rightarrow \frac{4 y+9 x}{x y}=\frac{21}{x y}$
$\Rightarrow 4 y+9 x=21---(2)$
Multiplying eq1 by 2 and subtracting it from eq 2 we get,
$\Rightarrow 4 y+9 x-2(2 y+3 x)=21-2(9) \Rightarrow 4 y+9 x-4 y-6 x=21-18 \Rightarrow 3 x=3$
$\Rightarrow \mathrm{x}=1$
Put the value of $x$ in 1 to get,
Thus, $2 \mathrm{y}+3(1)=92 \mathrm{y}+3=92 \mathrm{y}=9-32 \mathrm{y}=6 \mathrm{y}=3$
hence $x=1$ and $y=3$

## 23. Question

Solve the following systems of equations:
$\frac{6}{x+y}=\frac{7}{x-y}+3$
$\frac{1}{2(x+y)}=\frac{1}{3(x-y)}$
where, $x+y \neq 0$ and $x-y \neq 0$
Answer
Given : the following systems of equations:
$\frac{6}{x+y}=\frac{7}{x-y}+3$
$\frac{1}{2(x+y)}=\frac{1}{3(x-y)}$
To find : The value of $x$ and $y$.

## Solution :

Take $\frac{1}{x+y}=u$ and $\frac{1}{x-y}=v$

The equations become: $6 u=7 v+36 u-7 v=3 \ldots \ldots$ (3)And, $\frac{1}{2} u=\frac{1}{3} v$
$\Rightarrow 3 u=2 v \quad 3 u-2 v=0 \ldots \ldots$ (4)To find the value of $u$ and $v$, Multiply eq. 4 with 2 and subtract it from eq. $3 \Rightarrow 6 u-7 v-2(3 u-$
$2 v)=3-0 \Rightarrow 6 u-7 v-6 u+4 v=3 \Rightarrow-3 v=3 \Rightarrow v=-1$ Put the value of $v$ in eq. 4 to get, $\Rightarrow 3 u-2(-1)=0 \Rightarrow 3 u+2=0 \Rightarrow 3 u=-2 u=\frac{-2}{3}$
Now,
$\Rightarrow u=\frac{1}{x+y}=\frac{-2}{3}$
$\Rightarrow \frac{1}{x+y}=\frac{-2}{3}$
$\Rightarrow 3=-2(x+y) \Rightarrow 3=-2 x-2 y$
$\Rightarrow v=\frac{1}{x-y}=-1$
$\Rightarrow \frac{1}{x-y}=-1$
$\Rightarrow x-y=-1 \ldots$ (6)Multiply eq. 6 with 2 and add to eq. $5 \Rightarrow 2(x-y)+(-2 x-2 y)=-2+3 \Rightarrow-2 y-2 y-2 x-2 y=1 \Rightarrow-4 y=1 \Rightarrow y=\frac{-1}{4}$ Now put the value of y in eq. 6 to get $x-\left(\frac{-1}{4}\right)$
$x+\frac{1}{4}=-1$
$x=-1-\frac{1}{4}$
$x=\frac{-4-1}{4}$
$\Rightarrow x=\frac{-5}{4}$
Hence the values are $x=\frac{-5}{4}, y=\frac{-1}{4}$.

## 24. Question

Solve the following systems of equations:
$\frac{x y}{x+y}=\frac{6}{5}$
$\frac{x y}{y-x}=6$ where, $x+y \neq 0$ and $x-y \neq 0$
Answer
$\frac{x y}{x+y}=\frac{6}{5}$
$\frac{x y}{y-x}=6$
Dividing the two equations
$\Rightarrow(y-x) /(x+y)=1 / 5$
$\Rightarrow 5 y-5 x=x+y$
$\Rightarrow y=3 x / 2$
Thus, $x \times \frac{\frac{3 x}{2}}{x+\frac{3 x}{2}}=\frac{6}{5}$
$\Rightarrow 3 x / 5=6 / 5$
$\Rightarrow \mathrm{x}=2$
Thus, $y=3$
25. Question

Solve the following systems of equations:
$\frac{22}{x+y}+\frac{15}{x-y}=5$
$\frac{55}{x+y}+\frac{45}{x-y}=14$
Answer
$\frac{22}{x+y}+\frac{15}{x-y}=5$
$\frac{55}{x+y}+\frac{45}{x-y}=14$
Multiplying eq1 by 3 and subtracting from eq2
$\Rightarrow-11 /(x+y)=-1$
$\Rightarrow x+y=11$
Multiplying eq1 by 5 and eq2 by 2 and subtracting
$\Rightarrow 15 /(x-y)=3$
$\Rightarrow x-y=5-----$
$(3)+(4)$
$\Rightarrow 2 x=16$
$\Rightarrow x=8$
Thus, $\mathrm{y}=3$

## 26. Question

Solve the following systems of equations:
$\frac{5}{x+y}-\frac{2}{x-y}=-1$
$\frac{15}{x+y}+\frac{7}{x-y}=10$
Answer
$\frac{5}{x+y}-\frac{2}{x-y}=-1$
$\frac{15}{x+y}+\frac{7}{x-y}=10$
Multiplying eq1 by 3 and subtracting from eq2
$\Rightarrow 13 /(x-y)=13$
$\Rightarrow x-y=1$------
Multiplying eq 1 by 7 and eq 2 by 2 and adding
$\Rightarrow 65 /(x+y)=13$
$\Rightarrow x+y=5$
Thus, $2 x=6$
$\Rightarrow \mathrm{x}=3$
$Y=x-1$
$\Rightarrow y=2$
27. Question

Solve the following systems of equations:
$\frac{3}{x+y}+\frac{2}{x-y}=2$
$\frac{9}{x+y}-\frac{4}{x-y}=1$
Answer
$\frac{3}{x+y}+\frac{2}{x-y}=2$
$\frac{9}{x+y}-\frac{4}{x-y}=1$
Multiplying eq1 by 2 and adding to eq2
$\Rightarrow 15 /(x+y)=5$
$\Rightarrow x+y=3$
Multiplying eq1 by 3 and subtracting eq 2 from it
$\Rightarrow 10 /(x-y)=5$
$\Rightarrow x-y=2$----
Adding the two equation
$\Rightarrow 2 x=5$
$\Rightarrow x=5 / 2$
Thus, $y=1 / 2$

## 28. Question

Solve the following systems of equations:
$\frac{1}{2(x+2 y)}+\frac{5}{3(3 x-2 y)}=\frac{-3}{2}$
$\frac{5}{4(x+2 y)}-\frac{4}{5(3 x-2 y)}=\frac{73}{60}$

## Answer

$\frac{1}{2(x+2 y)}+\frac{5}{3(3 x-2 y)}=\frac{-3}{2}$
$\frac{5}{4(x+2 y)}-\frac{4}{5(3 x-2 y)}=\frac{73}{60}$
Multiplying eq1 by $5 / 2$ and subtracting from eq 2
$\Rightarrow-\frac{4}{5(3 x-2 y)}-\frac{25}{6(3 x-2 y)}=\frac{73}{60}+\frac{15}{4}$
$\Rightarrow-\frac{149}{30(3 x-2 y)}=\frac{298}{60}$
$\Rightarrow 3 x-2 y=-1------$
Multiplying eq1 by $12 / 25$ and adding to eq2
$\Rightarrow \frac{6}{25(x+2 y)}+\frac{5}{4(x+2 y)}=-\frac{18}{25}+\frac{73}{60}$
$\Rightarrow \frac{149}{100(x+2 y)}=\frac{149}{300}$
$\Rightarrow x+2 y=3$
Solving (3) and (4)
We get, $x=1 / 2$ and $y=5 / 4$
29. Question

Solve the following systems of equations:
$\frac{5}{x+1}-\frac{2}{y-1}=\frac{1}{2}$
$\frac{10}{x+1}+\frac{2}{y-1}=\frac{5}{2}$ where, $x \neq-1, y \neq 1$
Answer
$\frac{5}{x+1}-\frac{2}{y-1}=\frac{1}{2}$
$\frac{10}{x+1}+\frac{2}{y-1}=\frac{5}{2}$
Adding eq1 and eq2
$\Rightarrow 15 /(x+1)=3$
$\Rightarrow x+1=5$
$\Rightarrow \mathrm{x}=4$
Thus, $5 / 5-2 /(y-1)=12$
$\Rightarrow y-1=4$
$\Rightarrow y=5$

## 30. Question

Solve the following systems of equations:
$x+y=5 x y$
$x+2 y=13 x y, \quad x \neq 0, y \neq 0$

## Answer

$x+y=5 x y$
$x+2 y=13 x y, \quad x \neq 0, y \neq 0$
Subtracting the two eq.
$\Rightarrow-y=-8 x y$
$\Rightarrow x=1 / 8$
Thus, $1 / 8+y=5 y / 8$
$\Rightarrow y=1 / 3$

## 31. Question

Solve the following systems of equations:
$x+y=2 x y$
$\frac{x-y}{x y}=6, x \neq 0, y \neq 0$
Answer
$x+y=2 x y$
$x-y=6 x y$
Adding the two equation
$\Rightarrow 2 \mathrm{x}=8 \mathrm{xy}$
$\Rightarrow y=1 / 4$
Thus, $x+1 / 4=2 \times x \times 1 / 4$
$\Rightarrow x / 2=-1 / 4$
$\Rightarrow x=-1 / 2$

## 32. Question

Solve the following systems of equations:
$2(3 u-v)=5 u v$
$2(u+3 v)=5 u v$

## Answer

$2(3 u-v)=5 u v$
$2(u+3 v)=5 u v$
Equating both equations
$\Rightarrow 6 \mathrm{u}-2 \mathrm{v}=2 \mathrm{u}+6 \mathrm{v}$
$\Rightarrow u=2 v$
Substituting value of $u$
$\Rightarrow 2(6 v-v)=5 \times 2 v \times v$
$\Rightarrow \mathrm{v}=1$
Thus, $2(3 u-1)=5 u$
$\Rightarrow 6 \mathrm{u}-2=5 \mathrm{u}$
$\Rightarrow u=2$

## 33. Question

Solve the following systems of equations:
$\frac{2}{3 x+2 y}+\frac{3}{3 x-2 y}=\frac{17}{5}$
$\frac{5}{3 x+2 y}+\frac{1}{3 x-2 y}=2$
Answer
$\frac{2}{3 x+2 y}+\frac{3}{3 x-2 y}=\frac{17}{5}$
$\frac{5}{3 x+2 y}+\frac{1}{3 x-2 y}=2$
Multiplying eq 1 by 5 and eq 2 by 2 and subtracting
$\Rightarrow 13 /(3 x-2 y)=13$
$\Rightarrow 3 x-2 y=1------$
Multiplying eq 2 by 3 and subtracting eq1 from it
$\Rightarrow 13 /(3 x+2 y)=13 / 5$
$\Rightarrow 3 x+2 y=5$
$(3)+(4)$
$\Rightarrow 6 x=6$
$\Rightarrow \mathrm{x}=1$
Thus, $3+2=5$
$\Rightarrow y=1$

## 34. Question

Solve the following systems of equations:
$\frac{4}{x}+3 y=14$
$\frac{3}{x}-4 y=23$
Answer
$\frac{4}{x}+3 y=14$
$\frac{3}{x}-4 y=23$
Multiply eq 1 by 4 and eq2 by 3 and adding
$\Rightarrow 25 / x=125$
$\Rightarrow x=1 / 5$
Thus, $20+3 y=14$
$\Rightarrow y=-2$

## 35. Question

Solve the following systems of equations:
$99 x+101 y=499$
$101 x+99 y=501$
Answer
$99 x+101 y=499$
$101 x+99 y=501$
Adding both equations
$\Rightarrow 200 x+200 y=1000$
$\Rightarrow x+y=5$
Subtracting both equation
$\Rightarrow 2 \mathrm{y}-2 \mathrm{x}=-2$
$\Rightarrow \mathrm{x}-\mathrm{y}=1$
Adding 1 and 2
$\Rightarrow 2 \mathrm{x}=6$
$\Rightarrow \mathrm{x}=3$
Thus, $3+y=5$
$\Rightarrow y=2$

## 36. Question

Solve the following systems of equations:
$23 x-29 y=98$
$29 x-23 y=110$

## Answer

$23 x-29 y=98$
$29 x-23 y=110$
Adding both equation
$\Rightarrow 52 x-52 y=208$
$\Rightarrow x-y=4$----
Subtracting both equation
$\Rightarrow-6 x-6 y=-12$
$\Rightarrow x+y=12$----- (2)
$(1)+(2)$
$\Rightarrow 2 x=16$
$\Rightarrow x=8$
Thus, $y=4$

## 37. Question

Solve the following systems of equations:
$x-y+z=4$
$x-2 y+3 z=9$
$2 x+y+3 z=1$

## Answer

$x-y+z=4$
$x-2 y+3 z=9$
$2 x+y+3 z=1$
Subtracting eq2 and eq3
$\Rightarrow x+3 y=0$
$\Rightarrow x=-3 y$
Substituting in eq1
$\Rightarrow-3 y-y+z=4$
$\Rightarrow z=4+4 y$
Substituting in eq2
$\Rightarrow-3 y-2 y+12+12 y=1$
$\Rightarrow 7 y=-11$
$\Rightarrow y=-11 / 7$
Thus, $x=33 / 7$
And $z=4-44 / 7=-16 / 7$

## 38. Question

Solve the following systems of equations:
$x-y+z=4$
$x+y+z=2$
$2 x+y-3 z=0$
Answer
$x-y+z=4$
$x+y+z=2$
$2 x+y-3 z=0$
Adding eq 1 and eq2
$\Rightarrow 2(x+z)=6$
$\Rightarrow \mathrm{x}=3-\mathrm{z}$
$(3)-(2)-(1)$
$\Rightarrow y-5 z=-4$
$\Rightarrow y=-4+5 z$
Substituting in eq2
$\Rightarrow 3-z-4+5 z+z=2$
$\Rightarrow 5 z=3$
$\Rightarrow z=3 / 5$
Thus, $x=3-z$
$\Rightarrow x=12 / 5$
$Y=5 z-4$
$\Rightarrow y=-1$

## 39. Question

Solve the following systems of equations:
$\frac{44}{x+y}+\frac{30}{x-y}=10$
$\frac{55}{x+y}+\frac{40}{x-y}=13$
Answer
$\frac{44}{x+y}+\frac{30}{x-y}=10$
$\frac{55}{x+y}+\frac{40}{x-y}=13$
Multiplying eq1 by 5 and eq2 by 4 and subtracting
$\Rightarrow-10 /(x-y)=-2$
$\Rightarrow x-y=5$
Multiply eq1 by 4 and eq2 by 3 and subtracting
$\Rightarrow 11 /(x+y)=1$
$\Rightarrow(x+y)=11$
Thus, $2 x=16$
$\Rightarrow x=8$
$\therefore y=8-5=3$


## 40. Question

Solve the following systems of equations:
$\frac{4}{x}+5 y=7$
$\frac{3}{x}+4 y=5$
Answer
$\frac{4}{x}+5 y=7$
$\frac{3}{x}+4 y=5$
Multiply eq 1 by 4 and eq 2 by 5 and subtracting
$\Rightarrow 1 / x=3$
$\Rightarrow x=1 / 3$
Thus, $12+5 y=7$
$\Rightarrow y=1$

## 41. Question

Solve the following systems of equations:
$\frac{2}{x}+\frac{3}{y}=13$
$\frac{5}{x}-\frac{4}{y}=-2$
Answer
$\frac{2}{x}+\frac{3}{y}=13$
$\frac{5}{x}-\frac{4}{y}=-2$
Multiplying eq1 by 4 and eq2 by 3 and adding
$\Rightarrow 23 / x=46$
$\Rightarrow x=1 / 2$
Thus, $4+3 / y=13$
$\Rightarrow y=1 / 3$

## 42. Question

Solve the following systems of equations:
$\frac{5}{x-1}+\frac{1}{y-2}=2$
$\frac{6}{x-1}-\frac{3}{y-2}=1$
Answer
Given : The system of equations:
$\frac{6}{x-1}-\frac{3}{y-2}=1$
To find: The values of $x$ and $y$
Solution: Let $\frac{1}{x-y}=u$ and $\frac{1}{y-2}=v$
Now system of equations become:
$5 u+v=2$ $\qquad$ (1) $6 u-3 v=1$

Now multiply equation (1) by 3 and add to equation (2), $3(5 u+v)+6 u-3 v=3(2)+115 u+3 v+6 u-3 v=6+121 u=7$
$u=\frac{7}{21}$
$u=\frac{1}{3}$
so, $u=\frac{1}{x-1}=\frac{1}{3}$
$\Rightarrow \mathrm{x}-1=3 \Rightarrow \mathrm{x}=3+1 \Rightarrow \mathrm{x}=4$ Now put $u=\frac{1}{3}$ in the equation (1) to get v ,
$\frac{5}{3}+v=2$
$v=2-\frac{5}{3}$
$v=\frac{6-5}{3}$
$v=\frac{1}{3}$
So, $v=\frac{1}{y-2}=\frac{1}{3}$
$\Rightarrow y-2=3 \Rightarrow y=3+2 \Rightarrow y=5$ Hence the values are $x=4$ and $y=5$.

## 43. Question

Solve the following systems of equations:
$\frac{10}{x+y}+\frac{2}{x-y}=4$
$\frac{15}{x+y}-\frac{9}{x-y}=-2$
Answer
$\frac{10}{x+y}+\frac{2}{x-y}=4$
$\frac{15}{x+y}-\frac{9}{x-y}=-2$
Multiplying eq 1 by 9 and eq 2 by 2 and adding
$\Rightarrow 120 /(x+y)=32$
$\Rightarrow x+y=15 / 4$---- (1)
Multiplying eq 1 by 3 and eq 2 by 2 and subtracting
$\Rightarrow 24 /(x-y)=16$
$\Rightarrow x-y=3 / 2$---- (2)
Adding (1) and (2)
$\Rightarrow 2 \mathrm{x}=21 / 4$
$\Rightarrow x=21 / 8$
Thus, $21 / 8-y=3 / 2$
$\Rightarrow y=9 / 8$

## 44. Question

Solve the following systems of equations:
$\frac{1}{3 x+y}+\frac{1}{3 x-y}=\frac{3}{4}$
$\frac{1}{2(3 x+y)}-\frac{1}{2(3 x-y)}=-\frac{1}{8}$
Answer
$\frac{1}{3 x+y}+\frac{1}{3 x-y}=\frac{3}{4}$
$\frac{1}{2(3 x+y)}-\frac{1}{2(3 x-y)}=-\frac{1}{8}$
Multiplying eq2 by 2 and adding to eq1
$\Rightarrow 2 /(3 x+y)=3 / 4-2 / 8$
$\Rightarrow 3 x+y=4---$
Multiplying eq2 by 2 and subtracting from eq1
$\Rightarrow 2 /(3 x-y)=1$
$\Rightarrow 3 x-y=2$---- (4)
Adding (3) and (4)
$\Rightarrow 6 x=6$
$\Rightarrow x=1$
Thus, $y=3-2=1$

## 45. Question

Solve the following systems of equations:
$\frac{2}{\sqrt{x}}+\frac{3}{\sqrt{y}}=2$
$\frac{4}{\sqrt{x}}-\frac{9}{\sqrt{y}}=-1$
Answer
$\frac{2}{\sqrt{x}}+\frac{3}{\sqrt{y}}=2$
$\frac{4}{\sqrt{x}}-\frac{9}{\sqrt{y}}=-1$
Multiplying eq1 by 3 and adding to eq2
$\Rightarrow 10 / \sqrt{ } \mathrm{x}=5$
$\Rightarrow \sqrt{ } \mathrm{x}=2$
$\Rightarrow \mathrm{x}=4$
Thus,
$\Rightarrow 2 / \sqrt{ } 4+3 / \sqrt{ } y=2$
$\Rightarrow y=9$

## 46. Question

Solve the following systems of equations:
$\frac{7 x-2 y}{x y}=5$
$\frac{8 x+7 y}{x y}=15$
Answer
$\frac{7 x-2 y}{x y}=5$
$\Rightarrow 7 / y-2 / x=5----$
$\frac{8 x+7 y}{x y}=15$
$\Rightarrow 8 / y+7 / x=15----$
Multiplying eq 1 by 7 and eq 2 by 2 and adding
$\Rightarrow 65 / y=65$
$\Rightarrow y=1$
Thus, $7-2 / x=5$
$\Rightarrow \mathrm{x}=1$

## 47. Question

Solve the following systems of equations:
$152 x-378 y=-74$
$-378 x+158 y=-604$
Answer
$152 x-378 y=-74$
$-378 x+158 y=-604$
Adding (1) and (2)
$\Rightarrow-226 x-226 y=-678$
$\Rightarrow x+y=3----$
(1) - (2)
$\Rightarrow 530 x-530 y=530$
$\Rightarrow x-y=1$------ (4)
Adding (3) and (4)
$\Rightarrow 2 \mathrm{x}=4$
$\Rightarrow x=2$
Thus, $\mathrm{y}=1$

## Exercise 3.4

## 1. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$x+2 y+1=0$
$2 x-3 y-12=0$
Answer
Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $x+2 y+1=0$
$2 x-3 y-12=0$
$\frac{x}{-24+3}=\frac{y}{2+12}=\frac{1}{-3-4}$
$\Rightarrow \mathrm{x}=-21 /-7=3$
$\Rightarrow y=14 /-7=-2$

## 2. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$3 x+2 y+25=0$
$2 x+y+10=0$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $3 x+2 y+25=0$
$2 x+y+10=0$
$\therefore \frac{x}{2 \times 10-1 \times 25}=\frac{y}{2 \times 25-3 \times 10}=\frac{1}{3 \times 1-2 \times 2}$
$\Rightarrow \frac{x}{-5}=\frac{y}{20}=-1$
$\Rightarrow x=5$ and $y=-20$

## 3. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$2 x+y=35$
$3 x+4 y=65$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $2 x+y=35$
$3 x+4 y=65$
$\frac{x}{-65+140}=\frac{y}{-105+130}=\frac{1}{8-3}$
$\Rightarrow x=75 / 5=15$
$\Rightarrow y=25 / 5=5$

## 4. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$2 x-y=6$
$x-y=2$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $2 x-y=6$
$x-y=2$
$\frac{x}{2-6}=\frac{y}{-6+4}=\frac{1}{-2+1}$
$\Rightarrow x=-4 /-1=4$
$\Rightarrow y=-2 /-1=2$

## 5. Question

Solve each of the following systems of equations by the method of cross-multiplication: $\frac{x+y}{x y}=2, \frac{x-y}{x y}=6$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$\frac{x+y}{x y}=2, \quad \frac{x-y}{x y}=6$
$\Rightarrow \frac{1}{x}+\frac{1}{y}=2,-\frac{1}{x}+\frac{1}{y}=6$
$\frac{\frac{1}{x}}{-6+2}=\frac{\frac{1}{y}}{2+6}=\frac{1}{1+1}$
$\Rightarrow 1 / x=-2$
$\Rightarrow x=-1 / 2$
Also, $1 / \mathrm{y}=4$
$\Rightarrow y=1 / 4$

## 6. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$a x+b y=a-b$
$b x-a y=a+b$

## Answer

Method of cross multiplication
$a_{1} x+b_{1} y+c_{1}=0$
$a_{2} x+b_{2} y+c_{2}=0$
$\frac{x}{b_{1} c_{2}-b_{2} c_{1}}=\frac{-y}{a_{1} c_{2}-a_{2} c_{1}}=\frac{1}{a_{1} b_{2}-a_{2} b_{1}}$
Given,
$a x+b y=a-b$
$b x-a y=a+b$
This can be written as:
$a x+b y-(a-b)=0 b x-a y-(a+b)=0 S o$,
$\frac{x}{(b)(-(a+b))-(-a)(-(a-b))}=\frac{1-y}{a(-(a+b))-b(-(a-b))}=\frac{1}{a(-a)-b(b)}$
$\frac{x}{(b)(-a-b)+a(b-a)}=\frac{-y}{a(-a-b) \angle b(b-a)}=\frac{1}{-a^{2}-b^{2}}$
$\frac{x}{-b a-b^{2}+a b-a^{2}}=\frac{-y}{-a^{2}-a b-b^{2}+a b}=\frac{1}{-a^{2}-b^{2}}$
$\frac{x}{-b^{2}-a^{2}}=\frac{-y}{-a^{2}-b^{2}}=\frac{1}{-a^{2}-b^{2}}$
$\frac{x}{-b^{2}-a^{2}}=\frac{y}{a^{2}+b^{2}}=\frac{1}{-a^{2}-b^{2}}$
$\frac{x}{-b^{2}-a^{2}}=\frac{1}{-a^{2}-b^{2}}$ and $\frac{y}{a^{2}+b^{2}}=\frac{1}{-a^{2}-b^{2}}$
$x=\frac{-b^{2}-a^{2}}{-a^{2}-b^{2}}$ and $y=\frac{a^{2}+b^{2}}{-a^{2}-b^{2}}$
$x=\frac{-b^{2}-a^{2}}{-a^{2}-b^{2}}$ and $y=\frac{-\left(-a^{2}-b^{2}\right)}{-a^{2}-b^{2}}$
$\Rightarrow \mathrm{x}=1$ and $\mathrm{y}=-1$

## 7. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$x+a y=b$
$a x-b y=c$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $x+a y=b$
$a x-b y=c$
$\frac{x}{-a c-b^{2}}=\frac{y}{-a b+c}=\frac{1}{-b-a^{2}}$
$\Rightarrow x=\frac{a c+b^{2}}{a^{2}+b}$
$\Rightarrow y=\frac{a b+c}{a^{2}+b}$

## 8. Question

Solve each of the following systems of equations by the method of cross-multiplication:

$$
\begin{aligned}
& a x+b y=a^{2} \\
& b x+a y=b^{2}
\end{aligned}
$$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $a x+b y=a^{2}$
$b x+a y=b^{2}$
$\Rightarrow \frac{x}{-b^{3}+a^{3}}=\frac{y}{-b a^{2}+a b^{2}}=\frac{1}{a^{2}-b^{2}}$
$\Rightarrow x=\frac{a^{3}-b^{3}}{a^{2}-b^{2}}$
$\Rightarrow x=\frac{(a-b)\left(a^{2}+a b+b^{2}\right)}{(a-b)(a+b)}=\frac{a^{2}+a b+b^{2}}{a+b}$
$y=\frac{a b(b-a)}{(a-b)(a+b)}=-\frac{a b}{a+b}$

## 9. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{x}{a}+\frac{y}{b}=2$
$a x-b y=a^{2}-b^{2}$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$\frac{x}{a}+\frac{y}{b}=2$
$a x-b y=a^{2}-b^{2}$
$\frac{x}{\frac{b^{2}-a^{2}}{b}-2 b}=\frac{y}{-2 a+\frac{a^{2}-b^{2}}{a}}=\frac{1}{-\frac{b}{a}-\frac{a}{b}}$
$\Rightarrow \frac{\frac{x}{-a^{2}-b^{2}}}{b}=\frac{\frac{y}{-a^{2}-b^{2}}}{a}=\frac{\frac{1}{-a^{2}-b^{2}}}{a b}$
$\Rightarrow \mathrm{x}=\mathrm{a}$ and $\mathrm{y}=\mathrm{b}$

## 10. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{x}{a}+\frac{y}{b}=a+b$
$\frac{x}{a^{2}}+\frac{y}{b^{2}}=2$
Answer
Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $\frac{x}{a}+\frac{y}{b}=a+b$
$\frac{x}{a^{2}}+\frac{y}{b^{2}}=2$
$\frac{x}{-\frac{2}{b}+\frac{a+b}{b^{2}}}=\frac{y}{-\frac{a+b}{a^{2}}+\frac{2}{a}}=\frac{1}{\frac{1}{a b^{2}}-\frac{1}{a^{2} b}}$
$\Rightarrow \frac{\frac{x}{a-b}}{b^{2}}=\frac{\frac{y}{a-b}}{a^{2}}=\frac{1}{\frac{1}{a^{2} b^{2}}(a-b)}$
$\Rightarrow x=a^{2}, y=b^{2}$

## 11. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{x}{a}=\frac{y}{b}$
$a x+b y=a^{2}+b^{2}$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $\frac{x}{a}=\frac{y}{b}$
$a x+b y=a^{2}+b^{2}$
$\Rightarrow \frac{\frac{x}{a^{2}+b^{2}}}{b}=\frac{\frac{y}{a^{2}+b^{2}}}{a}=\frac{1}{\frac{b}{a}+\frac{a}{b}}$
$\Rightarrow \frac{\frac{x}{a^{2}+b^{2}}}{b}=\frac{\frac{y}{a^{2}+b^{2}}}{a}=\frac{a b}{a^{2}+b^{2}}$
$\Rightarrow \mathrm{x}=\mathrm{a}$ and $\mathrm{y}=\mathrm{b}$

## 12. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{5}{x+y}-\frac{2}{x-y}=-1$
$\frac{15}{x+y}+\frac{7}{x-y}=10$ where $x \neq 0$ and $y \neq 0$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$\frac{5}{x+y}-\frac{2}{x-y}=-1$
$\frac{15}{x+y}+\frac{7}{x-y}=10$
Multiplying eq1 by 3 and subtracting from eq2
$\Rightarrow \frac{13}{x-y}=13$
$\Rightarrow x-y=1$-------
Multiplying eq 2 by 2 and eq1 by 7 and adding
$\Rightarrow 65 /(x+y)=13$
$\Rightarrow x+y=5$
Thus,
$\frac{x}{5+1}=\frac{y}{-1+5}=\frac{1}{1+1}$
$\Rightarrow x=6 / 2=3$ and $y=4 / 2=2$

## 13. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{2}{x}+\frac{3}{y}=13$
$\frac{5}{x}-\frac{4}{y}=-2$ where $x \neq 0$ and $y \neq 0$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $\frac{2}{x}+\frac{3}{y}=13$
$\frac{5}{x}-\frac{4}{y}=-2$
$\Rightarrow \frac{\frac{1}{x}}{6-52}=\frac{\frac{1}{y}}{-65-4}=\frac{1}{-8-15}$
$\Rightarrow 1 / x=2$
$\Rightarrow x=1 / 2$
Also, $1 / y=3$
$\Rightarrow y=1 / 3$

## 14. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$a x+b y=\frac{a+b}{2}$
$3 x+5 y=4$
Answer
Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$a x+b y=\frac{a+b}{2}$
$3 x+5 y=8$
$\Rightarrow \frac{x}{-4 b+\frac{(5 a+5 b)}{2}}=\frac{y}{\frac{-3 a-3 b}{2}+4 a}=\frac{1}{5 a-3 b}$
$\Rightarrow \frac{2 x}{5 a-3 b}=\frac{2 y}{5 a-3 b}=\frac{1}{5 a-3 b}$
$\Rightarrow x=1 / 2, y=1 / 2$

## 15. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$2 a x+3 b y=a+2 b$
$3 a x+2 b y=2 a+b$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $2 a x+3 b y=a+2 b$
$3 a x+2 b y=2 a+b$
$\Rightarrow \frac{x}{-6 a b-3 b^{2}+2 a b+4 b^{2}}=\frac{y}{-3 a^{2}-6 a b+4 a^{2}+2 a b}=\frac{1}{4 a b-9 a b}$
$\Rightarrow \frac{x}{b^{2}-4 a b}=\frac{y}{a^{2}-4 a b}=\frac{1}{-5 a b}$
$\Rightarrow x=\frac{4 a-b}{5 a}, y=\frac{4 b-a}{5 b}$

## 16. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$5 a x+6 b y=28$
$3 a x+4 b y=18$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $5 a x+6 b y=28$
$3 a x+4 b y=18$
$\frac{x}{-108 b+112 b}=\frac{y}{-84 a+90 a}=\frac{1}{20 a b-18 a b}$
$\Rightarrow \frac{x}{4 b}=\frac{y}{6 a}=\frac{1}{2 a b}$
$\Rightarrow x=2 / a$ and $y=3 / b$

## 17. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$(a+2 b) x+(2 a-b) y=2$
$(a-2 b) x+(2 a+b) y=3$

## Answer

Method of cross multiplication

$$
\begin{aligned}
& a 1 x+b 1 y+c 1=0 \\
& a 2 x+b 2 y+c 2=0
\end{aligned}
$$

$$
\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}
$$

$$
(a+2 b) x+(2 a-b) y=2
$$

$$
(a-2 b) x+(2 a+b) y=3
$$

$$
\Rightarrow \frac{x}{3 b-6 a+4 a+2 b}=\frac{y}{3 a+6 b-2 a+4 b}
$$

$$
=\frac{1}{(2 a+b)(a+2 b)-(a-2 b)(2 a-b)}
$$

$$
\Rightarrow \frac{x}{5 b-2 a}=\frac{y}{a+10 b}=\frac{1}{2 a^{2}+a b+4 a b+2 b^{2}-\left(2 a^{2}-a b-4 a b+2 b^{2}\right)}
$$

$$
=\frac{1}{10 a b}
$$

$$
\Rightarrow x=\frac{5 b-2 a}{10 a b}, y=\frac{a+10 b}{10 a b}
$$

## 18. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$x\left(a-b+\frac{a b}{a-b}\right)=y\left(a+b-\frac{a b}{a-b}\right)$
$x+y=2 a^{2}$
Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
$x\left(a-b+\frac{a b}{a-b}\right)=y\left(a+b-\frac{a b}{a-b}\right)$
$x+y=2 a^{2}$
$\Rightarrow \frac{x}{2 a^{2} \times \frac{a^{2}-b^{2}-a b}{a-b}}=\frac{y}{2 a^{2} \times \frac{a^{2}+b^{2}-a b}{a-b}}=\frac{1}{\left(\frac{a^{2}+b^{2}-a b}{a-b}+\frac{a^{2}-b^{2}-a b}{a-b}\right)}$
$\Rightarrow \frac{x}{2 a^{2}\left(a^{2}-b^{2}-a b\right)}=\frac{y}{2 a^{2}\left(a^{2}+b^{2}-a b\right)}=\frac{1}{2 a(a-b)}$
$\Rightarrow x=\frac{a\left(a^{2}-b^{2}-a b\right)}{a-b}, y=\frac{a\left(a^{2}+b^{2}-a b\right)}{a-b}$

## 19. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$b x+c y=a+b \quad a x\left(\frac{1}{a-b}-\frac{1}{a+b}\right)+c y\left(\frac{1}{b-a}-\frac{1}{b+a}\right)=\frac{2 a}{a+b}$

## Answer

Method of cross multiplication

$$
\begin{aligned}
& a 1 x+b 1 y+c 1=0 \\
& a 2 x+b 2 y+c 2=0
\end{aligned}
$$

$$
\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}
$$

$$
b x+c y=a+b \quad a x\left(\frac{1}{a-b}-\frac{1}{a+b}\right)+c y\left(\frac{1}{b-a}-\frac{1}{b+a}\right)=\frac{2 a}{a+b}
$$

$$
\Rightarrow \frac{x}{-\frac{2 a c}{a+b}+(a+b) \times c \times \frac{2 a}{b^{2}-a^{2}}}=\frac{y}{-(a+b) \times a \times \frac{2 b}{a^{2}-b^{2}}+\frac{2 a b}{a+b}}
$$

$$
=\frac{1}{-b c \times \frac{2 a}{a^{2}-b^{2}}-a c \times \frac{2 b}{a^{2}-b^{2}}}
$$

$$
\Rightarrow \frac{x}{-\frac{2 a c}{a+b}-\frac{2 a c}{a-b}}=\frac{y}{\frac{2 a b}{a+b}-\frac{2 a b}{a-b}}=\frac{1}{-\frac{4 a b c}{a^{2}-b^{2}}}
$$

$$
\Rightarrow \frac{x}{-2 a c \times \frac{2 a}{a^{2}-b^{2}}}=\frac{y}{2 a b \times-\frac{2 b}{a^{2}-b^{2}}}=\frac{1}{-\frac{4 a b c}{a^{2}-b^{2}}}
$$

$$
\Rightarrow x=\frac{a}{b}, y=\frac{b}{c}
$$

## 20. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$(a-b) x+(a+b) y=2 a^{2}-2 b^{2}$
$(a+b)(x+y)=4 a b$

## Answer

Method of cross multiplication:For the system of equations:

$$
\begin{aligned}
& a_{1} \mathrm{x}+\mathrm{b}_{1} \mathrm{y}+\mathrm{c}_{1}=0 \mathrm{a}_{2} \mathrm{x}+\mathrm{b}_{2} \mathrm{y}+\mathrm{c}_{2}=0 \\
& \frac{x}{b_{1} c_{2}-b_{2} c_{1}}=\frac{y}{c_{1} a_{2}-c_{2} a_{1}}=\frac{1}{a_{1} b_{2}-a_{2} b_{1}}
\end{aligned}
$$

Here, $a_{1}=(a-b), b_{1}=(a+b), c_{1}=2 b^{2}-2 a^{2} a_{2}=(a+b), b_{2}=(a+b), c_{2}=-4 a b S o$,

$$
\begin{aligned}
& \Rightarrow \frac{x}{(a+b)(-4 a b)-(a+b)\left(2 b^{2}-2 a^{2}\right)}=\frac{y}{\left(2 b^{2}-2 a^{2}\right)(a+b)-(-4 a b)(a-b)}=\frac{1}{(a-b)(a+b)-(a+b)(a+b)} \\
& \Rightarrow \frac{x}{(a+b)(-4 a b)-2(a+b)\left(b^{2}-a^{2}\right)}=\frac{y}{2\left(b^{2}-a^{2}\right)(a+b)+4 a b(a-b)}=\frac{1}{(a+b)(a-b-a-b)}
\end{aligned}
$$

$$
\Rightarrow \frac{x}{2(a+b)\left[-2 a b-\left(b^{2}-a^{2}\right)\right]}=\frac{y}{2(b-a)(b+a)(a+b)+4 a b(a+b)}=\frac{1}{(a+b)(-2 b)}
$$

$$
\Rightarrow \frac{x}{-2(a+b)\left[2 a b+b^{2}-a^{2}\right]}=\frac{y}{2(b-a)\left[(a+b)^{2}-2 a b\right]}=\frac{1}{(a+b)(-2 b)}
$$

$$
\Rightarrow \frac{x}{-2(a+b)\left[2 a b+b^{2}-a^{2}\right]}=\frac{y}{2(b-a)\left[a^{2}+b^{2}+2 a b-2 a b\right]}=\frac{1}{(a+b)(-2 b)}
$$

$$
\Rightarrow \frac{x}{-2(a+b)\left[2 a b+b^{2}-a^{2}\right]}=\frac{y}{2(b-a)\left[a^{2}+b^{2}\right]}=\frac{1}{(a+b)(-2 b)}
$$

$$
\Rightarrow x=\frac{-2(a+b)\left[2 a b+b^{2}-a^{2}\right]}{(a+b)(-2 b)} \text { and } y=\frac{2(b-a)\left[a^{2}+b^{2}\right]}{(a+b)(-2 b)}
$$

$$
\Rightarrow x=\frac{\left[2 a b+b^{2}-a^{2}\right]}{b} \text { and } y=\frac{(a-b)\left[a^{2}+b^{2}\right]}{b(a+b)}
$$

## 21. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$a^{2} x+b^{2} y=c^{2}$
$b^{2} x+a^{2} y=a^{2}$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
$a^{2} x+b^{2} y=c^{2}$
$b^{2} x+a^{2} y=a^{2}$
$\Rightarrow \frac{x}{-b^{2} a^{2}+a^{2} c^{2}}=\frac{y}{-b^{2} c^{2}+a^{4}}=\frac{1}{a^{4}-b^{4}}$
$\Rightarrow x=\frac{a^{2} c^{2}-b^{2} a^{2}}{a^{4}-b^{4}}, y=\frac{a^{4}-b^{2} c^{2}}{a^{4}-b^{4}}$

## 22. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{57}{x+y}+\frac{6}{x-y}=5$
$\frac{38}{x+y}+\frac{21}{x-y}=9$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
$\frac{57}{x+y}+\frac{6}{x-y}=5$
$\frac{38}{x+y}+\frac{21}{x-y}=9$
$\Rightarrow \frac{\frac{1}{x+y}}{-6 \times 9+5 \times 21}=\frac{\frac{1}{x-y}}{-38 \times 5+57 \times 9}=\frac{1}{57 \times 21-6 \times 38}$
$\Rightarrow \mathrm{x}+\mathrm{y}=19$ and $\mathrm{x}-\mathrm{y}=8$
Solving the above two equation
$\Rightarrow x=11$ and $y=8$

## 23. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$2(a x-b y)+a+4 b=0$
$2(b x+a y)+b-4 a=0$
Answer
Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$2(a x-b y)+a+4 b=0$
$2 a x-2 b y+a+4 b=0$
$2(b x+a y)+b-4 a=0$
$2 b x+2 a y+b-4 a=0$
$\Rightarrow \frac{x}{(-2 b)(b-4 a)-2 a(a+4 b)}=\frac{y}{(2 b)(a+4 b)-(2 a)(b-4 a)}=\frac{1}{(2 a)(2 a)-(-2 b)(2 b)}$
$\Rightarrow \frac{x}{-2 b^{2}+8 a b-2 a^{2}-8 a b}=\frac{y}{2 a b+8 b^{2}-2 a b+8 a^{2}}=\frac{1}{4 a^{2}+4 b^{2}}$
$\Rightarrow \frac{x}{-2 b^{2}-2 a^{2}}=\frac{y}{8 b^{2}+8 a^{2}}=\frac{1}{4 a^{2}+4 b^{2}}$
$\Rightarrow \frac{x}{-2\left(b^{2}+a^{2}\right)}=\frac{y}{8\left(b^{2}+a^{2}\right)}=\frac{1}{4\left(a^{2}+b^{2}\right)}$
$\Rightarrow x=\frac{-2\left(b^{2}+a^{2}\right)}{4\left(a^{2}+b^{2}\right)}$ and $y=\frac{8\left(a^{2}+b^{2}\right)}{4\left(a^{2}+b^{2}\right)}$
$\Rightarrow x=\frac{-1}{2}$ and $y=2$

## 24. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$6(a x+b y)=3 a+2 b$
$6(b x-a y)=3 b-2 a$

## Answer

Method of cross multiplication

$$
\begin{aligned}
& a 1 x+b 1 y+c 1=0 \\
& a 2 x+b 2 y+c 2=0
\end{aligned}
$$

$$
\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}
$$

$$
6(a x+b y)=3 a+2 b
$$

$$
6(b x-a y)=3 b-2 a
$$

$$
\Rightarrow \frac{x}{6 b(2 a-3 b)-6 a(3 a+2 b)}=\frac{y}{-6 b(3 a+2 b)+6 a(3 b-2 a)}=\frac{1}{-36 a^{2}-3 b^{2}}
$$

$$
\Rightarrow \frac{x}{-18 a^{2}-18 b^{2}}=\frac{y}{-12 a^{2}-12 b^{2}}=\frac{1}{-36 a^{2}-36 b^{2}}
$$

$$
\Rightarrow x=1 / 2, y=1 / 3
$$

## 25. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{a^{2} b}{x}+\frac{b^{2} a}{y}=a+b, x, y \neq 0$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given,
$\frac{a^{2}}{x}-\frac{b^{2}}{y}=0$
$\frac{a^{2} b}{x}+\frac{b^{2} a}{y}=a+b, x, y \neq 0$
$\Rightarrow \frac{\frac{1}{x}}{b^{2}(a+b)}=\frac{\frac{1}{y}}{a^{2}(a+b)}=\frac{1}{a^{3} b^{2}+a^{2} b^{3}}$
$\Rightarrow \frac{\frac{1}{x}}{b^{2}(a+b)}=\frac{\frac{1}{y}}{a^{2}(a+b)}=\frac{1}{a^{2} b^{2}(a+b)}$
$\Rightarrow x=a^{2}, y=b^{2}$

## 26. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$m x-n y=m^{2}+n^{2}$
$x+y=2 m$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $m x-n y=m^{2}+n^{2}$
$x+y=2 m$
$\Rightarrow \frac{x}{2 m n+m^{2}+n^{2}}=\frac{y}{-m^{2}-n^{2}+2 m^{2}}=\frac{1}{m+n}$
$\Rightarrow \frac{x}{(m+n)^{2}}=\frac{y}{m^{2}-n^{2}}=\frac{1}{m+n}$
$\Rightarrow \mathrm{x}=\mathrm{m}+\mathrm{n}$ and $\mathrm{y}=\mathrm{m}-\mathrm{n}$

## 27. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{a x}{b}-\frac{b y}{a}=a+b$
$a x-b y=2 a b$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $\frac{a x}{b}-\frac{b y}{a}=a+b$
$a x-b y=2 a b$
$\Rightarrow \frac{x}{2 b^{2}-a b-b^{2}}=\frac{y}{-a^{2}-a b+2 a^{2}}=\frac{1}{-a+b}$
$\Rightarrow \frac{x}{b(b-a)}=\frac{y}{a(a-b)}=\frac{1}{b-a}$
$\Rightarrow x=b, y=-a$

## 28. Question

Solve each of the following systems of equations by the method of cross-multiplication:
$\frac{b}{a} x+\frac{a}{b} y=a^{2}+b^{2}$
$x+y=2 a b$

## Answer

Method of cross multiplication
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 y+c 2=0$
$\frac{x}{b 1 c 2-b 2 c 1}=\frac{y}{a 2 c 1-a 1 c 2}=\frac{1}{a 1 b 2-a 2 b 1}$
Given, $\frac{b}{a} x+\frac{a}{b} y=a^{2}+b^{2}$
$x+y=2 a b$
$\frac{x}{-2 a^{2}+a^{2}+b^{2}}=\frac{y}{-a^{2}-b^{2}+2 b^{2}}=\frac{1}{\frac{b}{a}-\frac{a}{b}}$
$\Rightarrow \frac{x}{b^{2}-a^{2}}=\frac{y}{b^{2}-a^{2}}=\frac{a b}{b^{2}-a^{2}}$
$\Rightarrow x=y=a b$

## Exercise 3.5

## 1. Question

In each of the following systems of equations determine whether the system has a unique solution, no solution or infinitely many solutions. In case there is a unique solution, find it:
$x-3 y=3$
$3 x-9 y=2$
Answer
$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 x+c 2=0$
if $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, infinite solution
if $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, no solution
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, unique solution
$x-3 y=3$
$3 x-9 y=2$
Thus, $\frac{1}{3}=\frac{1}{3} \neq \frac{3}{2}$
The system has no solution

## 2. Question

In each of the following systems of equations determine whether the system has a unique solution, no solution or infinitely many solutions. In case there is a unique solution, find it:
$2 x+y=5$
$4 x+2 y=10$

## Answer

$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 x+c 2=0$
if $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, infinite solution
if $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, no solution
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, unique solution
$2 x+y=5$
$4 x+2 y=10$
Thus, $\frac{1}{2}=\frac{1}{2}=\frac{1}{2}$
Infinitely many solution

## 3. Question

In each of the following systems of equations determine whether the system has a unique solution, no solution or infinitely many solutions. In case there is a unique solution, find it:

$$
\begin{aligned}
& 3 x-5 y=20 \\
& 6 x-10 y=40
\end{aligned}
$$

## Answer

$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 x+c 2=0$
if $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, infinite solution
if $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, no solution
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, unique solution
$3 x-5 y=20$
$6 x-10 y=40$
Thus, $\frac{1}{2}=\frac{1}{2}=\frac{1}{2}$
Infinitely many solution

## 4. Question

In each of the following systems of equations determine whether the system has a unique solution, no solution or infinitely many solutions. In case there is a unique solution, find it:
$x-2 y=8$
$5 x-10 y=10$

## Answer

$a 1 x+b 1 y+c 1=0$
$a 2 x+b 2 x+c 2=0$
if $\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$, infinite solution
if $\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, no solution
If $\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$, , nique solution
$x-2 y=8$
$5 x-10 y=10$
Thus, $\frac{1}{5}=\frac{1}{5} \neq \frac{4}{5}$
No solution.

## 5. Question

Find the value of $k$ for which the following system of equations has a unique solution:
$k x+2 y=5$
$3 x+y=1$

## Answer

$K x+2 y=5$
$3 x+y=1$
Multiplying eq2 by 2 and subtracting from eq1
$(k-6) x=3$
$\Rightarrow \mathrm{x}=3 /(\mathrm{k}-6)$
Thus, for $k \neq 6$ the system has unique solution

## 6. Question

Find the value of $k$ for which the following system of equations has a unique solution:
$4 x+k y+8=0$
$2 x+2 y+2=0$

## Answer

$4 x+k y+8=0$
$2 x+2 y+2=0$
Multiplying eq2 by 2 and subtracting from eq1
$\Rightarrow(\mathrm{k}-4) \mathrm{y}+6=0$
$\Rightarrow y=6 /(4-k)$
Thus, for $k \neq 4$ it has a unique solution

## 7. Question

Find the value of $k$ for which the following system of equations has a unique solution:
$4 x-5 y=k$
$2 x-3 y=12$

## Answer

Multiplying eq2 by 2 and subtracting from eq1
$\Rightarrow-5 y+6 y=k-24$
$\Rightarrow \mathrm{y}=\mathrm{k}-24$
Thus, for any value of $k$ it has a unique solution

## 8. Question

Find the value of $k$ for which the following system of equations has a unique solution:
$x+2 y=3$
$5 x+k y+7=0$

## Answer

$x+2 y=3$
$5 x+k y+7=0$
Multiplying eq1 by 5 and subtracting from eq2
$\Rightarrow(\mathrm{k}-10) \mathrm{y}=-22$
Thus for all $k$ except 10 it has a unique solution

## 9. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$2 x+3 y-5=0$
$6 x+k y-15=0$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y-5=0$
$6 x+k y-15=0$
$\Rightarrow \frac{2}{6}=\frac{3}{k}=\frac{5}{15}$
$\Rightarrow k=3 \times 3=9$

## 10. Question

Find the value of k for which each of the following systems of equations have infinitely many solution:
$4 x+5 y=3$
$k x+15 y=9$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$4 x+5 y=3$
$K x+15 y=9$
$\Rightarrow \frac{4}{k}=\frac{5}{15}=\frac{3}{9}$
$\Rightarrow \mathrm{k}=4 \times 3=12$

## 11. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$k x-2 y+6=0$
$4 x-3 y+9=0$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\mathrm{kx}-2 \mathrm{y}+6=0$
$4 x-3 y+9=0$
$\frac{k}{4}=\frac{2}{3}=\frac{6}{9}$
$\Rightarrow \mathrm{k}=4 \times 2 / 3=8 / 3$

## 12. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$8 x+5 y=9$
$k x+10 y=18$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$8 x+5 y=9$
$K x+10 y=18$
$\frac{8}{k}=\frac{5}{10}=\frac{9}{18}$
$\Rightarrow \mathrm{k}=2 \times 8=16$

## 13. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$2 x-3 y=7$
$(k+2) x-(2 k+1) y=3(2 k-1)$
Answer
Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x-3 y=7$
$(k+2) x-(2 k+1) y=3(2 k-1)$
$\frac{2}{k+2}=\frac{3}{2 k+1}=\frac{7}{3(2 k-1)}$
$\Rightarrow 4 \mathrm{k}+2=3 \mathrm{k}+6$
$\Rightarrow \mathrm{k}=4$

## 14. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$2 x+3 y=2$
$(k+1) x+9 y=k+1$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y=2$
$(k+1) x+9 y=k+1$
$\Rightarrow \frac{2}{k+1}=\frac{3}{9}=\frac{2}{k+1}$
$\Rightarrow \mathrm{k}+1=6$
$\Rightarrow \mathrm{k}=5$

## 15. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$x+(k+1) y=4$
$(k+1) x+9 y=5 k+2$
Answer
Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$x+(k+1) y=4$
$(k+1) x+9 y=5 k+2$
$\frac{1}{k+1}=\frac{k+1}{9}=\frac{4}{5 k+2}$
$\Rightarrow 5 \mathrm{k}+2=4 \mathrm{k}+4$
$\Rightarrow k=2$

## 16. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$k x+3 y=2 k+1$
$2(k+1) x+9 y=7 k+1$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$K x+3 y=2 k+1$
$2(k+1)+9 y=7 k+1$
$\frac{k}{2(k+1)}=\frac{3}{9}=\frac{2 k+1}{7 k+1}$
$\Rightarrow 9 \mathrm{k}=6 \mathrm{k}+6$
$\Rightarrow 3 \mathrm{k}=6$
$\Rightarrow \mathrm{k}=2$

## 17. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$2 x+(k-2) y=k$
$6 x+(2 k-1) y=2 k+5$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+(k-2) y=k$
$6 x+(2 k-1 y=2 k+5$
$\frac{2}{6}=\frac{k-2}{2 k-1}=\frac{k}{2 k+5}$
$\Rightarrow 4 \mathrm{k}-2=6 \mathrm{k}-12$
$\Rightarrow 2 \mathrm{k}=10$
$\Rightarrow \mathrm{k}=5$

## 18. Question

Find the value of k for which each of the following systems of equations have infinitely many solution:
$2 x+3 y=7$
$(k+1) x+(2 k-1) y=4 k+1$

## Answer

Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y=7$
$(k+1) x+(2 k-1) y=4 k+1$
$\frac{2}{k+1}=\frac{3}{2 k-1}=\frac{7}{4 k+1}$
$\Rightarrow 4 \mathrm{k}-2=3 \mathrm{k}+3$
$\Rightarrow \mathrm{k}=5$

## 19. Question

Find the value of $k$ for which each of the following systems of equations have infinitely many solution:
$2 x+3 y=k$
$(k-1) x+(k+2) y=3 k$
Answer
Infinitely many solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y=k$
$(k-1) x+(k+2) y=3 k$
$\frac{2}{k-1}=\frac{3}{2+k}=\frac{k}{3 k}$
$\Rightarrow 4+2 \mathrm{k}=3 \mathrm{k}-3$
$\Rightarrow \mathrm{k}=7$

## 20. Question

Find the value of $k$ for which the following system of equations has no solution:
$k x-5 y=2$
$6 x+2 y=7$

## Answer

No solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$k x-5 y=2$
$6 x+2 y=7$
$\frac{k}{6}=-\frac{5}{2}$
$\Rightarrow \mathrm{k}=-15$

## 21. Question

Find the value of $k$ for which the following system of equations has no solution:
$x+2 y=0$
$2 x+k y=5$

## Answer

No solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$x+2 y=0$
$2 x+k y=5$
$\frac{1}{2}=\frac{2}{k}$
$\Rightarrow \mathrm{k}=4$

## 22. Question

Find the value of $k$ for which the following system of equations has no solution:
$3 x-4 y+7=0$
$k x+3 y-5=0$

## Answer

No solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$3 x-4 y+7=0$
$k x+3 y-5=0$
$\frac{3}{k}=-\frac{4}{3}$
$\Rightarrow \mathrm{k}=-9 / 4$

## 23. Question

Find the value of $k$ for which the following system of equations has no solution:
$2 x-k y+3=0$
$3 x+2 y-1=0$

No solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$2 x-k y+3=0$
$3 x+2 y-1=0$
$\frac{2}{3}=-\frac{k}{2}$
$\Rightarrow \mathrm{k}=-4 / 3$

## 24. Question

Find the value of $k$ for which the following system of equations has no solution:
$2 x+k y=11$
$5 x-7 y=5$

## Answer

No solution will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$2 x+k y=11$
$5 x-7 y=5$
$\frac{2}{5}=-\frac{k}{7}$
$\Rightarrow \mathrm{k}=-14 / 5$

## 25. Question

Find the value of $k$ for which the following system of equations has no solution:
$k x+3 y=3$
$12 x+k y=6$
Answer
No solution will be when
$a 1 / b 1=b 1 / b 2 \neq C 1 / C 2$
$k x+3 y=3$
$12 x+k y=6$
$k / 12=3 / k$
$\Rightarrow \mathrm{k}= \pm 6$

## 26. Question

For what value of $k$ the following system of equations will be inconsistent?
$4 x+6 y=11$
$2 x+k y=7$
Answer

System will be inconsistent will be when
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$4 x+6 y=11$
$2 x+k y=7$
$\frac{4}{2}=\frac{6}{k} \neq \frac{11}{7}$
$\frac{4}{2}=\frac{6}{k}$
$\Rightarrow k=3$

## 27. Question

For what value of $a$, the system of equations is inconsistent
$a x+3 y=a-3$
$12 x+a y=a$

## Answer

System will be inconsistent will be when
$\mathrm{a} 1 / \mathrm{a} 2=\mathrm{b} 1 / \mathrm{b} 2 \neq \mathrm{c} 1 / \mathrm{c} 2$
$a x+3 y=a-3$
$12 x+a y=a$
$a / 12=3 / 1 \neq a-3 / a$
$\Rightarrow \mathrm{a}= \pm 6$
But +6 doesn't satisfy
$a / 12=3 / 1 \neq 1-3 / a$
Thus, $a=-6$

## 28. Question

Find the value of $k$ for which the system
$k x+2 y=5$
$3 x+y=1$
has (i) a unique solution, and (ii) no solution.

## Answer

$k x+2 y=5$
$3 x+y=1$
i) For unique solution:
$\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$\Rightarrow \frac{k}{3} \neq \frac{2}{1}$
$\Rightarrow \mathrm{k} \neq 6$
ii) For no solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$\Rightarrow \frac{k}{3}=\frac{2}{1}$
$\Rightarrow k=6$
29. Question

Prove that there is a value of $c(\neq 0)$ for which the system
$6 x+3 y=c-3$
$12 x+c y=c$
Has infinitely many solutions. Find this value.

## Answer

For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$6 x+3 y=c-3$
$12 x+c y=c$
$\frac{6}{12}=\frac{3}{c}$
$\Rightarrow c=6$

## 30. Question

Find the values of k for which the system
$2 x+k y=1$
$3 x-5 y=7$
Will have (i) a unique solution and (ii) no solution. Is there a value of $k$ for which the system has infinitely many solutions?

## Answer

$2 x+k y=1$
$3 x-5 y=7$
i) For unique solution:
$\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$\frac{2}{3} \neq \frac{k}{-5}$
$\Rightarrow k \neq-10 / 3$
ii) For no solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2} \neq \frac{c 1}{c 2}$
$\frac{2}{3}=\frac{k}{-5}$
$\Rightarrow \mathrm{k}=-10 / 3$
For infinite solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\Rightarrow \frac{2}{3}=\frac{k}{-5} \neq \frac{1}{7}$
Thus, for no value of $k$ will the system have infinite solution

## 31. Question

For what value of $k$, the following system of equations will represent the coincident lines?
$x+2 y+7=0$
$2 x+k y+14=0$

## Answer

For coincident lines
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$x+2 y+7=0$
$2 x+k y+14=0$
$\frac{1}{2}=\frac{2}{k}=\frac{7}{14}$
$\Rightarrow \mathrm{k}=4$

## 32. Question

Obtain the condition for the following system of linear equations to haye a unique solution

$$
\begin{aligned}
& a x+b y=c \\
& l x+m y=n
\end{aligned}
$$

## Answer

For unique solution:
$\frac{a 1}{a 2} \neq \frac{b 1}{b 2} \neq \frac{c 1}{c 2}$ Given
$a x+b y=c$
$l x+m y=n$
$\frac{a}{l} \neq \frac{b}{m}$
$\Rightarrow \mathrm{am} \neq \mathrm{lb}$ Hence the system of given linear equations will have unique solution when $\mathrm{am} \neq \mathrm{lb}$.

## 33. Question

Determine the values of $a$ and $b$ so that the following system of linear equations have infinitely many solutions:
$(2 a-1) x+3 y-5=0$
$3 x+(b-1) y-2=0$

## Answer

For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$(2 a-1) x+3 y-5=0$
$3 x+(b-1) y-2=0$
$\frac{2 a-1}{3}=\frac{3}{b-1}=\frac{5}{2}$
$\Rightarrow 2 \mathrm{a}-1=15 / 2$
$\Rightarrow \mathrm{a}=17 / 4$
$6=5 \mathrm{~b}-5$
$\Rightarrow \mathrm{b}=11 / 5$

## 34. Question

Find the values of $a$ and $b$ for which the following system of linear equations has infinite number of solutions:
$2 x-3 y=7$
$(a+b) x-(a+b-3) y=4 a+b$
Answer
For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x-3 y=7$
$(a+b) x-(a+b-3) y=4 a+b$
$\frac{2}{a+b}=\frac{3}{a+b-3}=\frac{7}{4 a+b}$
$\Rightarrow 2 \mathrm{a}+2 \mathrm{~b}-6=3 \mathrm{a}+3 \mathrm{~b}$ and $12 \mathrm{a}+3 \mathrm{~b}=7 \mathrm{a}+7 \mathrm{~b}-21$
$\Rightarrow a+b=-6----(1)$ and $5 a-4 b=-21$
Multiplying eq1 by 4 and adding to eq2
$\Rightarrow 9 \mathrm{a}=-45$
$\Rightarrow a=-5$
Thus, $\mathrm{b}=-1$

## 35. Question

Find the values of $p$ and $q$ for which the following system of linear equations has infinite number of solutions:
$2 x+3 y=9$
$(p+q) x-(2 p-q) y=3(p+q+1)$

## Answer

For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y=9$
$(p+q) x-(2 p-q) y=3(p+q+1)$
$\frac{2}{p+q}=\frac{3}{-(2 p-q)}=\frac{9}{p+q+1}$
$\Rightarrow-4 p+2 q=3 p+3 q$ and $2 p+2 q+2=9 p+9 q$
$\Rightarrow q=-7 p$ and $7 \mathrm{p}+7 q=2$
$\Rightarrow 7 q-q=2$
$\Rightarrow q=1 / 3$
Thus, $\mathrm{p}=-1 / 21$

## 36. Question

Find the values of $a$ and $b$ for which the following system of equations has infinitely many solutions:
(i) $(2 a-1) x-3 y=5$
$3 x+(b-2) y=3$
(ii) $2 x-(2 a+5 y) y=5$
$(2 b+1) x-9 y=15$
(iii) $(a-1) x+3 y=2$
$6 x+(1-2 b) y=6$
(iv) $3 x+4 y=12$
$(a+b) x+2(a-b) y=5 a-1$
(v) $2 x+3 y=7$
$(a-b) x+(a+b) y=3 a+b-2$
(vi) $2 x+3 y-7=0$
$(a-1) x+(a+1) y=(3 a-1)$
(vii) $2 x+3 y=7$
$(a-1) x+(a+2) y=3 a$
Answer
For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\frac{2 a-1}{3}=-\frac{3}{b-2}=\frac{5}{3}$
$\Rightarrow 6 \mathrm{a}-3=15$ and $-9=5 \mathrm{~b}-10$
$\Rightarrow \mathrm{a}=3$ and $\mathrm{b}=1 / 5$
(ii) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\frac{2}{2 b+1}=-\frac{2 a+5}{-9}=\frac{5}{15}$
$\frac{2}{2 b+1}=\frac{2 a+5}{9}=\frac{1}{3}$
$\Rightarrow 6=2 b+1$ and $6 a+15=9$
$\Rightarrow \mathrm{b}=5 / 2$ and $\mathrm{a}=-1$
(iii) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\frac{a-1}{6}=\frac{3}{1-2 b}=\frac{2}{6}$
$\Rightarrow \frac{a-1}{6}=\frac{3}{1-2 b}=\frac{1}{3}$
$\Rightarrow 3 \mathrm{a}-3=6$ and $9=1-2 \mathrm{~b}$
$\Rightarrow \mathrm{a}=3$ and $\mathrm{b}=-4$
(iv) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\frac{3}{a+b}=\frac{4}{2(a-b)}=\frac{12}{5 a-1}$
$\Rightarrow 15 \mathrm{a}-3=12 \mathrm{a}+12 \mathrm{~b}$ and $20 \mathrm{a}-4=24 \mathrm{a}-24 \mathrm{~b}$
$\Rightarrow 3 \mathrm{a}-12 \mathrm{~b}=3-----(1)$ and $6 \mathrm{~b}-\mathrm{a}=1-----$
Multiplying eq2 by 3 and adding to eq1
$\Rightarrow 6 b=6$
$\Rightarrow \mathrm{b}=1$
Thus, $3 \mathrm{a}-12=3$
$\Rightarrow \mathrm{a}=5$
(v) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\frac{2}{a-b}=\frac{3}{a+b}=\frac{7}{3 a+b-2}$
$\Rightarrow 2 \mathrm{a}+2 \mathrm{~b}=3 \mathrm{a}-3 \mathrm{~b}$ and $6 \mathrm{a}+2 \mathrm{~b}-4=7 \mathrm{a}-7 \mathrm{~b}$
$\Rightarrow \mathrm{a}=5 \mathrm{~b}$ and $9 \mathrm{~b}-\mathrm{a}=4$
Thus, $9 \mathrm{~b}-5 \mathrm{~b}=4$
$\Rightarrow \mathrm{b}=1$
$\Rightarrow \mathrm{a}=5$
(vi) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$2 x+3 y-7=0$
$(a-1) x+(a+1) y=(3 a-1)$
$\frac{2}{a-1}=\frac{3}{a+1}=-\frac{7}{-(3 a-1)}$
$\Rightarrow 2 a+2=3 a-3$
$\Rightarrow \mathrm{a}=5$
(vii) For infinitely many solution
$\frac{a 1}{a 2}=\frac{b 1}{b 2}=\frac{c 1}{c 2}$
$\Rightarrow \frac{2}{a-1}=\frac{3}{a+2}=\frac{7}{3 a}$
$\Rightarrow 2 \mathrm{a}+4=3 \mathrm{a}-3$
$\Rightarrow \mathrm{a}=7$

## Exercise 3.6

## 1. Question

5 pens and 6 pencils together cost Rs 9 and 3 pens and 2 pencils cost Rs 5 . Find the cost of 1 pen and 1 pencil.

## Answer

Let the cost of 1 pen be ' $a$ ' and the cost of 1 pencil be ' $b$ '.
Given, 5 pens and 6 pencils together cost Rs 9.
$5 a+6 b=9$ $\qquad$
Given, 3 pens and 2 pencils cost Rs 5 .
$3 a+2 b=5$ $\qquad$
Multiplying eq2 by 3 and subtracting eq1 from it. $3(3 a+2 b)-(5 a+6 b)=5(3)-9 \Rightarrow 9 a+6 b-5 a-6 b=15-9$
$\Rightarrow 4 \mathrm{a}=6$
$\Rightarrow a=3 / 2$
Substituting value of 'a' in (1)
$\Rightarrow 15 / 2+6 b=9$
$\Rightarrow 6 \mathrm{~b}=3 / 2$
$\Rightarrow \mathrm{b}=1 / 4$

## 2. Question

7 audio cassettes and 3 video cassettes cost Rs 1110, while 5 audio cassettes and 4 video cassettes cost Rs 1350 . Find the cost of an audio cassette and a video cassette.

## Answer

Let the cost of an audio cassette be ' $a$ ' and a video cassette be ' $b$ '.
Given, 7 audio cassettes and 3 video cassettes cost Rs 1110.
$\Rightarrow 7 \mathrm{a}+3 \mathrm{~b}=1110$ $\qquad$
Also, 5 audio cassettes and 4 video cassettes cost Rs 1350.
$\Rightarrow 5 \mathrm{a}+4 \mathrm{~b}=1350$
Multiplying eq 1 by 4 and eq 2 by 3 and subtracting eq 2 from eq1.
$\Rightarrow 28 a+12 b-15 a-12 b=4440-4050$
$\Rightarrow 13 \mathrm{a}=390$
$\Rightarrow \mathrm{a}=$ Rs. 30
Substituting value of a in eq1
$\Rightarrow 7 \times 30+3 \mathrm{~b}=1110$
$\Rightarrow 3 b=900$
$\Rightarrow \mathrm{b}=$ Rs. 300

## 3. Question

Reena has pens and pencils which together are 40 in number. If she has 5 more pencils and 5 less pens, then number of pencils would become 4 times the number of pens. Find the original number of pens and pencils.

## Answer

Let the number of pens be ' $a$ ' and number of pencils be ' $b$ '.
Given, Reena has pens and pencils which together are 40 in number. If she has 5 more pencils and 5 less pens, then number of pencils would become 4 times the number of pens.
$\Rightarrow \mathrm{a}+\mathrm{b}=40$
Also, $b+5=4(a-5)$
$\Rightarrow \mathrm{b}=4 \mathrm{a}-25$
Subtracting eq2 from eq1
$\Rightarrow \mathrm{a}+\mathrm{b}-\mathrm{b}=40-4 \mathrm{a}+25$
$\Rightarrow 5 \mathrm{a}=65$
$\Rightarrow a=13$
Substituting the value of 'a' in equation (1), we get $\Rightarrow 13+b=40 \Rightarrow b=27$
Hence, Reena has 13 pens and 27 pencils.

## 4. Question

4 tables and 3 chairs, together, cost Rs 2,250 and 3 tables and 4 chairs cost Rs 1950 . Find the cost of 2 chairs and 1 table.

## Answer

Let the cost of 1 table be ' $a$ ' and cost of 1 chair be ' $b$ '.
Given, 4 tables and 3 chairs, together, cost Rs 2,250 and 3 tables and 4 chairs cost Rs 1950.
$\Rightarrow 4 a+3 b=2250$ $\qquad$
Also, 3a $+4 b=1950$
Multiplying eq 1 by 3 and eq 2 by 4 and subtracting eq2 from eq1.
$\Rightarrow 12 a+9 b-12 a-16 b=6750-7800$
$\Rightarrow 7 b=1050$
$\Rightarrow b=150$
Substituting ' $b$ ' in eq1
$\Rightarrow 4 \mathrm{a}+450=2250$
$\Rightarrow \mathrm{a}=$ Rs. 450
Cost of 2 chair and 1 table $=2 b+a=$ Rs. 750

## 5. Question

3 bags and 4 pens together cost Rs 257 whereas 4 bags and 3 pens together cost Rs 324 . Find the total cost of 1 bag and 10 pens.

## Answer

Let the cost of 1 bag be ' $a$ ' and 1 pen be ' $b$ '.
Given, 3 bags and 4 pens together cost Rs 257 whereas 4 bags and 3 pens together cost Rs 324 .
$\Rightarrow 3 a+4 b=257$---------- (1) and $4 a+3 b=324$
Multiplying eq1 by 4 and eq2 by 3 and subtracting eq2 from eq1.
$\Rightarrow 12 a+16 b-12 a-9 b=1028-972$
$\Rightarrow 7 b=56$
$\Rightarrow \mathrm{b}=$ Rs. 8
Substituting in eq1
$\Rightarrow 3 \mathrm{a}+32=257$
$\Rightarrow a=R s .75$
Cost of 1 bag and 10 pens $=75+10 \times 8=$ Rs. 155

## 6. Question

5 books and 7 pens together cost Rs 79 whereas 7 books and 5 pens together cost Rs 77. Find the total cost of 1 book and 2 pens.

## Answer

Let the cost of 1 book be ' $a$ ' and cost of 1 pen be ' $b$ '.
Given, 5 books and 7 pens together cost Rs 79 whereas 7 books and 5 pens together cost Rs 77 .
$\Rightarrow 5 a+7 b=79-----(1)$ and $7 a+5 b=77$
Multiplying eq 1 by 7 and eq 2 by 5 and subtracting eq 2 from eq1.
$\Rightarrow 35 a+49 b-35 a-25 b=553-385$
$\Rightarrow 24 \mathrm{~b}=168$
$\Rightarrow \mathrm{b}=$ Rs. 7
Substituting value of $b$ in eq1, we get
$\Rightarrow 5 a+49=79$
$\Rightarrow \mathrm{a}=$ Rs. 6
Cost of 1 book and 2 pens $=6+2 \times 7=$ Rs. 20

## 7. Question

$A$ and $B$ each have a certain number of mangoes. A says to $B$, "if you give 30 of your mangoes, I will have twice as many as left with you." B replies, "if you give me 10, I will have thrice as many as left with you." How many mangoes does each have?

## Answer

Let the number of mangoes $A$ has be ' $a$ ' and number of mangoes $B$ has be ' $b$ '.
Given, . A says to B, "if you give 30 of your mangoes, I will have twice as many as left with you." B replies, "if you give me 10 , I will have thrice as many as left with you"
$\Rightarrow a+30=2(b-30)$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}-90$

Also, $b+10=3(a-10)$
$\Rightarrow \mathrm{b}=3 \mathrm{a}-40$
Substituting value of a from eq1 in eq2
$\Rightarrow b=6 b-270-40$
$\Rightarrow 5 b=310$
$\Rightarrow b=$ Rs. 62
Substituting value of $b$ in eq1
$\Rightarrow \mathrm{a}=124-90$
$\Rightarrow \mathrm{a}=$ Rs. 34

## 8. Question

On selling a T.V. at 5\% gain and a fridge at $10 \%$ gain, a shopkeeper gains Rs 2000. But if he sells the T.V. at $10 \%$ gain and the fridge at $5 \%$ loss. He gains Rs 1500 on the transaction. Find the actual prices of T.V. and fridge.

## Answer

Let the actual price of Tv be ' $a$ ' and actual price of fridge be ' $b$ '.
Given, on selling a T.V. at 5\% gain and a fridge at 10\% gain, a shopkeeper gains Rs 2000.
$\therefore 5 \%$ of $\mathrm{a}+10 \%$ of $\mathrm{b}=2000$
$\Rightarrow \frac{5}{100} a+\frac{10}{100} b=2000$
$\Rightarrow 5 \mathrm{a}+10 \mathrm{~b}=200000$
Also, if he sells the T.V. at 10\% gain and the fridge at 5\% loss.
$\therefore 10 \%$ of $\mathrm{a}-5 \%$ of $\mathrm{b}=1500$
$\Rightarrow \frac{10}{100} a-\frac{5}{100} b=1500$
$\Rightarrow 10 a-5 b=150000$
Multiplying eq 2 by 2 and adding eq 1 to it
$\Rightarrow 5 \mathrm{a}+10 \mathrm{~b}+20 \mathrm{a}-10 \mathrm{~b}=200000+300000$
$\Rightarrow 25 \mathrm{a}=500000$
$\Rightarrow \mathrm{a}=$ Rs. 20000
Thus, $5 \times 20000+10 b=200000$
$\Rightarrow b=$ Rs. 10000

## 9. Question

The coach of a cricket team buys 7 bats and 6 balls for Rs 3800 . Later, he buys 3 bats and 5 balls for Rs 1750 . Find the cost of each bat and each ball.

## Answer

Let the cost of each bat be ' $a$ ' and each ball be ' $b$ '.
Given, coach of a cricket team buys 7 bats and 6 balls for Rs 3800 . Later, he buys 3 bats and 5 balls for Rs 1750
$\Rightarrow 7 a+6 b=3800---$ (1) and
$3 a+5 b=1750---(2)$

Multiplying eq 1 by 3 and eq 2 by 7 and subtracting eq 2 from eq1.
$\Rightarrow 3(7 a+6 b)-7(3 a+5 b)=3(3800)-7(1750)$
$\Rightarrow 21 a+18 b-21 a-35 b=11400-12250$
$\Rightarrow-17 \mathrm{~b}=-850$
$\Rightarrow 17 \mathrm{~b}=850$
$\Rightarrow b=50$ Putting this in eq 1 , we get $7 \mathrm{a}+6(50)=3800 \Rightarrow 7 a+300=3800 \Rightarrow 7 a=3500 \Rightarrow a=500$ Hence, Each bat cost $a=$ 500 Rupees and Each ball costs $b=50$ Rupees.

## 10. Question

One says, "Give me a hundred, friend! I shall then become twice as rich as you." The other replies, "If you give me ten, I shall be six times as rich as you". Tell me what is the amount of their respective capital?

## Answer

Given: One says, "Give me a hundred, friend! I shall then become twice as rich as you." The other replies, "If you give me ten, I shall be six times as rich as you".

To find: the amount of their respective capital.
Solution:Let the capital of two friends be 'a'and 'b' respectively.
Given, one says, "Give me a hundred, friend! I shall then become twice as rich as you.It means if one is giving Rs. 100 other is losing the Rs. 100.Since $a$ is gaining 100 and $b$ is losing $100 . \Rightarrow a+100=2(b-100)$
$\Rightarrow \mathrm{a}+100=2 \mathrm{~b}-200$
$\Rightarrow \mathrm{a}-2 \mathrm{~b}=-200-100 \Rightarrow \mathrm{a}-2 \mathrm{~b}=-300 \quad \ldots .$. (1)In another condition 2 nd friend replies, "Give me a ten, I shall be six times as rich as you".It means if one person is gaining 10 other person is losing 10.

Here $b$ is gaining Rs 10 and $a$ is losing Rs $10 \Rightarrow b+10=6(a-10) \Rightarrow b+10=6 a-60 \Rightarrow 6 a-b=-60-10 \Rightarrow 6 a-b=-70$ $\ldots .$. (2)Now solve equations (1) and (2) to get the amount a and b.Multiply eq. (1) with 6 and subtract we. (2) from it. $\Rightarrow 6(a-2 b)-(6 a-b)=6(-300)-70 \Rightarrow 6 a-12 b-6 a+b=-1800-70 \Rightarrow-11 b=-1870 \Rightarrow b=170$ put the value of $b$ in the eq.(1) to get value of $a, \Rightarrow a-2(170)=-300 \Rightarrow a-340=-300 \Rightarrow a=-300+340 \Rightarrow a=40$

Hence the amount of capital of two friends is Rs 40 and Rs 170.

## 11. Question

A lending library has a fixed charge for the first three days and an additional charge for each day thereafter. Saritha paid Rs 27 for a book kept for seven days, while Susy paid Rs 21 for the book she kept for five days. Find the fixed charge and the charge for each extra day.

## Answer

Let the fixed charge and the charge for each extra day be 'a'and ' $b$ ' respectively.
Given, a lending library has a fixed charge for the first three days and an additional charge for each day thereafter
Saritha paid Rs 27 for a book kept for seven days $\Rightarrow a+4 b=27$ -
Susy paid Rs 21 for the book she kept for five days $\Rightarrow a+2 b=21$
Subtracting eq2 from eq1
$\Rightarrow 2 \mathrm{~b}=6$
$\Rightarrow \mathrm{b}=3$
Putting this value in eq(1), we get $\Rightarrow a+4(3)=27 \Rightarrow a=27-12 \Rightarrow a=15$ Therefore, fixed charge, $a=15$ Rupees and charge thereafter, $b=3$ Rupees per day
$\Rightarrow a=R s .15$

## Exercise 3.7

## 1. Question

The sum of two numbers is 8 . If their sum is four times their difference, find the number.

## Answer

Let the numbers be ' $a$ ' and ' $b$ '.
Given, sum of two numbers is 8 . If their sum is four times their difference, find the number.
$\Rightarrow \mathrm{a}+\mathrm{b}=8$
Also,
$a+b=4(a-b)$
$\Rightarrow \mathrm{a}+\mathrm{b}=4 \mathrm{a}-4 \mathrm{~b}$
$\Rightarrow a=5 b / 3$
Substituting value of a in eq1
$\Rightarrow 5 b / 3+b=8$
$\Rightarrow 8 \mathrm{~b} / 3=8$
$\Rightarrow \mathrm{b}=3$
Thus, $\mathrm{a}=5$

## 2. Question

The sum of digits of a two digit number is 13 . If the number is subtracted from the one obtained by interchanging the digits, the result is 45 . What is the number?

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '
Given, sum of digits of a two digit number is 13 . If the number is subtracted from the one obtained by interchanging the digits, the result is 45 .
$\Rightarrow \mathrm{a}+\mathrm{b}=13$----- (1) and,
$10 a+b-(10 b+a)=45$
$\Rightarrow 9 \mathrm{a}-9 \mathrm{~b}=45$
$\Rightarrow \mathrm{a}-\mathrm{b}=5$
Adding (1) and (2)
$\Rightarrow 2 \mathrm{a}=18$
$\Rightarrow \mathrm{a}=9$
Thus, $\mathrm{b}=4$
Number is $10 b+a$
$\Rightarrow$ Number $=49$

## 3. Question

A number consists of two digits whose sum is five. When the digits are reversed, the number becomes greater by nine. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '
Given, number consists of two digits whose sum is five. When the digits are reversed, the number becomes greater by nine.
$\Rightarrow a+b=5----(1)$ and
$10 a+b-(10 b+a)=9$
$\Rightarrow \mathrm{a}-\mathrm{b}=1$
Adding (1) and (2)
Thus, 2a $=6$
$\Rightarrow \mathrm{a}=3$
$\therefore \mathrm{b}=2$
Number is 23.

## 4. Question

The sum of digits of a two digit number is 15 . The number obtained by reversing the order of digits of the given number exceeds the given number by 9 . Find the given number.

## Answer

Let the unit's digit be $a$ and tens digit be $b$.
Number $=10 b+a$
Reverse of the number $=10 a+b$
Given, sum of digits of a two digit number is 15 .
$\Rightarrow \mathrm{a}+\mathrm{b}=15$ $\qquad$
Also, the number obtained by reversing the order of digits of the given number exceeds the given number by 9 .
$\Rightarrow 10 \mathrm{a}+\mathrm{b}-10 \mathrm{~b}-\mathrm{a}=9$
$\Rightarrow \mathrm{a}-\mathrm{b}=1$ $\qquad$
Solving (1) and (2), we get
$\Rightarrow \mathrm{a}=8$ and $\mathrm{b}=7$
The number is 78 .

## 5. Question

The sum of two-digit number and the number formed by reversing the order of digits is 66 . If the two digits differ by 2 , find the number. How many such numbers are there?

## Answer

Given : The sum of two-digit number and the number formed by reversing the order of digits is 66 and the two digits differ by 2 .

To find: the number. How many such numbers are there.
Solution:Let the one's digit be 'a' and ten's digit be 'b'. The 2 digit number is formed as ( $10 \times n u m b e r$ on tens' digit + number on one's digit )So the number is $10 b+a$, If we reverse the digits one's digit will be ' $b$ ' and tens' digit will be 'a'. So number after reversing will become $10 \mathrm{a}+\mathrm{b}$.

As it is given that sum of two-digit number and the number formed by reversing the order of digits is 66 .
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}+10 \mathrm{a}+\mathrm{b}=66$
$\Rightarrow 11 \mathrm{~b}+11 \mathrm{a}=66$
$\Rightarrow \mathrm{a}+\mathrm{b}=6$
Also, digits differ by 2 .
$\Rightarrow \mathrm{a}-\mathrm{b}=2 \ldots \ldots$ (2)or $\mathrm{b}-\mathrm{a}=2$

Adding eq 1 and 2 we geta $+b+a-b=6+2 \Rightarrow 2 a=8 \Rightarrow a=4$ Putting value of $a$ in 1 we get, $4+b=6 \Rightarrow b=6-4 \Rightarrow b=$ 2Adding eq 1 and 3 we geta $+b+b-a=6+2 \Rightarrow 2 b=8$
$\Rightarrow b=4$ Putting value of $a$ in 1 we get, $a+4=6 \Rightarrow a=6-4 \Rightarrow a=2$
Thus, $a=4$ and $b=2$ or $a=2$ and $b=4$ Now 2 digit number is $10 b+a F o r ~ a=4$ and $b=2$ The 2 digit number is 10 (2) $+4=20+4=24$ For $a=2$ and $b=4$ The 2 digit number is $10(4)+2=40+2=42$

Hence Numbers can be 24 or 42

## 6. Question

The sum of two numbers is 1000 and the difference between their squares is 256000 . Find the numbers.

## Answer

Let the numbers be ' $a$ ' and ' $b$ '
Given, of two numbers is 1000 and the difference between their squares is 256000
$\Rightarrow a+b=1000---$ (1) and
$\Rightarrow \mathrm{a}^{2}-\mathrm{b}^{2}=25600$
$\Rightarrow(a+b)(a-b)=25600 \quad[$ From 1]
$\Rightarrow 1000(\mathrm{a}-\mathrm{b})=256000$
$\Rightarrow \mathrm{a}-\mathrm{b}=256$----- (2)
Adding (1) and (2)
$\Rightarrow 2 \mathrm{a}=1256$
$\Rightarrow a=628$
From (1) $628+b=1000 \Rightarrow b=1000-628=372$

## 7. Question

The sum of a two digit number and the number obtained by reversing the order of its digits is 99 . If the digits differ by 3 , find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '
Given, sum of two-digit number and the number formed by reversing the order of digits is 99 .
$\Rightarrow 10 \mathrm{a}+\mathrm{b}+10 \mathrm{~b}+\mathrm{a}=99$
$\Rightarrow \mathrm{a}+\mathrm{b}=9$
Also, digits differ by 3.
$\Rightarrow \mathrm{a}-\mathrm{b}=3$ or $\mathrm{b}-\mathrm{a}=3$
Adding both equation
$2 \mathrm{a}=12$ or $2 \mathrm{~b}=12$
$\Rightarrow \mathrm{a}=6$ and $\mathrm{b}=3$ or $\mathrm{a}=3$ and $\mathrm{b}=6$
Number can be 36 or 63

## 8. Question

A two-digit number is 4 times the sum of its digits. If 18 is added to the number, the digits are reversed. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '

Given, number is 4 times the sum of its digits.
$10 b+a=4(a+b)$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}----(1)$
Also, if 18 is added to the number, the digits are reversed.
$\Rightarrow 10 b+a+18=10 a+b$
$\Rightarrow \mathrm{a}-\mathrm{b}=2$
Substituting a from eq1 in eq2
$\Rightarrow \mathrm{b}=2$
Thus, $\mathrm{a}=4$
Number is 24

## 9. Question

A two-digit number is 3 more than 4 times the sum of its digits. If 18 is added to the number, the digits are reversed. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '
Then, the number is $=10 b+a$
Given, the number is 3 more than 4 times the sum of its digits.
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}=4(\mathrm{a}+\mathrm{b})+3$
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}=4 \mathrm{a}+4 \mathrm{~b}+3$
$\Rightarrow 3 a=6 b-3$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}-1$
Also, if 18 is added to the number, the digits are reversed.
$\Rightarrow 10 b+a+18=10 a+b$
$\Rightarrow 9 \mathrm{a}-9 \mathrm{~b}=18$
$\Rightarrow \mathrm{a}-\mathrm{b}=2$ using (1)
$\Rightarrow 2 \mathrm{~b}-1-\mathrm{b}=2 \Rightarrow \mathrm{~b}=3$
Thus, again from (1)a = 6-1 = 5
Hence, Number is 35 .

## 10. Question

A two-digit number is 4 more than 6 times the sum of its digits. If 18 is subtracted from the number, the digits are reversed. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '
Given, two-digit number is 4 more than 6 times the sum of its digits.
$\Rightarrow 10 b+a=6(a+b)+4$
$\Rightarrow 4 b=5 a+4$
Also, if 18 is subtracted from the number, the digits are reversed.
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}-18=10 \mathrm{a}+\mathrm{b}$
$\Rightarrow \mathrm{b}-\mathrm{a}=2$
Multiplying eq2by 4 and subtracting from eq1
$\Rightarrow 4 b-5 a-4 b+4 a=4-8$
$\Rightarrow \mathrm{a}=4$
Thus, $\mathrm{b}=6$
Number is 64

## 11. Question

A two-digit number is 4 times the sum of its digits and twice the product of the digits. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '.
Given, two digit number is 4 times the sum of its digits and twice the product of the digits
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}=4(\mathrm{a}+\mathrm{b})$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}$
Also, $10 \mathrm{~b}+\mathrm{a}=2 \mathrm{ab}$
Substituting value of a.
$\Rightarrow 10 \mathrm{~b}+2 \mathrm{~b}=2 \times 2 \mathrm{~b} \times \mathrm{b}$
$\Rightarrow \mathrm{b}=3$
Thus, $\mathrm{a}=6$
Number is 36

## 12. Question

A two-digit number is such that the product of its digits is 20. If 9 is added to the number, the digits interchange their places. Find the number.

## Answer

Let the one's digit be 'a' and ten's digit be ' b ':
Given, two-digit number is such that the product of its digits is 20 .
$\Rightarrow \mathrm{ab}=20$-----
Also, if 9 is added to the number, the digits interchange their places.
$\Rightarrow 10 \mathrm{~b}+\mathrm{a}+9=10 \mathrm{a}+\mathrm{b}$
$\Rightarrow \mathrm{a}-\mathrm{b}=1$-----
Substituting value of a from eq1 in to eq2
$\Rightarrow 20 / \mathrm{b}-\mathrm{b}=1$
$\Rightarrow b^{2}+\mathrm{b}-20=0$
$\Rightarrow(b+5)(b-4)=0$
Thus, $\mathrm{b}=4$ and $\mathrm{a}=\mathrm{b}+1=5$
Number is 45.

## 13. Question

The difference between two numbers is 26 and one number is three times the other. Find them.

Answer
Let the numbers be a and b .
Given, difference between two numbers is 26 and one number is three times the other.
$\Rightarrow \mathrm{a}-\mathrm{b}=26 \quad[1]$ and $\mathrm{a}=3 \mathrm{~b} \quad$ [2]From [1] and [2], we get
$\Rightarrow 3 \mathrm{~b}-\mathrm{b}=26$
$\Rightarrow 2 b=26$
$\Rightarrow b=13$
Thus, $a=3 b=3(13)=39$

## 14. Question

The sum of the digits of a two-digit number is 9 . Also, nine times this number is twice the number obtained by reversing the order of the digits. Find the number.

## Answer

Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '.therefore no is $=10 b+$ Reversed no $=10 a+b$
Given, Sum of the digits of a two-digit number is 9 . Also, nine times this number is twice the number obtained by reversing the order of the digits.
$\Rightarrow \mathrm{a}+\mathrm{b}=9$ $\qquad$
And $9(10 b+a)=2(10 a+b)$
$\Rightarrow 90 b+9 a=20 a+2 b$
$\Rightarrow 88 \mathrm{~b}=11 \mathrm{a}$
$\Rightarrow \mathrm{a}=8 \mathrm{~b}$
Substituting value of a in eq1
$\Rightarrow 8 \mathrm{~b}+\mathrm{b}=9$
$\Rightarrow 9 b=9$
$\Rightarrow \mathrm{b}=1$
Thus, $a=8(1)=9$
Hence, no is $10(1)+8=18$

## 15. Question

Seven times a two-digit number is equal to four times the number obtained by reversing the digits. If the difference between the digits is 3 . Find the number.

## Answer

Given:Seven times a two-digit number is equal to four times the number obtained by reversing the digits and the difference between the digits is 3 .

To find: the number.
Solution:Let the one's digit be ' $a$ ' and ten's digit be ' $b$ '. The the number will be $10 b+a$ If the digits are reversed the number will be 10a+b

Given, seven times a two-digit number is equal to four times the number obtained by reversing the digits.
$\Rightarrow 7(10 b+a)=4(10 a+b) \Rightarrow 7(10 b)+7 a=4(10 a)+4 b \Rightarrow 70 b+7 a=40 a+4 b \Rightarrow 70 b-4 b=40 a-7 a$
$\Rightarrow 66 \mathrm{~b}=33 \mathrm{a}$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}$

Also, difference between the digits is 3
$\Rightarrow \mathrm{a}-\mathrm{b}=3$
Substitute value of a from (1)
$\Rightarrow 2 \mathrm{~b}-\mathrm{b}=3$
Thus, $b=3$
$\Rightarrow a=2 \times 3=6$
The number is $10 b+a=10(3)+6=36$
$\therefore$ Number is 36 .

## Exercise 3.8

## 1. Question

The numerator of a fraction is 4 less than the denominator. If the numerator is decreased by 2 and denominator is increased by 1 , then the denominator is eight times the numerator. Find the fraction.

## Answer

Let the numerator be $a$ and denominator be $b$.
Given, numerator of a fraction is 4 less than the denominator.
$\Rightarrow \mathrm{a}=\mathrm{b}-4$ $\qquad$
Also, if the numerator is decreased by 2 and denominator is increased by 1 , then the denominator is eight times the numerator.
$\Rightarrow b+1=8(a-2)$
$\Rightarrow b=8 a-17$--------
Substituting value of $b$ from (2) in (1).
$\Rightarrow a=8 a-17-4$
$\Rightarrow \mathrm{a}=3$
Thus, $\mathrm{b}=3+4=7$
Fraction is 3/7.

## 2. Question

A fraction becomes $9 / 11$ if 2 is added to both numerator and the denominator, it becomes $5 / 7$ if 2 is subtracted from both numerator and the denominator. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, fraction becomes $9 / 11$ if 2 is added to both numerator and the denominator, it becomes $5 / 7$ if 2 is subtracted from both numerator and the denominator
$\frac{\Rightarrow(a+2)}{b+2}=\frac{9}{11}$
$\Rightarrow 11 a+22=9 b+18$
$\Rightarrow 11 a=9 b-4$
Also, $\frac{a-2}{b-2}=\frac{5}{7}$
$\Rightarrow 7 \mathrm{a}-14=5 \mathrm{~b}-10$
$\Rightarrow 7 a-5 b=4$
Multiplying eq1 by 7 and eq2 by 11 and subtracting eq2 from eq1
$\Rightarrow 77 \mathrm{a}-63 \mathrm{~b}-77 \mathrm{a}+55 \mathrm{~b}=-28-44$
$\Rightarrow 8 b=72$
$\Rightarrow b=9$
Thus, $7 \mathrm{a}-45=4$
$\Rightarrow \mathrm{a}=7$
Fraction is $7 / 9$.

## 3. Question

A fraction becomes $1 / 3$ if 1 is subtracted from both its numerator and denominator. If 1 is added to both the numerator and denominator, it becomes $1 / 2$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, fraction becomes $1 / 3$ if 1 is subtracted from both its numerator and denominator. If 1 is added to both the numerator and denominator, it becomes $1 / 2$.
$\Rightarrow \frac{a-1}{b-1}=\frac{1}{3}$
$\Rightarrow 3 \mathrm{a}-3=\mathrm{b}-1$
$\Rightarrow \mathrm{b}=3 \mathrm{a}-2$------
Also, if 1 is added to both the numerator and denominator, it becomes $1 / 2$.
$\Rightarrow \frac{a+1}{b+1}=\frac{1}{2}$
$\Rightarrow \mathrm{b}=2 \mathrm{a}+1$
Equating (1) and (2)
$\Rightarrow 3 a-2=2 a+1$
$\Rightarrow a=3$
Thus, $b=7$
Fraction is $3 / 7$

## 4. Question

If we add 1 to the numerator and subtract 1 from the denominator, a fraction becomes 1 . It also becomes $1 / 2$ if we only add 1 to the denominator. What is the fraction?

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, if add 1 to the numerator and subtract 1 from the denominator, a fraction becomes 1 .
$\Rightarrow \frac{a+1}{b-1}=1$
$\Rightarrow \mathrm{a}=\mathrm{b}-2$
Also, it becomes $1 / 2$ if we only add 1 to the denominator.
$\Rightarrow \frac{a}{b+1}=\frac{1}{2}$
$\Rightarrow 2 \mathrm{a}=\mathrm{b}+1$
Subtracting eq 1 from eq 2
$\Rightarrow 2 \mathrm{a}-\mathrm{a}=\mathrm{b}+1-\mathrm{b}+2$
$\Rightarrow \mathrm{a}=3$
Thus, $\mathrm{b}=5$
Fraction is $3 / 5$

## 5. Question

If the numerator of a fraction is multiplied by 2 and the denominator is reduced by 5 the fraction becomes $6 / 5$. And, if the denominator is doubled and the numerator is increased by 8 , the fraction becomes $2 / 5$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, if the numerator of a fraction is multiplied by 2 and the denominator is reduced by 5 the fraction becomes $6 / 5$
$\Rightarrow \frac{2 a}{b-5}=\frac{6}{5}$
$\Rightarrow 10 a=6 b-30$
$\Rightarrow 5 a=3 b-15$
Also, if the denominator is doubled and the numerator is increased by 8 , the fraction becomes $2 / 5$
$\Rightarrow \frac{a+8}{2 b}=\frac{2}{5}$
$\Rightarrow 5 a+40=4 b$
Subtracting eq2 from eq1
$\Rightarrow 5 \mathrm{a}-5 \mathrm{a}-40=3 \mathrm{~b}-15-4 \mathrm{~b}$
$\Rightarrow \mathrm{b}=25$
Thus, 5a = 75-15
$\Rightarrow \mathrm{a}=12$
Fraction is $12 / 25$

## 6. Question

When 3 is added to the denominator and 2 is subtracted from the numerator a fraction becomes $1 / 4$. And, when 6 is added to numerator and the denominator is multiplied by 3 , it becomes $2 / 3$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, 3 is added to the denominator and 2 is subtracted from the numerator a fraction becomes $1 / 4$.
$\Rightarrow \frac{a-2}{b+3}=\frac{1}{4}$
$\Rightarrow 4 \mathrm{a}-8=\mathrm{b}+3$
$\Rightarrow 4 \mathrm{a}-\mathrm{b}=11$------
Also, when 6 is added to numerator and the denominator is multiplied by 3 , it becomes 2/3.
$\Rightarrow \frac{a+6}{3 b}=\frac{2}{3}$
$\Rightarrow 3 a+18=2 b$
$\Rightarrow a+6=2 b-$
Multiplying eq 2 by 4 and subtracting from eq1
$\Rightarrow 4 \mathrm{a}-\mathrm{b}-4 \mathrm{a}-24=11-8 \mathrm{~b}$
$\Rightarrow 7 b=35$
$\Rightarrow \mathrm{b}=5$
Thus, $\mathrm{a}=4$
Fraction is $4 / 5$

## 7. Question

The sum of a numerator and denominator of a fraction is 18 . If the denominator is increased by 2 , the fraction reduces to $1 / 3$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '
Given, sum of a numerator and denominator of a fraction is 18.
$\Rightarrow \mathrm{a}+\mathrm{b}=18$
Also, if the denominator is increased by 2 , the fraction reduces to $1 / 3$.
$\Rightarrow a /(b+2)=1 / 3$
$\Rightarrow 3 \mathrm{a}-\mathrm{b}=2$
Adding (1) and (2)
$\Rightarrow 4 a=20$
$\Rightarrow a=5$
Thus, $\mathrm{b}=13$
Fraction is $5 / 13$

## 8. Question

If 2 is added to the numerator of a fraction, it reduces to $1 / 2$ and if 1 is subtracted from the denominator, it reduces to $1 / 3$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '.
Given, if 2 is added to the numerator of a fraction, it reduces to $1 / 2$ and if 1 is subtracted from the denominator, it reduces to $1 / 3$
$\Rightarrow(a+2) / b=1 / 2$
$\Rightarrow 2 \mathrm{a}+4=\mathrm{b}$
Also, $a /(b-1)=1 / 3$
$\Rightarrow 3 \mathrm{a}+1=\mathrm{b}$
Subtracting eq2 from eq1
$\Rightarrow 2 a+4-3 a-1=b-b$
$\Rightarrow \mathrm{a}=3$

Thus, $\mathrm{b}=2 \mathrm{a}+4=10$
Fraction is $3 / 10$

## 9. Question

The sum of the numerator and denominator of a fraction is 4 more than twice the numerator. If the numerator and denominator are increased by 3, they are in the ratio 2:3. Determine the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '.
Given, sum of the numerator and denominator of a fraction is 4 more than twice the numerator. If the numerator and denominator are increased by 3 , they are in the ratio $2: 3$.
$\Rightarrow \mathrm{a}+\mathrm{b}=2 \mathrm{a}+4$
$\Rightarrow \mathrm{b}-\mathrm{a}=4$
Also, $\frac{a+3}{b+3}=\frac{2}{3}$
$\Rightarrow 3 a+9=2 b+6$
$\Rightarrow 3 \mathrm{a}-2 \mathrm{~b}=-3$
Multiplying eq1 by 2 and adding to eq1
$\Rightarrow 2 b-2 a+3 a-2 b=8-3$
$\Rightarrow a=5$
Thus $\mathrm{b}=9$
Fraction is 5/9

## 10. Question

The sum of the numerator and denominator of a fraction is 3 less than twice the denominator. If the numerator and denominator are decreased by 1 , the numerator becomes half the denominator. Determine the fraction.

## Answer

Let the numerator be 'a' and denominator be ' $b$ '
Given, sum of the numerator and denominator of a fraction is 3 less than twice the denominator.
$\Rightarrow \mathrm{a}+\mathrm{b}=2 \mathrm{~b}-3$
$\Rightarrow \mathrm{a}=\mathrm{b}-3$
Also, if the numerator and denominator are decreased by 1 , the numerator becomes half the denominator.
$\Rightarrow a-1=(b-1) / 2$
$\Rightarrow \mathrm{b}=2 \mathrm{a}-1$
Substituting value of $b$ in eq1.
$\Rightarrow \mathrm{a}=2 \mathrm{a}-1-3$
$\Rightarrow a=4$.
Thus, $b=2 \times 4-1=7$

## 11. Question

The sum of the numerator and denominator of a fraction is 12 . If the denominator is increased by 3 , the fraction becomes $1 / 2$. Find the fraction.

## Answer

Let the numerator be ' $a$ ' and denominator be ' $b$ '.
Given, sum of the numerator and denominator of a fraction is 12 . If the denominator is increased by 3 , the fraction becomes $1 / 2$.
$\Rightarrow \mathrm{a}+\mathrm{b}=12$
Also, $a /(b+3)=1 / 2$
$\Rightarrow 2 \mathrm{a}-\mathrm{b}=3$ $\qquad$
Adding eq1 and eq2
$\Rightarrow \mathrm{a}+\mathrm{b}+2 \mathrm{a}-\mathrm{b}=15$
$\Rightarrow 3 a=15$
$\Rightarrow \mathrm{a}=5$
Thus, $\mathrm{b}=7$
Fraction is $5 / 7$.

## Exercise 3.9

## 1. Question

A father is three times as old as his son. After twelve years, his age will be twice as that of his son then. Find their present ages.

## Answer

Given: A father is three times as old as his son. After twelve years, his age will be twice as that of his son.To find: The present age of father and his son. Solution: Let the present age of father be 'a' and present age of son be $b$.

Given, father is three times as old as his son.
$\Rightarrow \mathrm{a}=3 \mathrm{~b}----(1)$
Also, after twelve years, his age will be twice as that of his son then. 12 years later age of father will be $a+12$ and son will be $b+12$.
$\Rightarrow \mathrm{a}+12=2(\mathrm{~b}+12) \Rightarrow \mathrm{a}+12=2 \mathrm{~b}+24$
$\Rightarrow a=2 b+12$
Put the value of a from eq. (1)
$\Rightarrow 3 b=2 b+12$
$\Rightarrow 3 \mathrm{~b}-2 \mathrm{~b}=12$
$\Rightarrow b=12$
Put the value of $a$ in eq. 1 to get, $a=3 b a=3(12) a=36$
Thus, present age of father is 36 years and present age of son is 12 years.

## 2. Question

Ten years later, A will be twice as old as B and five years ago, A was three times as old as B. What are the present ages of $A$ and $B$ ?

## Answer

Let the present ages of $A$ and $B$ be ' $a$ ' and ' $b$ ' respectively.
Given, ten years later, A will be twice as old as B and five years ago, A was three times as old as B
$\Rightarrow a+10=2(b+10)$
$\Rightarrow a=2 b+10$

Also, $a-5=3(b-5)$
$\Rightarrow a=3 b-10$
Equating eq2 and eq1
$\Rightarrow 2 b+10=3 b-10$
$\Rightarrow \mathrm{b}=20$
Thus, $a=2 b+10=50$

## 3. Question

$A$ is elder to $B$ by 2 years. $A$ 's father $F$ is twice as old as $A$ and $B$ is twice as old as his sister $S$. If the ages of the father and sister differ by 40 years, find the age of $A$.

## Answer

Let the present ages of $A, B, F$ and $S$ be ' $a$ ', ' $b$ ', ' $c$ ' and ' $d$ ' respectively.
Given, $A$ is elder to $B$ by 2 years
$\Rightarrow \mathrm{a}=\mathrm{b}+2$
A's father $F$ is twice as old as $A$ and $B$ is twice as old as his sister $S$
$\Rightarrow \mathrm{c}=2 \mathrm{a}$ and $\mathrm{b}=2 \mathrm{~d}$ $\qquad$
Also, the ages of the father and sister differ by 40 years.
$\Rightarrow \mathrm{c}-\mathrm{d}=40$
From [2], we have

$$
\begin{aligned}
& \Rightarrow 2 \mathrm{a}-\mathrm{b} / 2=40 \\
& 2 a-\frac{(a-2)}{2}=40 \\
& \Rightarrow \frac{4 a-a+2}{2}=40 \\
& \Rightarrow 3 a+2=80 \\
& \Rightarrow 3 a=78 \\
& \Rightarrow a=26
\end{aligned}
$$

Hence, Age of ' A ' is 26 years.

## 4. Question

Six years hence a man's age will be three times the age of his son and three years ago he was nine times as old as his son. Find their present ages.

## Answer

Let the present age of man be 'a' and present age of son be b.
Given, Six years hence a man's age will be three times the age of his son and three years ago he was nine times as old as his son

$$
\begin{equation*}
\Rightarrow a+6=3(b+6) \tag{1}
\end{equation*}
$$

$\Rightarrow a=3 b+12$
Also, three years ago he was nine times as old as his son
$\Rightarrow a-3=9(b-3)$
$\Rightarrow a=9 b-24----(2)$
Equating eq1 and eq2
$\Rightarrow 3 b+12=9 b-24$
$\Rightarrow b=6$
Thus, $a=3 b+12=30$
Hence age of man is 30 yrs and age of son is 6 yrs .

## 5. Question

Ten years ago, a father was twelve times as old as his son and ten years hence, he will be twice as old as his son will be then. Find their present ages.

## Answer

Let the present age of father be ' $a$ ' and present age of son be $b$.
Given, ten years ago, a father was twelve times as old as his son and ten years hence, he will be twice as old as his son will be then.
$\Rightarrow \mathrm{a}-10=12(\mathrm{~b}-10)$
$\Rightarrow a=12 b+110-----$
Also, $a+10=2(b+10)$
$\Rightarrow a=2 b+10$
Equating eq1 and eq2.
$\Rightarrow 12 \mathrm{~b}+110=2 \mathrm{~b}+10$
$\Rightarrow \mathrm{b}=10$
Thus, $\mathrm{a}=30$

## 6. Question

The present age of a father is three years more than three times the age of the son. Three years hence father's age will be 10 years more than twice the age of the son. Determine their present ages.

## Answer

Let the father's age be 'a' and son's age be 'b'
Given, present age of a father is three years more than three times the age of the son.
$\Rightarrow a=3 b+3$
Also, three years hence father's age will be 10 years more than twice the age of the son.
$\Rightarrow a+3=2(b+3)+10$
$\Rightarrow a=2 b+13$
Equating (1) and (2), we get
$3 b+3=2 b+13$
$\Rightarrow \mathrm{b}=10$ years
Father's age (a) $=3 \times 10+3=33$

## 7. Question

A father is three times as old as his son. In 12 years time, he will be twice as old as hi son. Find the present ages of father and the son.

Answer
Let the present age of father be ' $a$ ' and present age of son be $b$.
Given, father is three times as old as his son. In 12 years time, he will be twice as old as hi son.
$\Rightarrow \mathrm{a}=3 \mathrm{~b}$ and
$a+12=2(b+12)$
$\Rightarrow 3 b+12=2 b+24$
$\Rightarrow \mathrm{b}=12$
Thus, $\mathrm{a}=36$

## 8. Question

Father's age is three times the sum of ages of his two children. After 5 years his age will be twice the sum of ages of two children. Find the age of father.

## Answer

Given: Father's age is three times the sum of ages of his two children. After 5 years his age will be twice the sum of ages of two children.

To find: the age of father.
Solution: Let the present age of father be 'a' and present sum of age of both sons be b.
Given, Father's age is three times the sum of ages of his two children.
$\Rightarrow a=3 b$
After 5 years his age will be twice the sum of ages of two children. So age of father will be $a+5$ and as there are two sons, age of both sons combined after 5 years will be $b+10$.
$\Rightarrow \mathrm{a}+5=2(\mathrm{~b}+10)$
Put the value of a in above equation,
$\Rightarrow 3 b+5=2 b+20$
$\Rightarrow 3 \mathrm{~b}-2 \mathrm{~b}=20-15$
$\Rightarrow \mathrm{b}=15$
Thus, $a=3 b=3(15)=45$ Hence father's present age is 45 years.

## 9. Question

Two years ago, a father was five times as old as his son. Two years later, his age will be 8 more than three times the age of the son. Find the present ages of father and son.

## Answer

Let the present age of father be ' $a$ ' and present age of son be $b$.
Given, two years ago, a father was five times as old as his son. Two years later, his age will be 8 more than three times the age of the son.
$\Rightarrow \mathrm{a}-2=5(\mathrm{~b}-2)$
$\Rightarrow \mathrm{a}=5 \mathrm{~b}-8$
Also, $a+2=3(b+2)+8$
$\Rightarrow \mathrm{a}=3 \mathrm{~b}+12$----- (2)
Equating (1) and (2)
$\Rightarrow 5 b-8=3 b+12$
$\Rightarrow b=10$
From [1], we havea $=5(10)-8$ Thus father's age, $a=50-8=42$ Years

## 10. Question

Five years ago, Nuri was thrice as old as Sonu. Ten years later, Nuri will be twice as old as Sonu. How old are Nuri and Sonu?

## Answer

Given: Five years ago, Nuri was thrice as old as Sonu. Ten years later, Nuri will be twice as old as Sonu.
To find: The age of Nuri and Sonu.
Solution:Let the present age of Nuri and his son be ' $a$ ' and ' $b$ ' respectively.
Given, Five years ago, Nuri was thrice as old as Sonu.
This implies age of Nuri and Sonu five years ago was a-5 and b-5.
$\Rightarrow \mathrm{a}-5=3(\mathrm{~b}-5)$
$\Rightarrow \mathrm{a}-5=3 \mathrm{~b}-15 \Rightarrow \mathrm{a}=3 \mathrm{~b}-15+5$
$\Rightarrow a=3 b-10$
Ten years later, Nuri will be twice as old as Sonu. This implies after ten years the age of Nuri and Sonu will be $a+10$ and $b$ +10 .
$\Rightarrow a+10=2(b+10)$
$\Rightarrow \mathrm{a}+10=2 \mathrm{~b}+20 \Rightarrow \mathrm{a}=2 \mathrm{~b}+20-10$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}+10$
Equating (1) and (2), we get
$3 b-10=2 b+10$
$\Rightarrow 3 \mathrm{~b}-2 \mathrm{~b}=10+10 \Rightarrow \mathrm{~b}=20$
Thus, $a=60-10=50$ Hence Nuri's present age is 50 years and Sonu's age is 20 years.

## 11. Question

The ages of two friends Ani and Biju differ by 3 years. Ani's father Dharam is twice as old as Ani and Biju as twice as old as his sister Cathy. The ages of Cathy and Dharam differ by 30 years. Find the ages of Ani and Biju.

## Answer

Let the ages of Ani, Biju, Dharam and Cathy be a, b, c and d respectively.
Given, ages of two friends Ani and Biju differ by 3 years. Ani's father Dharam is twice as old as Ani and Biju as twice as old as his sister Cathy. The ages of Cathy and Dharam differ by 30 years.
$a-b=3$
$c=2 a$ and $b=2 d$
$c-d=30$
Solving the above four equations
$\Rightarrow 2 \mathrm{a}-\mathrm{b} / 2=30$
$\Rightarrow 2 \mathrm{a}-\mathrm{a} / 2+3 / 2=30$
$\Rightarrow \mathrm{a}=19$
Thus, $\mathrm{b}=16$ years

## Exercise 3.10

## 1. Question

Points $A$ and $B$ are 70 km a part on a highway. A car starts from $A$ and another car starts from $B$ simultaneously. If they travel in the same direction, they meet in 7 hours, but if they travel towards each other, they meet in one hour. Find the speed of the two cars.

## Answer

Let the speed of car from $A$ be ' $a$ ' and of car from $B$ be ' $b$ '
Speed = distance/time
Relative speed of cars when moving in same direction $=a+b$
Relative speed of cars when moving in opposite direction $=a-b$
Given, if they travel in the same direction, they meet in 7 hours, but if they travel towards each other, they meet in one hour. $A$ and $B$ are 70 km a part on a highway
$\Rightarrow \mathrm{a}+\mathrm{b}=70$
Also, $a-b=70 / 7=10-----(2)$
Adding (1) and (2)
$\Rightarrow 2 \mathrm{a}=80$
$\Rightarrow \mathrm{a}=40 \mathrm{~km} / \mathrm{hr}$
Thus, $\mathrm{b}=40-10=30 \mathrm{~km} / \mathrm{hr}$

## 2. Question

A sailor goes 8 km downstream in 40 minutes and returns in 1 hour. Determine the speed of the sailor in still water and the speed of the current.

## Answer

Speed $=$ distance/time
Let the speed of sailor in still water be ' $a$ ' and speed of the current be ' $b$ '.
The relative speed of sailor going upstream $=a-b$
The relative speed of sailor going downstream $=a+b$
Given, sailor goes 8 km downstream in 40 minutes and returns in 1 hour.
$\Rightarrow a+b=\frac{8}{\frac{40}{60}}$
$\Rightarrow \mathrm{a}+\mathrm{b}=12$
Also,
$a-b=8 / 1=8$
Adding (1) and (2).
$\Rightarrow 2 \mathrm{a}=20$
$\Rightarrow \mathrm{a}=10 \mathrm{~km} / \mathrm{hr}$
Thus, $\mathrm{b}=12-10=2 \mathrm{~km} / \mathrm{hr}$

## So, speed of sailor is 10 km/h and current is $\mathbf{2} \mathbf{~ k m} / \mathrm{h}$.

## 3. Question

The boat goes 30 km upstream and 44 km downstream in 10 hours. In 13 hours, it can go 40 km upstream and 55 km downstream. Determine the speed of stream and that of the boat in still water.

## Answer

Given: The boat goes 30 km upstream and 44 km downstream in 10 hours. In 13 hours, it can go 40 km upstream and 55 km downstream.

To find: the speed of stream and that of the boat in still water.
Solution:Speed = distance/time
Let the speed of boat be ' $a$ ' and speed of stream be ' $b$ '
Relative speed of boat going upstream $=a-b$
Relative speed of boat going downstream $=a+b$
Given, boat goes 30 km upstream and 44 km downstream in 10 hours. In 13 hours, it can go 40 km upstream and 55 km downstreamand we know, time $=\frac{\text { speed }}{\text { distance }}$
$\Rightarrow \frac{30}{a-b}+\frac{44}{a+b}=10$
Also, $\frac{40}{a-b}+\frac{55}{a+b}=13$----- (2)
Now take, $\frac{1}{a-b}=u, \frac{1}{a+b}=v$
Eq 1 and 2 becomes $\Rightarrow 30 u+44 v=10$ Take 2 common out of above equation $\Rightarrow 15 u+22 v-5=0$
..... (3)and40 u + 55 $v-13=0 \ldots$. (4)Solve the equations by cross multiplication method
$\frac{u}{22 \times(-13)-55 \times(-5)}=\frac{-v}{15 \times(-13)-40 \times(-5)}=\frac{1}{15 \times(55)-40 \times(22)}$
$\frac{u}{-286+275}=\frac{-v}{-195+200}=\frac{1}{825-880}$
$\frac{u}{-11}=\frac{-v}{5}=\frac{1}{-55}$
$u=\frac{-11}{-55}, v=\frac{-5}{-55}$
$u=\frac{1}{5}, v=\frac{1}{11}$
$\Rightarrow a-b=5 \ldots$ (4) $a+b=11 \ldots$ (5)Add eq 4 and 5 to geta $-b+a+b=5+11 \Rightarrow 2 a=16 \Rightarrow a=8$ Substitute value of $a$ in eq 4 we get, $8-b=5 \Rightarrow b=8-5 \Rightarrow b=3$ Speed of boat $=8 \mathrm{~km} / \mathrm{hr}$ and speed of stream $=3 \mathrm{~km} / \mathrm{hr}$

## 4. Question

A boat goes 24 km upstream and 28 km downstream in 6 hrs . It goes 30 km upstream and 21 km downstream in $6 \frac{1}{2} \mathrm{hrs}$. Find the speed of the boat in still water and also speed of the stream.

## Answer

Speed $=$ distance/time
Let the speed of boat be ' $a$ ' and speed of stream be ' $b$ '

Relative speed of boat going upstream $=a-b$
Relative speed of boat going downstream $=a+b$
Given, boat goes 24 km upstream and 28 km downstream in 6 hrs . It goes 30 km upstream and 21 km downstream in $6 \frac{1}{2}$ hrs
$\Rightarrow \frac{24}{a-b}+\frac{28}{a+b}=6$
Also, $\frac{30}{a-b}+\frac{21}{a+b}=\frac{13}{2}$
Multiplying eq 1 by 3 and eq2 by 4 and (1) - (2)
$\Rightarrow \frac{72}{a-b}-\frac{120}{a-b}=-8$
$\Rightarrow \mathrm{a}-\mathrm{b}=6$
Substituting value of ( $a-b$ ) into eq1
$\Rightarrow \frac{24}{6}+\frac{28}{a+b}=6$
$\Rightarrow \mathrm{a}+\mathrm{b}=14$
From (1) and (2), we get
$\mathrm{a}=10 \mathrm{~km} / \mathrm{hr}$ and $\mathrm{b}=4 \mathrm{~km} / \mathrm{hr}$

## 5. Question

While covering distance of 30 km . Ajeet takes 2 hours more than Amit. If Ajeet doubles his speed, he would take 1 hour less than Amit. Find their speeds of walking.

## Answer

Speed = distance/time
Let the speed of Ajeet be ' $a$ ' and speed of Amit be ' $b$ '
Given, while covering distance of 30 km . Ajeet takes 2 hours more than Amit. If Ajeet doubles his speed, he would take 1 hour less than Amit.
$\Rightarrow \frac{30}{a}-\frac{30}{b}=2$
Also, $\frac{30}{b}-\frac{30}{2 a}=1$
Adding the two equations
$\Rightarrow 30 / a-15 / a=3$
$\Rightarrow \mathrm{a}=5 \mathrm{~km} / \mathrm{hr}$
Thus, $30 / 5-30 / b=2$
$\Rightarrow \mathrm{b}=7.5 \mathrm{~km} / \mathrm{hr}$

## 6. Question

A man walks a certain distance with certain speed. If he walks $1 / 2 \mathrm{~km}$ an hour faster, he takes 1 hour less. But, if he walks 1 km an hour slower, he takes 3 more hours. Find the distance covered by the man and his original rate of walking.

## Answer

Given: A man walks a certain distance with certain speed. If he walks $1 / 2 \mathrm{~km}$ an hour faster, he takes 1 hour less. But, if he walks 1 km an hour slower, he takes 3 more hours. '

To find: the distance covered by the man and his original rate of walking.
Solution:Let the original speed, original time taken and distance be ' $a$ ', ' $t$ ' and ' $d$ '. As we know, distance $=$ speed $\times$ time $\Rightarrow d=a t$ $\qquad$
Given, if he walks $1 / 2 \mathrm{~km}=0.5 \mathrm{~km}$ an hour faster, he takes 1 hour less,
$\Rightarrow d=(a+0.5)(t-1) \Rightarrow d=a t+0.5 t-a-0.5 \Rightarrow$ at $=a t+0.5 t-a-0.5$
[From 1] $\Rightarrow 0.5 \mathrm{t}-\mathrm{a}=0.5$ Multiply the above equation by 10 to get, $\Rightarrow 5 \mathrm{t}-10 \mathrm{a}=5 \Rightarrow 10 \mathrm{a}=5 \mathrm{t}-5$

Also if he walks 1 km an hour slower, her takes 3 more hours., $\Rightarrow d=(a-1)(t+3) \Rightarrow d=a t+3 a-t-3 \Rightarrow a t=a t+3 a-t-$
$3 \quad[$ From 1] $\Rightarrow 3 \mathrm{a}-\mathrm{t}=3 \Rightarrow \mathrm{t}=3 \mathrm{a}-3 \quad--\cdots--(3)$ Put the value of t in eq $(2) \Rightarrow 10 \mathrm{a}=5(3 \mathrm{a}-3)-5 \Rightarrow 10 \mathrm{a}=15 \mathrm{a}-15-$ $5 \Rightarrow 10 \mathrm{a}-15 \mathrm{a}=-15-5 \Rightarrow-5 \mathrm{a}=-20 \Rightarrow \mathrm{a}=4$ Putting back in (3), we get $\Rightarrow \mathrm{t}=3(4)-3=9$ Therefore, $\mathrm{d}=\mathrm{at}=4(9)=$ 36 Hence, speed of man $=a=4 \mathrm{~km} /$ hrdistance covered by man $=\mathrm{d}=36 \mathrm{~km}$

## 7. Question

Ramesh travels 760 km to his home partly by train and partly by car. He takes 8 hours if he travels 160 km by train and the rest by car. He takes 12 minutes more if the travels 240 km by train and the rest by car. Find the speed of the train and car respectively.

## Answer

Let the speed of train be 'a' and speed of car be ' $b$ '.
Speed $=$ distance/time
Given, Ramesh travels 760 km to his home partly by train and partly by car. He takes 8 hours if he travels 160 km by train and the rest by car. He takes 12 minutes more if the travels 240 km by train and the rest by car.
$\Rightarrow \frac{160}{a}+\frac{600}{b}=8$
Also, $\frac{240}{a}+\frac{520}{b}=8+\frac{12}{60}$
$\Rightarrow 240 / a+520 / b=41 / 5----(2)$
Multiplying eq 1 by 3 and eq 2 by 2 and subtracting eq 2 from eq 1
$\Rightarrow \frac{1800}{b}-\frac{1040}{b}=24-\frac{82}{5}$
$\Rightarrow \frac{760}{b}=\frac{38}{5}$
$\Rightarrow \mathrm{b}=100 \mathrm{~km} / \mathrm{hr}$
Thus, $160 / a+6=8$
$\Rightarrow \mathrm{a}=80 \mathrm{~km} / \mathrm{hr}$

## 8. Question

A man travels 600 km partly by train and partly by car. If he covers 400 km by train and the rest by car, it takes him 6 hours and 30 minutes. But, if he travels 200 km by train and the rest by car, he takes half an hour longer. Find the speed of the train and that of the car.

## Answer

Given: A man travels 600 km partly by train and partly by car. If he covers 400 km by train and the rest by car, it takes him 6 hours and 30 minutes. But, if he travels 200 km by train and the rest by car, he takes half an hour longer.

To find: the speed of the train and that of the car.
Solution:Let the speed of train be ' $a$ ' and speed of car be ' $b$ '.
Speed $=$ distance/time
Given, man travels 600 km partly by train and partly by car. If he covers 400 km by train and the rest by car, it takes him 6 hours and 30 minutes.
$\Rightarrow \frac{400}{a}+\frac{200}{b}=6.5-\cdots-\cdots$
But, if he travels 200 km by train and the rest by car, he takes half an hour longer.
$\frac{200}{a}+\frac{400}{b}=7$
Multiplying eq1 by 2 and subtracting from eq2
$\left(\frac{200}{a}+\frac{400}{b}\right)-2\left(\frac{400}{a}+\frac{200}{b}\right)=7-2(6.5)$
$\frac{200}{a}+\frac{400}{b}-\frac{800}{a}-\frac{400}{b}=7-13$
$\Rightarrow \frac{200}{a}-\frac{800}{a}=7-13 \Rightarrow \frac{-600}{a}=-6$
$\Rightarrow-600=-6 a$
$\Rightarrow \mathrm{a}=100 \mathrm{~km} / \mathrm{hr}$
Thus, $4+200 / b=6.5200 / b=6.5-4$
$\Rightarrow 200 / b=2.5 \Rightarrow 2.5 b=200$
$\Rightarrow \mathrm{b}=80 \mathrm{~km} / \mathrm{hr}$

## 9. Question

Places $A$ and $B$ are 80 km apart form each other on a highway. $A$ car starts from $A$ and other from $B$ at the same time. If they move in the same direction, they meet in 8 hours and if they move in opposite directions, they meet in 1 hour and 20 minutes. Find the speeds of the cars.

## Answer

Given: places A and B are 80 km apart form each other on a highway. A car starts from A and other from $B$ at the same time. If they move in the same direction, they meet in 8 hours and if they move in opposite directions, they meet in 1 hour and 20 minutes.

To find: the speeds of the cars.
Solution:Let the speed of car from A be ' $a$ ' and of car from B be ' $b$ '.
Speed $=$ distance/time
Relative speed of cars when moving in same direction $=a+b$
Relative speed of cars when moving in opposite direction $=a-b$
Given, places $A$ and $B$ are 80 km apart form each other on a highway. A car starts from $A$ and other from $B$ at the same time. If they move in the same direction, they meet in 8 hours and if they move in opposite directions, they meet in 1 hour and 20 minutes.


Also, $a+b=\frac{80}{1+\frac{20}{60}}=60-\cdots---$
Adding (1) and (2) $\Rightarrow \mathrm{a}-\mathrm{b}+\mathrm{a}+\mathrm{b}=10+60$
$\Rightarrow 2 \mathrm{a}=70$
$\Rightarrow \mathrm{a}=35 \mathrm{~km} / \mathrm{hr}$
Put the value of $a$ in (1).
Thus, $\mathrm{b}=35-10=25 \mathrm{~km} / \mathrm{hr}$
Hence, speed of two cars are $35 \mathrm{~km} / \mathrm{h}$ and $25 \mathrm{~km} / \mathrm{h}$

## 10. Question

A boat goes 12 km upstream and 40 km downstream in 8 hours. It can go 16 km upstream and 32 km downstream in the same time. Find the speed of the oat in still water and the speed of the stream.

## Answer

Speed $=$ distance/time
Let the speed of boat be ' $a$ ' and speed of stream be ' $b$ '
Relative speed of boat going upstream $=a-b$
Relative speed of boat going downstream $=a+b$
Given, boat goes 12 km upstream and 40 km downstream in 8 hours. It can go 16 km upstream and 32 km downstream in the same time
$\Rightarrow \frac{12}{a-b}+\frac{40}{a+b}=8$
Also, $\frac{16}{a-b}+\frac{32}{a+b}=8$
Equating (1) and (2), we get
$\Rightarrow 8 /(a+b)=4 /(a-b)$
$\Rightarrow \mathrm{a}=3 \mathrm{~b}$
Substitute value of a in eq1
$\Rightarrow 12 / 2 \mathrm{~b}+40 / 4 \mathrm{~b}=8$
$\Rightarrow 16 / \mathrm{b}=8$
$\Rightarrow \mathrm{b}=2 \mathrm{~km} / \mathrm{hr}$
Thus, $\mathrm{a}=6 \mathrm{~km} / \mathrm{hr}$.

## 11. Question

Roohi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and the remaining by bus. If she travels 100 km by train and the remaining by bus, she takes 10 minutes longer. Find the speed of the train and the bus respectively.

## Answer

Let the speed of train be ' $a$ ' and speed of bus be ' $b$ '.
Speed $=$ distance/time
Roohi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and the remaining by bus. If she travels 100 km by train and the remaining by bus, she takes 10 minutes longer
$\Rightarrow \frac{60}{a}+\frac{240}{b}=4-\cdots----$

Also, $\frac{100}{a}+\frac{200}{b}=4+\frac{10}{60}$
$\frac{100}{a}+\frac{200}{b}=\frac{25}{6}$
Multiplying eq 1 by 5 and eq 2 by 3 and subtracting eq 2 from eq 1
$\Rightarrow \frac{1200}{b}-\frac{600}{b}=20-\frac{25}{2}$
$\Rightarrow \mathrm{b}=80 \mathrm{~km} / \mathrm{hr}$
Thus, $60 / a+3=4$
$\Rightarrow \mathrm{a}=60 \mathrm{~km} / \mathrm{hrHence}$ speed of train is $60 \mathrm{~km} / \mathrm{h}$ and bus is $80 \mathrm{~km} / \mathrm{h}$.

## 12. Question

Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hours. Find her speed of rowing in still water and the speed of the current.

## Answer

Let the speed of her rowing in still water be ' $a$ ' and speed of current be 'b.'We know, speed $=\frac{\text { distance }}{\text { time }}$
Relative speed of boat going upstream $=a-b$
Relative speed of boat going downstream $=a+b$
Given, Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hours
$\Rightarrow \mathrm{a}+\mathrm{b}=20 / 2=10$ -
(1) and $a-b=4 / 2=2$ $\qquad$
Adding eq1 and eq2
$\Rightarrow 2 a=12$
$\Rightarrow \mathrm{a}=6 \mathrm{~km} / \mathrm{hr}$
Also, $\mathrm{b}=\mathrm{a}-2=4 \mathrm{~km} / \mathrm{hr}$
Therefore, her speed of rowing in still water is $6 \mathrm{~km} / \mathrm{h}$ and the speed of the current is $4 \mathrm{~km} / \mathrm{h}$

## 13. Question

A takes 3 hours more than $B$ to walk a distance of 30 km . But, if A doubles his pace (speed) he is ahead of B by $1 \frac{1}{2}$ hours.
Find the speeds of A and B .

## Answer

Let the speed of $A$ be ' $a$ ' and speed of $B$ be ' $b$ '.
Given, A takes 3 hours more than B to walk a distance of 30 km . But, if A doubles his pace (speed) he is ahead of B by $1 \frac{1}{2}$ hours
$\Rightarrow \frac{30}{a}-\frac{30}{b}=3$
Also, $\frac{30}{b}-\frac{30}{2 a}=1.5-----$
Adding (1) and (2)
$\Rightarrow 15 / \mathrm{a}=4.5$
$\Rightarrow \mathrm{a}=150 / 45=10 / 3 \mathrm{~km} / \mathrm{hr}$
Thus,
$\frac{30}{\frac{10}{3}}-\frac{30}{b}=3$
$\Rightarrow \mathrm{b}=5 \mathrm{~km} / \mathrm{hr}$

## 14. Question

Abdul travelled 300 km by train and 200 km by taxi, it took him 5 hours 30 minutes. But if he travels 260 km by train and 240 km by taxi he takes 6 minutes longer. Find the speed of the train and that of the taxi.

## Answer

Let the speed of train be ' $a$ ' and speed of taxi be ' $b$ '.
Speed $=$ distance/time
Abdul travelled 300 km by train and 200 km by taxi, it took him 5 hours 30 minutes. But if he travels 260 km by train and 240 km by taxi he takes 6 minutes longer.
$\Rightarrow \frac{300}{a}+\frac{200}{b}=5.5--\cdots--$ (1)
Also, $\frac{260}{a}+\frac{240}{b}=5.5+\frac{6}{60}$
$\frac{260}{a}+\frac{240}{b}=5.6-\cdots---$ (2)
Multiplying eq 1 by 6 and eq2 by 5 and subtracting eq 2 from eq 1
$\Rightarrow \frac{1800}{a}-\frac{1300}{a}=33-28$
$\Rightarrow \mathrm{a}=100 \mathrm{~km} / \mathrm{hr}$
Thus, $3+200 / \mathrm{b}=5.5$
$\Rightarrow \mathrm{b}=80 \mathrm{~m} / \mathrm{hr}$

## 15. Question

A train covered a certain distance at a uniform speed. If the train could have been $10 \mathrm{~km} / \mathrm{hr}$. faster, it would have taken 2 hours less than the scheduled time. And, if the train were slower by $10 \mathrm{~km} / \mathrm{hr}$, it would have taken 3 hours more than the scheduled time. Find the distance covered by train.

## Answer

Let the speed of train be ' $s$ ', scheduled time be ' $t$ ' and distance be ' d '.
Speed $=$ distance/time
Given, covered a certain distance at a uniform speed. If the train could have been $10 \mathrm{~km} / \mathrm{hr}$. faster, it would have taken 2 hours less than the scheduled time. And, if the train were slower by $10 \mathrm{~km} / \mathrm{hr}$, it would have taken 3 hours more than the scheduled time.
$\Rightarrow d=s t$
$d=(s+10)(t-2)$
$d=(s-10)(t+3)-----$
Solving the above three equation we get, $\mathrm{d}=600 \mathrm{~km}, \mathrm{~s}=50 \mathrm{~km} / \mathrm{hr}$ and $\mathrm{t}=12$ hours

## 16. Question

Places $A$ and $B$ are 100 km apart on a highway. One car starts form $A$ and another from $B$ at the same time. If the cars travel in the same direction at different speeds, they meet in 5 hours. If they travel towards each other, they meet in 1 hour. What are the speeds of two cars?

## Answer

Let the speed of car from $A$ be ' $a$ ' and of car from $B$ be ' $b$ '
Speed = distance/time
Relative speed of cars when moving in same direction $=a+b$
Relative speed of cars when moving in opposite direction $=a-b$
Given, places $A$ and $B$ are 100 km apart on a highway. One car starts from $A$ and another from $B$ at the same time. If the cars travel in the same direction at different speeds, they meet in 5 hours. If they travel towards each other, they meet in 1 hour
$\Rightarrow \mathrm{a}-\mathrm{b}=100 / 5=20$
Also, $a+b=100 / 1=100$
Adding (1) and (2)
$a-b+a+b=20+100$
$\Rightarrow 2 \mathrm{a}=120$
$\Rightarrow \mathrm{a}=60 \mathrm{~km} / \mathrm{hr}$
Putting value of a in (1) we get,
Thus, $b=60-20=40 \mathrm{~km} / \mathrm{hr}$ Speed of two cars are $60 \mathrm{~km} / \mathrm{h}$ and $40 \mathrm{~km} / \mathrm{h}$

## Exercise 3.11

## 1. Question

If in a rectangle, the length is increased and breadth reduced each by 2 units, the area is reduced by 28 square units. If, however the length is reduced by 1 unit and the breadth increased by 2 units, the area increases by 33 square units. Find the area of the rectangle.

## Answer

Area of a rectangle $=1 \times b$
Given, if in a rectangle, the length is increased and breadth reduced each by 2 units, the area is reduced by 28 square units. If, however the length is reduced by 1 unit and the breadth increased by 2 units, the area increases by 33 square units.
$\Rightarrow(1+2)(b-2)=1 b-28$
$\Rightarrow 2 b-21=-24-----(1)$
Also, $(\mathrm{l}-1)(\mathrm{b}+2)=\mathrm{lb}+33$
$\Rightarrow 21-\mathrm{b}=35$ $\qquad$
Adding (1) and (2), we get
$\Rightarrow b=11$
Thus, $21=46, I=23$
Area of the rectangle $=\mathrm{lb}=253$ square units.

## 2. Question

The area of a rectangle remains the same if the length is increased by 7 metres and the breadth is decreased by 3 metres. If the length is decreased by 7 metres and breadth is increased by 4 metres, the area is decreased by 21 sq. metres. Find the dimensions of the rectangle.

## Answer

Area of a rectangle $=\mathrm{I} \times \mathrm{b}$
Given, area of a rectangle remains the same if the length is increased by 7 metres and the breadth is decreased by 3 metres. If the length is decreased by 7 metres and breadth is increased by 4 metres, the area is decreased by 21 sq.
metres.
$\Rightarrow(I+7)(b-3)=|b| b-3 \mid+7 b-21=l b$
$\Rightarrow 7 b-3 I=21$
Also, $(\mathrm{I}-7)(\mathrm{b}+4)=\mathrm{lb}-21$
$\mathrm{lb}+4 \mathrm{l}-7 \mathrm{~b}-28=\mathrm{lb}-21$
$\Rightarrow 41-7 b=7$
Adding (1) and (2), we get7b-3I $+4 \mathrm{l}-7 \mathrm{~b}=21+7$
$\Rightarrow I=28 \mathrm{~m}$
put the value of I in 1 to get7b-3(28)=21
Thus, $7 \mathrm{~b}-84=21$
$7 b=21+847 b=105$
$\Rightarrow \mathrm{b}=15 \mathrm{mHence}$ the length is 28 m and breadth is 15 m .

## 3. Question

In a rectangle, if the length is increased by 3 metres and breadth is decreased by 4 metres, the area of the rectangle is reduced by 67 square metres. If length is reduced by 1 metre and breadth is increased by 4 metres, the area is increased by 89 sq. metres. Find the dimensions of the rectangle.

## Answer

Area of a rectangle $=I \times b$
Given, if the length is increased by 3 metres and breadth is decreased by 4 metres, the area of the rectangle is reduced by 67 square metres. If length is reduced by 1 metre and breadth is increased by 4 metres, the area is increased by 89 sq. metres.
$\Rightarrow(\mathrm{I}+3)(\mathrm{b}-4)=\mathrm{lb}-67$
$\Rightarrow 3 b-4 I=-55$ $\qquad$
Also, $(I-1)(b+4)=l b+89$
$\Rightarrow 41-\mathrm{b}=93$ $\qquad$
Adding (1) and (2), we get
$\Rightarrow 2 \mathrm{~b}=38$
$\Rightarrow \mathrm{b}=19$
Thus, 4 I- $19=93$
$\Rightarrow \mid=28 \mathrm{~m}$

## 4. Question

The incomes of $X$ and $Y$ are in the ratio of $8: 7$ and their expenditures are in the ratio $19: 16$. If each saves Rs 1250, find their incomes.

## Answer

Given, incomes of $X$ and $Y$ are in the ratio of $8: 7$ and their expenditures are in the ratio $19: 16$.
Let the incomes of $X$ and $Y$ be $8 a$ and $7 a$
Let the expenditures of $X$ and $Y$ be 19b and 16b
Each saves Rs. 1250
(1) and $7 a-16 b=1250$

Equating both equation
$\Rightarrow 8 \mathrm{a}-19 \mathrm{~b}=7 \mathrm{a}-16 \mathrm{~b}$
$\Rightarrow a=3 b$
Substituting value of a in eq1
$\Rightarrow 24 b-19 b=1250$
$\Rightarrow \mathrm{b}=250$
Thus, $a=750$
X's income $=8 \mathrm{a}=$ Rs. 6000
Y's income $=7 \mathrm{a}=$ Rs. 5250

## 5. Question

$A$ and $B$ each has some money. If $A$ gives Rs 30 to $B$, then $B$ will have twice the money left with $A$. But, if $B$ gives Rs 10 to $A$, then a will have thrice as much as is left with $B$. How much money does each have?

## Answer

Let the amount of money which $A$ has be ' $a$ ' and which $B$ has be ' $b$ '.
Given, if A gives Rs 30 to $B$, then $B$ will have twice the money left with $A$.
$\Rightarrow b+30=2(a-30) \Rightarrow b+30=2 a-60 \Rightarrow b=2 a-60-30 \Rightarrow b=2 a-90--$
(1)But, if B gives Rs 10 to A, then A will have thrice as much as is left with $B$
$a+10=3(b-10) a+10=3 b-30 a=3 b-30-10$
$\Rightarrow \mathrm{a}=3 \mathrm{~b}-40$
Substituting ' $a$ ' from eq2 in eq $1 b=2(3 b-40)-90$
$\Rightarrow b=6 b-80-90$
$\Rightarrow \mathrm{b}-6 \mathrm{~b}=-80-90 \Rightarrow-5 \mathrm{~b}=-170 \Rightarrow \mathrm{~b}=-170 /-5$
$\Rightarrow b=R s .34$
Substitute value of $b$ in eq. $2, a=3(34)-40$
Thus, $\mathrm{a}=102-40=$ Rs. 62 Hence, $A$ has Rs 62 and $B$ has Rs 34 .

## 6. Question

There are two examination rooms $A$ and $B$. If 10 candidates are sent from $A$ to $B$, the number of students in each room is same. If 20 candidates are sent from $B$ to $A$, the number of students in $A$ is double the number of students in $B$. Find the number of students in each room.

## Answer

Let the number of candidates in rooms $A$ and $B$ be ' $a$ ' and ' $b$ ' respectively.
Given, if 10 candidates are sent from $A$ to $B$, the number of students in each room is same.
$\Rightarrow \mathrm{a}-10=\mathrm{b}+10$
$\Rightarrow \mathrm{a}-\mathrm{b}=20$-----
Also, if 20 candidates are sent from $B$ to $A$, the number of students in $A$ is double the number of students in $B$.
$\Rightarrow \mathrm{a}+20=2(\mathrm{~b}-20)$
$\Rightarrow \mathrm{a}-2 \mathrm{~b}=-60$
Subtracting eq2 from eq1
$\Rightarrow \mathrm{a}-\mathrm{b}-\mathrm{a}+2 \mathrm{~b}=20+60$
$\Rightarrow b=80$
Thus, $\mathrm{a}=80+20=100$

## 7. Question

2 men and 7 boys can do a piece of work in 4 days. The same work is done in 3 days by 4 men and 4 boys. How long would it take one man and one boy to do it?

## Answer

Given: 2 men and 7 boys can do a piece of work in 4 days. The same work is done in 3 days by 4 men and 4 boys. To find: How long would it take one man and one boy to do it.Solution:Let the number of days in which 1 man and 1 boy can do the work be 'a' and ' $b$ ' respectively.

In 1 day, In a days 1 man can work $\Rightarrow$ In 1 day $1 / a$ man can do work $\Rightarrow 2$ men can do work in $2 / a$ daysSimilarlyIn $b$ days 1 boy can work $\Rightarrow$ In 1 day $1 /$ b boy can do work $\Rightarrow 7$ boys can do work in $7 / \mathrm{b}$ daysGiven, 2 men and 7 boys can do a piece of work in 4 days. The same work is done in 3 days by 4 men and 4 boys.
$\Rightarrow \frac{2}{a}+\frac{7}{b}=\frac{1}{4}$
$\Rightarrow \frac{4}{a}+\frac{4}{b}=\frac{1}{3}$
Multiplying eq1 by 2 and subtracting eq2 from eq1

$$
\begin{aligned}
& \Rightarrow 2\left(\frac{2}{a}\right)+2\left(\frac{7}{b}\right)-\frac{4}{a}-\frac{4}{b}=2\left(\frac{1}{4}\right)-\frac{1}{3} \\
& \Rightarrow \frac{4}{a}+\frac{14}{b}-\frac{4}{a}-\frac{4}{b}=\frac{2}{4}-\frac{1}{3} \\
& \Rightarrow \frac{14}{b}-\frac{4}{b}=\frac{1}{2}-\frac{1}{3} \\
& \Rightarrow \frac{14-4}{b}=\frac{3-2}{6}
\end{aligned}
$$

$$
\Rightarrow 10 / b=1 / 6
$$

$$
\Rightarrow \mathrm{b}=60 \text { days }
$$

Substitute the value of b in eq. $2 \Rightarrow \frac{4}{a}+\frac{4}{60}=\frac{1}{3}$

$$
\Rightarrow \frac{4}{a}+\frac{A^{1}}{\mathscr{6} O_{15}}=\frac{1}{3}
$$

Thus, $4 / a+1 / 15=1 / 3$

$$
\Rightarrow \frac{4}{a}=\frac{1}{3}-\frac{1}{15}
$$

$$
\Rightarrow \frac{4}{a}=\frac{5-1}{15}
$$

$$
\Rightarrow \frac{4}{a}=\frac{4}{15}
$$

$\Rightarrow a=15$ days
thus 1 man can do work in 15 days and 1 boy can do work in 60 days.

## 8. Question

In a $\triangle A B C, \angle A=x^{\circ}, \angle B=(3 x-2)^{\circ}$,
$\angle C=y^{\circ}$. Also, $\angle C-\angle B=9^{\circ}$. Find the three angles.
Answer
Sum of angles of a triangle $=180^{\circ}$
Given, $\angle A=x^{\circ}, \angle B=(3 x-2)^{\circ}$,
$\angle C=y^{\circ}$.
$\Rightarrow x+3 x-2+y=180$
$\Rightarrow 4 x+y=182-----$
Also, $\angle C-\angle B=9^{\circ}$.
$\Rightarrow \mathrm{y}-3 \mathrm{x}+2=9$
$\Rightarrow \mathrm{y}-3 \mathrm{x}=7$
(1) $-(2)$
$\Rightarrow 4 x+y-y+3 x=182-7$
$\Rightarrow 7 x=175$
$\Rightarrow x=25^{\circ}$
Thus, $\mathrm{y}=75+7=82^{\circ}$
$\angle A=25^{\circ}$
$\angle B=3 X-2=73^{\circ}$
$\angle C=82^{\circ}$

## 9. Question

In a cyclic quadrilateral $\mathrm{ABCD} \angle A=(2 x+4)^{\circ}, \angle B=(y+3)^{\circ}, \angle C=(2 y+10)^{\circ}, \angle D=(4 x-5)^{\circ}$. Find the four angles.

## Answer

Opposite angles of a cyclic quadrilateral are supplementary
$\angle \mathrm{A}+\angle \mathrm{C}=180^{\circ}$
$\angle B+\angle D=180^{\circ}$
Given, $\angle A=(2 x+4)^{\circ}, \angle B=(y+3)^{\circ}, \angle C=(2 y+10)^{\circ}, \angle D=(4 x-5)^{\circ}$
$2 x+4+2 y+10=180$
$\Rightarrow x+y=83$
$y+3+4 x-5=180$
$\Rightarrow y+4 x=182$
(1) - (2)
$\Rightarrow \mathrm{x}-4 \mathrm{x}=83-182$
$\Rightarrow x=33$
Thus, $y=50$
$\angle A=2 x+4=70^{\circ}$
$\angle B=y+3=53^{\circ}$
$\angle C=2 y+10=110^{\circ}$
$\angle D=4 x-5=127^{\circ}$

## 10. Question

A railway half ticket costs half the full fare and the reservation charge is the same on half ticket as on full ticket. One reserved first class ticket from Mumbai to Ahmedabad costs Rs 216 and one full and one half reserved first class tickets cost Rs 327. What is the basic first class full fare and what is the reservation charge?

## Answer

Let the basic full fare be ' $a$ ', half far be ' $b$ ' and reservation charges be ' $r$ '.
Given, railway half ticket costs half the full fare and the reservation charge is the same on half ticket as on full ticket.
$a=2 b----$
Also, reserved first class ticket from Mumbai to Ahmedabad costs Rs 216 and one full and one half reserved first class tickets cost Rs 327.
$\Rightarrow a+r=216$
Also, $a+b+2 r=327$----- (3)
Substituting value of $a$ in eq 2 and eq3
$\Rightarrow 2 b+r=216$ and $3 b+2 r=327$
Solving the above equations, we get
$r=$ Rs. 6 and $b=$ Rs. 105
Thus a = Rs. 210

## 11. Question

In a $\triangle A B C, \angle A=x^{\circ}, \angle B=3 x^{\circ}, \angle C=y^{\circ}$. If $3 y-5 x=30$, prove that the triangle is right angled.

## Answer

Sum of angles of a triangle $=180^{\circ}$
Given, $\angle A=x^{\circ}, \angle B=3 x^{\circ}, \angle C=y^{\circ}$
$\therefore \mathrm{x}+3 \mathrm{x}+\mathrm{y}=180$
$\Rightarrow y+4 x=180$
Also, $3 y-5 x=30$
Multiplying eq 1 by 5 and eq 2 by 4 and adding them
$\Rightarrow 5 y+12 y=900+120$
$\Rightarrow y=60$
Thus, $60+4 x=180$
$\Rightarrow x=30$
$\angle A=30^{\circ}, \angle B=90^{\circ}$ and $\angle C=60^{\circ}$
Triangle is right angled at B.

## 12. Question

The car hire charges in a city computerise of a fixed charges together with the charge for the distance covered. For a journey of 12 km , the charge paid is Rs 89 and for a journey of 20 km , the charge paid is Rs 145 . What will a person have
to pay for travelling a distance of 30 km ?

## Answer

Let the fixed charge be ' $a$ ' and the charge per km travelled be ' $b$ '
Given, for a journey of 12 km , the charge paid is Rs 89 and for a journey of 20 km , the charge paid is Rs 145
$\Rightarrow a+12 b=89----(1)$
and $a+20 b=145----(2)$
(1) - (2)
$\Rightarrow-8 \mathrm{~b}=-56$
$\Rightarrow \mathrm{b}=7$
Thus, $a+84=89$
$\Rightarrow \mathrm{a}=5$
For a distance of 30 km , amount paid $=$ distance travelled x charge per kilometre + fixed charge
$=30 \times 7+5=$ Rs. 215

## 13. Question

A part of monthly hostel charges in a college are fixed and the remaining depend on the number of days one has taken food in the mess. When a student a takes food for 20 days, he has to pay Rs 1000 as hostel charges whereas a student $B$, who takes food for 26 days, pays Rs 1180 as hostel charges. Find the fixed charge and the cost of food per day.

## Answer

Let the fixed charges be ' $a$ ' and the cost of food per day be ' $b$ '
Given, when a student a takes food for 20 days, he has to pay Rs 1000 as hostel charges whereas a student B, who takes food for 26 days, pays Rs 1180 as hostel charges.
$\Rightarrow a+20 b=1000$
$a+26 b=1180$
Subtracting one from another
$\Rightarrow 6 \mathrm{~b}=180$
$\Rightarrow b=$ Rs. 30
Thus, $a+600=1000$
$\Rightarrow \mathrm{a}=$ Rs. 400

## 14. Question

Half the perimeter of a garden, whose length is 4 more than its width is 36 m . Find the dimensions of the garden.

## Answer

Given, half the perimeter of a garden, whose length is 4 more than its width is 36 m .
$\Rightarrow \mathrm{I}=\mathrm{b}+4$ and $\mathrm{I}+\mathrm{b}=36$
Solving these two equations, we get
Length $=20 \mathrm{~m}$, Width $=16 \mathrm{~m}$

## 15. Question

The larger of two supplementary angles exceeds the smaller by 18 degrees. Find them.

## Answer

Given: The larger of two supplementary angles exceeds the smaller by 18 degrees.
To find: The measure of both angles.
solution: Let the larger angle be ' $a$ ' and the smaller angle be ' $b$ '.
Given, larger of two supplementary angles exceeds the smaller by 18 degrees.
$\Rightarrow \mathrm{a}=\mathrm{b}+18 \Rightarrow \mathrm{a}-\mathrm{b}=18 \ldots \ldots$ (1)The sum of supplementary angles is $180^{\circ} . \Rightarrow \mathrm{a}+\mathrm{b}=180 \ldots$. (2)
Adding the equations 1 and 2 we get,
$a-b+a+b=18+180$
$\Rightarrow 2 \mathrm{a}=198$
$\Rightarrow a=99^{\circ}$ Put the value of $b$ in eq. 1 to get, $99-b=18 \Rightarrow-b=18-99 \Rightarrow-b=-81 \Rightarrow b=81$
Thus, $\mathrm{b}=81^{\circ}$ Hence the measure of smaller angle is $81^{\circ}$ and larger angle is $99^{\circ}$.

## 16. Question

2 Women and 5 men can together finish a piece of embroidery in 4 days, while 3 women and 6 men can finish it in 3 days. Find the time taken by 1 woman alone to finish the embroidery, and that taken by 1 man alone.

## Answer

Let the number of days in which 1 woman and 1 man can do the work be ' $a$ ' and ' $b$ ' days respectively.
In 1 day, 1 woman completes $1 /$ a part while 1 man does $1 / \mathrm{b}$ part
Given, 2 Women and 5 men can together finish a piece of embroidery in 4 days, while 3 women and 6 men can finish it in 3 days.
$\Rightarrow \frac{2}{a}+\frac{5}{b}=\frac{1}{4}$
$\frac{3}{a}+\frac{6}{b}=\frac{1}{3}$
Multiplying eq1 by 3 and eq2 by 2
$\frac{6}{a}+\frac{15}{b}=\frac{3}{4}$
$\frac{6}{a}+\frac{12}{b}=\frac{2}{3}$
subtracting eq3 from eq4
$\Rightarrow \frac{15}{b}-\frac{12}{b}=\frac{3}{4}-\frac{2}{3}$
$\Rightarrow 3 / \mathrm{b}=1 / 12$
$\Rightarrow \mathrm{b}=36$ days
Thus, $3 / a+1 / 6=1 / 3$
$\Rightarrow 3 / a=1 / 6$
$\Rightarrow \mathrm{a}=18$ daysHence, A women can finish the embroidery in 18 days and A single man can finish the embroidery in 36 days

## 17. Question

A wizard having powers of mystic in candations and magical medicines seeing a cock, fight going on, spoke privately to both the owners of cocks. To one he said; if your bird wins, than you give me your stake-money, but if you do not win, I shall give you two third of that. Going to the other, he promised in the same way to give three fourths. From both of them his gain would be only 12 gold coins. Find the stake of money each of the cock-owners have.

Answer
Let the stake money be 'a' and 'b' respectively.
Given, to one he said; if your bird wins, than you give me your stake-money, but if you do not win, I shall give you two third of that. Going to the other, he promised in the same way to give three fourths.

From both of them his gain would be only 12 gold coins
If the $1^{\text {st }}$ one wins
$\Rightarrow \mathrm{a}-3 \mathrm{~b} / 4=12$
If the $2^{\text {nd }}$ one wins
$\Rightarrow \mathrm{b}-2 \mathrm{a} / 3=12$-----
Equating 1 and 2
$\Rightarrow 5 \mathrm{a} / 3=7 \mathrm{~b} / 4$
$\Rightarrow a=21 b / 20$
Thus, $21 \mathrm{~b} / 20-3 \mathrm{~b} / 4=12$
$\Rightarrow 6 \mathrm{~b} / 20=12$
$\Rightarrow b=40$
Thus, $a=21 b / 20=$ Rs. 42
18. Question

Meena went to a bank to withdraw Rs 2000. She asked the cashier to give her Rs 50 and Rs 100 notes only. Meena got 25 notes in all. Find how many note Rs 50 and Rs 100 she received.

## Answer

Given: Meena went to a bank to withdraw Rs 2000. She asked the cashier to give her Rs 50 and Rs 100 notes only. Meena got 25 notes in all.

To find: how many notes of Rs 50 and Rs 100 she received.
Solution: Let the number of Rs. 50 and Rs. 100 notes be ' $a$ ' and ' $b$ '.
Given, Meena went to a bank to withdraw Rs 2000. She asked the cashier to give her Rs 50 and Rs 100 notes only.
$\Rightarrow 50 \mathrm{a}+100 \mathrm{~b}=2000$
$\Rightarrow a+2 b=40$
Also Meena got 25 notes in all.
$\Rightarrow \mathrm{a}+\mathrm{b}=25$----- (2)
(1) $-(2) a+2 b-(a+b)=40-25$
$\Rightarrow \mathrm{a}+2 \mathrm{~b}-\mathrm{a}-\mathrm{b}=40-25$
$\Rightarrow b=15$
Put the value of $b$ in eq. 1 to get, $a+15=25 \Rightarrow a=25-15$
Thus, $a=10$ Therefore, Meena received 10 notes of denomination 50 and 15 notes of denomination 100 .

## 19. Question

Yash scored 40 marks in a test, getting 3 marks for each right answer and losing 1 mark for each wrong answer. Had 4 marks been awarded for each correct answer and 2 marks been deducted for each incorrect answer, then Yash would have scored 50 marks. How many questions were there in the test?

Answer

Given: Yash scored 40 marks in a test, getting 3 marks for each right answer and losing 1 mark for each wrong answer. Had 4 marks been awarded for each correct answer and 2 marks been deducted for each incorrect answer, then Yash would have scored 50 marks.

To find: How many questions were there in the test?
Solution: Let the number of right answers be ' $a$ ' and number of wrong answers be ' $b$ '
Given, Yash scored 40 marks in a test, getting 3 marks for each right answer and losing 1 mark for each wrong answer. Deducted marks are represented by "-" sign.
$\Rightarrow 3 \mathrm{a}-\mathrm{b}=40$------ (1)Had 4 marks been awarded for each correct answer and 2 marks been deducted for each incorrect answer, then Yash would have scored 50 marks
$\Rightarrow 4 \mathrm{a}-2 \mathrm{~b}=50$----
Multiplying eq1 by 2 and subtracting eq2 from $i t \Rightarrow 4 a-2 b-2(3 a-b)=50-2(40) \Rightarrow 4 a-2 b-6 a+2 b=50-80 \Rightarrow 4 a-6 a=$ 50-80
$\Rightarrow 6 \mathrm{a}-4 \mathrm{a}=80-50$
$\Rightarrow 2 \mathrm{a}=30$
$\Rightarrow a=15$ Put the value of $a$ in eq. 1 to get, $3(15)-b=40 \Rightarrow 45-b=40 \Rightarrow-b=40-45 \Rightarrow-b=-5 \Rightarrow b=5$
Total number of questions in the test $=$ right answers + wrong answers $=a+b=15+5=20$,

## 20. Question

The students of a class are made to stand in rows. If 3 students are extra in a row, there would be 1 row less. If 3 students are less in a row there would be 2 rows more. Find the number of students in the class.

## Answer

Let the number of students in a row be ' $a$ ' and number of rows be ' $b$ '.
Given, 3 students are extra in a row, there would be 1 row less. If 3 students are less in a row there would be 2 rows more.
Number of students remain constant.
$\Rightarrow a b=(a+3)(b-1) a b=(a-3)(b+2)$
So, $a b=a b-a+3 b-3 a-3 b=-3 \ldots \ldots$ (1) andab $=a b+2 a-3 b-62 a-3 b=6 \ldots \ldots$ (2)Subtract 1 from 2 to get, $2 a-3 b-$ $(a-3 b)=6-(-3) 2 a-3 b-a+3 b=6+3 a=9$ Put the value of $a$ in 1 to get, $9-3 b=-3-3 b=-3-9-3 b=-12 b=4$

Solving the above equations we get, $a=9$ and $b=4$
Thus, number of students $=a b=(9)(4)=36$

## 21. Question

One says, "give me hundred, friend! I shall then become twice as rich as you" The other replies, "If you give me ten, I shall be six times as rich as you." Tell me what is the amount of their respective capital?

## Answer

Given: One says, "give me hundred, friend! I shall then become twice as rich as you" The other replies, "If you give me ten, I shall be six times as rich as you."

To find: the amount of their respective capital.
Solution: Let the capitals be ' $a$ ' and ' $b$ '.
Given, one says, "give me hundred, friend! I shall then become twice as rich as you" .Lets assume "b" gives hundred to " a ". According to given condition
$a+100=2(b-100) \Rightarrow a+100=2 b-200$
$\Rightarrow a=2 b-200-100$
$\Rightarrow \mathrm{a}=2 \mathrm{~b}-300 \Rightarrow \mathrm{a}-2 \mathrm{~b}=-300-----(1)$ Now The other replies, "If you give me ten, I shall be six times as rich as you."

Which means "a" gives 10 to "b".
So, $b+10=6(a-10) \Rightarrow b+10=6 a-60 \Rightarrow b=6 a-60-10$
$\Rightarrow b=6 a-70 \Rightarrow 6 a-b=70$
Multiplying eq1 by 6 and subtract from eq 2
$\Rightarrow 6 \mathrm{a}-\mathrm{b}-6(\mathrm{a}-2 \mathrm{~b})=70-6(-300) \Rightarrow 6 \mathrm{a}-\mathrm{b}-6 \mathrm{a}+12 \mathrm{~b}=70+1800 \Rightarrow 11 \mathrm{~b}=1870 \Rightarrow \mathrm{~b}=170$ substitute the value of b in eq 1 to get, $a-2(170)=-300 \Rightarrow a-340=-300 \Rightarrow a=-300+340 \Rightarrow a=40$ The amount of their respective capital is Rs 40 and Rs 170.

## 22. Question

In a cyclic quadrilateral $\mathrm{ABCD} \angle A=(2 x+4)^{\circ}, \angle B=(y+3)^{\circ}, \angle C=(2 y+10)^{\circ}, \angle D=(4 x-5)^{\circ}$. Find the four angles.

## Answer

In a cyclic quadrilateral sum of opposite angles is $180^{\circ}$.
Given, in a cyclic quadrilateral $\mathrm{ABCD} \angle A=(2 x+4)^{\circ}, \angle B=(y+3)^{\circ}, \angle C=(2 y+10)^{\circ}, \angle D=(4 x-5)^{\circ}$
$\therefore \angle A+\angle C=180^{\circ}$ and $\angle B+\angle D=180^{\circ}$
$\Rightarrow 2 x+4+2 y+10=180$ and $y+3+4 x-5=180$
$\Rightarrow x+y=83$
(1) and $y+4 x=182$

Subtracting eq1 from eq2.
$\Rightarrow y+4 x-x-y=182-83$
$\Rightarrow 3 x=99$
$\Rightarrow x=33$
Substituting in eq1.
$\Rightarrow y=50$
$\angle A=2 \times 33+4=70^{\circ}$
$\angle B=50+3=53^{\circ}$
$\angle \mathrm{C}=2 \times 50+10=110^{\circ}$
$\angle D=4 \times 33-5=127^{\circ}$

## CCE - Formative Assessment

## 1. Question

Write the value of $k$ for which the system of equations $x+y-4=0$ and $2 x+k y-3=0$ has no solution.

## Answer

Given:
Equation 1: $x+y=4$
Equation 2: $2 x+k y=3$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=1$
$a_{2}=2$
$\mathrm{b}_{1}=1$
$\mathrm{b}_{2}=\mathrm{k}$
$c_{1}=4$
$c_{2}=3$
Putting the above values in equation (i) we get:
$\frac{1}{2}=\frac{1}{k}$
$\Rightarrow \mathbf{k}=2$
Also we find $\frac{1}{2} \neq \frac{4}{3}$
The value of $k$ for which the system of equations has no solution is $k=2$

## 2. Question

Write the value of $k$ for which the system of equations
$2 x-y=5$
$6 x+k y=15$
has infinitely many solutions.

## Answer

Given:
Equation 1: $2 x-y=5$
Equation 2: $6 x+k y=15$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$ $\qquad$
According to the problem:
$a_{1}=2$
$a_{2}=6$
$\mathrm{b}_{1}=-1$
$b_{2}=k$
$c_{1}=5$
$c_{2}=15$
Putting the above values in equation (i) we get:
$\frac{2}{6}=\frac{-1}{k}$
$\Rightarrow 2 \mathrm{k}=-6 \Rightarrow \mathrm{k}=-3$
Also we find $\frac{2}{6}=\frac{-1}{-3}=\frac{5}{15}$
The value of $k$ for which the system of equations has infinitely many solution is $k=-3$

## 3. Question

Write the value of $k$ for which the system of equations $3 x-2 y=0$ and $k x+5 y=0$ has infinitely many solutions.

## Answer

Given:
Equation 1: $3 x-2 y=0$
Equation 2: $k x+5 y=0$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=3$
$\mathrm{a}_{2}=\mathrm{k}$
$\mathrm{b}_{1}=-2$
$b_{2}=5$
$c_{1}=0$
$c_{2}=0$
In this problem since $c_{1} \& c_{2}=0$ so $\frac{c_{1}}{c_{2}}=\frac{0}{0}$ which is undefined.
So for this problem the system of linear equations will have infinite solutions if
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}$.
Putting the above values in equation (ii) we get:
$\frac{3}{k}=\frac{-2}{5}$
$\Rightarrow-2 k=15$
$\Rightarrow \mathrm{k}=-\frac{15}{2}$
The value of k for which the system of equations has infinitely many solution is $\underline{k}=-\frac{15}{2}$

## 4. Question

Write the values of $k$ for which the system of equations $x+k y=0,2 x-y=0$ has unique solution.

## Answer

Given:
Equation 1: $x+k y=0$
Equation 2: $2 x-y=0$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
According to the problem:
$a_{1}=1$
$a_{2}=2$
$\mathrm{b}_{1}=\mathrm{k}$
$b_{2}=-1$
$c_{1}=0$
$c_{2}=0$
So for this problem the system of linear equations will have unique solution if
$\frac{a_{1}}{a_{2}} \neq \frac{b_{1}}{b_{2}}$
Putting the above values in equation (i) we get:
$\frac{1}{2} \neq \frac{k}{-1}$
$\Rightarrow \mathbf{k} \neq-\frac{1}{2}$
The value of k for which the system of equations has unique solution is $\underline{k} \neq-\frac{1}{2}$

## 5. Question

Write the set of values of $a$ and $b$ for which the following system of equations has infinitely many solutions.
$2 x+3 y=7$
$2 a x+(a+b) y=28$
Answer
Given:
Equation 1: $2 x+3 y=7$
Equation 2: $2 a x+(a+b) y=28$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=2 a$
$b_{1}=3$
$b_{2}=(a+b)$
$c_{1}=7$
$c_{2}=28$
Putting the above values in equation (i) we get:
$\frac{2}{2 a}=\frac{3}{a+b}=\frac{7}{28}$.

To obtain the value of a \& be need to solve the above equality. First we solve the extreme left and extreme right of the equality to obtain the value of a.
$\Rightarrow \frac{2}{2 a}=\frac{7}{28} \Rightarrow 2 a * 7=2 * 28 \Rightarrow 14 a=56 \Rightarrow a=4$
After obtaining the value of a we again solve the extreme left and middle portion of the equality (ii)
$\frac{2}{2 * 4}=\frac{3}{4+b} \Rightarrow 2 *(4+b)=3 * 2 * 4 \Rightarrow b+4=12 \Rightarrow b=8$
The value of $a \& b$ for which the system of equations has infinitely many solution is $a=4 \& b=8$

## 6. Question

For what value of $k$, the following pair of linear equations has infinitely many solutions?
$10 x+5 y-(k-5)=0$
$20 x+10 y-k=0$
Answer
Given:

Equation 1: $10 x+5 y=(k-5)$ Equation 2: $20 x+10 y=k$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=10$
$a_{2}=20$
$\mathrm{b}_{1}=5$
$b_{2}=10$
$c_{1}=\mathrm{k}-5$
$\mathrm{c}_{2}=\mathrm{k}$
Putting the above values in equation (i) we get:
$\frac{10}{20}=\frac{5}{10}=\frac{k-5}{k} \ldots$ (ii)
On solving the equality (ii) we get
$5 k=10(k-5) \Rightarrow 5 k=10 k-50 \Rightarrow 5 k=50 \Rightarrow k=10$
The value of $k$ for which the system of equations has infinitely many solution is $k=10$

## 7. Question

Write the number of solutions of the following pair of linear equations:
$x+2 y-8=0$
$2 x+4 y=16$

## Answer

Given:
Equation 1: $x+2 y=8$ Equation $2: 2 x+4 y=16$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
The system of linear equations needs to be analyzed by checking the nature of ratios of each coefficients in the above two equations.

According to the problem:
$a_{1}=1$
$\mathrm{a}_{2}=2$
$\mathrm{b}_{1}=2$
$b_{2}=4$
$c_{1}=8$
$c_{2}=16$
Comparing the ratios of the coefficients we see:
$\Rightarrow \frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{1}{2} \ldots$ (i)
$\Rightarrow \frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathbf{2}}{4}$
$\Rightarrow \frac{\mathbf{b}_{1}}{\mathbf{b}_{2}}=\frac{\mathbf{1}}{2}$
$\Rightarrow \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}=\frac{8}{16}$
$\Rightarrow \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}=\frac{1}{2}$.
On seeing equation (i), (ii) and (iii) we find
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
Conclusion: The system of linear equations have infinite number of solution.
The given system of linear equations will have infinite number of solutions for all values of $x$ and $y$

## 8. Question

Write the number of solutions of the following pair of tinear equations:
$x+3 y-4=0$
$2 x+6 y=7$

## Answer

Given:
Equation 1: $x+3 y=4$ Equation $2: 2 x+6 y=7$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
According to the problem:
$a_{1}=1$
$a_{2}=2$
$\mathrm{b}_{1}=3$
$b_{2}=6$
$c_{1}=4$
$c_{2}=7$
Comparing the ratios of the coefficients we see:
$\Rightarrow \frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{1}{2} \ldots$ (i)
$\Rightarrow \frac{b_{1}}{b_{2}}=\frac{3}{6} \Rightarrow \frac{b_{1}}{b_{2}}=\frac{1}{2}$
$\Rightarrow \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}=\frac{4}{7}$.
On seeing equation (i), (ii) and (iii) we find
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
Conclusion: The system of linear equations has no solutions.
The given system of linear equations will have no solution for all values of $x$ and $y$

## 1. Question

The value of $k$ for which the system of equations
$k x-y=2$
$6 x-2 y=3$
has a unique solution, is
A. $=3$
B. $\neq 3$
C. $\neq 0$
D. $=0$

## Answer

Given:
Equation 1: $k x-y=2$
Equation 2: $6 x-2 y=3$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have unique solution we must have
$\frac{a_{1}}{a_{2}} \neq \frac{b_{1}}{b_{2}}$
According to the problem:
$\mathrm{a}_{1}=\mathrm{k}$
$a_{2}=6$
$\mathrm{b}_{1}=-1$
$b_{2}=-2$
$c_{1}=2$
$c_{2}=3$
Putting the above values in equation (i) we get
$\frac{k}{6} \neq \frac{-1}{-2} \Rightarrow k \neq \frac{-6}{-2} \Rightarrow k \neq 3$
The value of $k$ for which the system of equations has unique solution is $\underline{k} \neq 3$

## 2. Question

The value of $k$ for which the system of equations
$2 x+3 y=5$
$4 x+k y=10$
has infinite number of solutions, is
A. 1
B. 3
C. 6
D. 0

Answer
Given:
Equation 1: $2 x+3 y=5$
Equation 2: $4 x+k y=10$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=4$
$b_{1}=3$
$\mathrm{b}_{2}=\mathrm{k}$
$c_{1}=5$
$\mathrm{c}_{2}=10$

Putting the above values in equation (i) and solving the extreme left and middle portion of the equality we get the value of k
$\frac{2}{4}=\frac{3}{k}$
$\Rightarrow 2 \mathrm{k}=12 \Rightarrow \mathrm{k}=6$
Also we find $\frac{2}{4}=\frac{3}{6}=\frac{5}{10}$
The value of $k$ for which the system of equations has infinitely many solution is $k=6$

## 3. Question

The value of $k$ for which the system of equations $x+2 y-3=0$ and $5 x+k y+7=0$ has no solution, is
A. 10
B. 6
C. 3
D. 1

Answer
Given:
Equation 1: $x+2 y=3$
Equation 2: $5 x+k y=-7$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have no solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=1$
$a_{2}=5$
$b_{1}=2$
$\mathrm{b}_{2}=\mathrm{k}$
$c_{1}=3$
$c_{2}=-7$
Putting the above values in equation (i) and solving we get:
$\frac{1}{5}=\frac{2}{k}$
$\Rightarrow \mathbf{k}=10$

Also we find $\frac{1}{5}=\frac{2}{10} \neq \frac{3}{-7}$
The value of $k$ for which the system of equations has no solution is $k=10$

## 4. Question

The value of $k$ for which the system of equations $3 x+5 y=0$ and $k x+10 y=0$ has a non-zero solution, is
A. 0
B. 2
C. 6
D. 8

Answer
Given:
Equation 1: $3 x+5 y=0$
Equation $2: k x+10 y=0$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
According to the problem:
$a_{1}=3$
$\mathrm{a}_{2}=\mathrm{k}$
$\mathrm{b}_{1}=5$
$\mathrm{b}_{2}=10$
$c_{1}=0$
$c_{2}=0$
The equation will have a non zero solution only when it will satisfy a non trivial solution i.e. the equations should satisfy_ with values other than $x=0 \& y=0$.For the given system of equations the equation will have a non zero solution if
$\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}$ $\qquad$
Putting the above values in equation (i) we get:
$\frac{3}{k}=\frac{5}{10}$
$\Rightarrow 5 \mathrm{k}=30 \Rightarrow \mathrm{k}=6$
The value of $k$ for which the system of equations has non zero solution is $k=6$

## 5. Question

If the system of equations
$2 x+3 y=7$
$(a+b) x+(2 a-b) y=21$
has infinitely many solutions, then
A. $a=1, b=5$
B. $a=5, b=1$
C. $a=-1, b=5$
D. $a=5, b=-1$

## Answer

Given:
Equation 1: $2 x+3 y=7$
Equation 2: $(a+b) x+(2 a-b) y=21$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}=\frac{c_{1}}{c_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=(a+b)$
$b_{1}=3$
$b_{2}=(2 a-b)$
$c_{1}=7$
$c_{2}=21$
Putting the above values in equation (i) we get:
$\frac{2}{a+b}=\frac{3}{2 a-b}=\frac{7}{21}$
On cross multiplication and solving the above equalities we get two sets of linear equation with the variables $\mathrm{a} \& \mathrm{~b}$.
$\Rightarrow 7(a+b)=15^{*} 2 \Rightarrow 7 a+7 b=42$ $\qquad$
$\Rightarrow 7(2 a-b)=15^{*} 3 \Rightarrow 14 a-7 b=63$
Equation (ii) and (iii) are two linear equations with $a$ and $b$ as variables. To solve this two set of linear equations we use the elimination technique.

In the elimination technique one variable is eliminated by equating it's coefficient with the other equation. From equation (ii) and (iii) we first eliminate the variable $b$ and find the value of $a$. Since the coefficient of $b$ are equal but of opposite signs so we add equations (ii) and (iii) On adding we get
$(14+7) a=42+63 \Rightarrow 21 a=105 \Rightarrow a=5$
Putting the value of a in equation (ii) we get
$7 * 5+7 b=42 \Rightarrow 7 b=42-35 \Rightarrow b=1$
The value of $a \& b$ for which the system of equations has infinitely many solutions is $a=5 \& b=1$.

## 6. Question

If the system of equations
$3 x+y=1$
$(2 k-1) x+(k-1) y=2 k+1$
is inconsistent, then $\mathrm{k}=$
A. 1
B. 0
C. -1
D. 2

Answer
Given:
Equation 1: $3 x+y=1$
Equation 2: $(2 k-1) x+(k-1) y=(2 k+1)$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have no solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=3$
$\mathrm{a}_{2}=(2 \mathrm{k}-1)$
$b_{1}=1$
$b_{2}=(k-1)$
$c_{1}=1$
$c_{2}=(2 k+1)$
Putting the above values in equation (i) and solving we get:
$\frac{3}{2 k-1}=\frac{1}{k-1}$
$\Rightarrow 3(\mathrm{k}-1)=2 \mathrm{k}-1 \Rightarrow 3 \mathrm{k}-3=2 \mathrm{k}-1 \Rightarrow \mathrm{k}=3-1 \Rightarrow \mathrm{k}=2$
Therefore $\frac{c_{1}}{c_{2}}=\frac{1}{2 k+1} \Rightarrow \frac{c_{1}}{c_{2}}=\frac{1}{5}$

Putting the value of $k$ we calculate $\frac{a_{1}}{a_{2}}, \frac{b_{1}}{b_{2}} \& \frac{c_{1}}{c_{2}}$
After comparing the ratio we find $\frac{1}{1}=\frac{1}{1} \neq \frac{1}{5}$
So the given system of equations are inconsistent.
The value of $k$ for which the system of equations is inconsistent is $k=\mathbf{2}$
7. Question

If $a m \neq b l$, then the system of equations
$a x+b y=c$
$\mathrm{lx}+\mathrm{my}=\mathrm{n}$
A. has a unique solution
B. has no solution
C. has infinitely many solutions
D. may or may not have a solution.

## Answer

Given:
Equation 1: $\mathrm{ax}+\mathrm{by}=\mathrm{c}$
Equation 2: $\mathrm{lx}+\mathrm{my}=\mathrm{n}$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
According to the problem:
$a_{1}=a$
$a_{2}=1$
$\mathrm{b}_{1}=\mathrm{b}$
$b_{2}=m$
$c_{1}=c$
$c_{2}=n$
According to the question the condition given is
$\mathbf{a m}_{\neq} \mathbf{b l} \ldots$.. $\left.\mathbf{i}\right)$
To develop a relationship between the coefficients we divide both sides of the equation by l*m
After dividing we get
$\frac{\mathbf{a}}{\mathbf{l}} \neq \frac{\mathrm{b}}{\mathrm{m}}$

So $\frac{a_{1}}{a_{2}} \neq \frac{b_{1}}{b_{2}}$
We know from our properties of linear equations that if the ratio of the coefficients of $x$ and $y$ are not equal then their exists a unique solution.
The given system of equation has a unique solution for all values of $x$ and $y$

## 8. Question

If the system of equations
$2 x+3 y=7$
$2 a x+(a+b) y=28$
has infinitely many solutions, then
A. $a=2 b$
B. $b=2 a$
C. $a+2 b=0$
D. $2 a+b=0$

## Answer

Given:
Equation 1: $2 x+3 y=7$
Equation 2: $2 a x+(a+b) y=28$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}=\frac{c_{1}}{c_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=2 a$
$b_{1}=3$
$b_{2}=(a+b)$
$c_{1}=7$
$c_{2}=28$
Putting the above values in equation (i) and solving the extreme left and extreme right portion of the equality we get the value of a
$\frac{2}{2 a}=\frac{7}{28}$
$\Rightarrow 14 \mathrm{a}=56 \Rightarrow \mathrm{a}=4$
We now put the value of a and solve for $b$
$\frac{3}{a+b}=\frac{7}{28} \Rightarrow \frac{3}{a+b}=\frac{1}{4} \Rightarrow a+b=12 \Rightarrow b=8$
So $\mathbf{b}=\mathbf{2 a}$
The correct relationship between a \& $b$ for which the system of equations has infinitely many solution is $b=$ 2a

## 9. Question

The value of k for which the system of equations
$x+2 y=5$
$3 x+k y+15=0$
has no solution is
A. 6
B. -6
C. $3 / 2$
D. None of these

## Answer

Given:
Equation 1: $x+2 y=5$
Equation 2: $3 x+k y=-15$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have no solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$ $\qquad$
According to the problem:
$a_{1}=1$
$a_{2}=3$
$\mathrm{b}_{1}=2$
$b_{2}=\mathrm{k}$
$c_{1}=5$
$c_{2}=-15$
Putting the above values in equation (i) and solving we get:
$\frac{1}{3}=\frac{2}{k}$
$\Rightarrow \mathrm{k}=\mathbf{6}$
Also we find $\frac{1}{3}=\frac{2}{6} \neq \frac{5}{-15}$

## The value of $k$ for which the system of equations has no solution is $k=6$

## 10. Question

If $2 x-3 y=7$ and $(a+b) x-(a+b-3) y=4 a+b$ represent coincident lines, then $a$ and $b$ satisfy the equation
A. $a+5 b=0$
B. $5 \mathrm{a}+\mathrm{b}=0$
C. $a-5 b=0$
D. $5 \mathrm{a}-\mathrm{b}=0$

Answer
Given:
Equation 1: $2 x-3 y=7$
Equation $2:(a+b) x+(a+b-3) y=4 a+b$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
When two sets of linear equations which are coincident then they will have infinite number of solutions since both the equations represent the same line. So we have to use the conditions for the infinitely many number of solution.

For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=a+b$
$b_{1}=-3$
$b_{2}=a+b-3$
$c_{1}=7$
$c_{2}=4 a+b$
Putting the above values in equation (i) and solving the extreme left and middle portion of the equality
$\frac{2}{a+b}=\frac{-3}{a+b-3}$
$\Rightarrow-3(a+b)=2(a+b-3) \Rightarrow 5 a+5 b=6$
Again We Solve for the extreme left and right side of the equality
$\frac{2}{a+b}=\frac{7}{4 a+b}$
$\Rightarrow 8 \mathrm{a}+2 \mathrm{~b}=7 \mathrm{a}+7 \mathrm{~b} \Rightarrow \mathrm{a}=5 \mathrm{~b}$ (iii)
We solve for $\mathbf{a} \& \mathrm{~b}$ from Equation (ii) \& (iii).We substitute the value of a from equation (iii) in equation (ii)
After substituting we get
$5 * 5 b+5 b=6 \Rightarrow 30 b=6 \Rightarrow b=\frac{1}{5}$
Putting the value of $b$ in equation (iii) we get $a=1$
So 5b = a
The relationship between $a$ and $b$ for which the two equations represent coincident line is $a=5 b$ or $a-5 b=0$

## 11. Question

If a pair of linear equations in two variables is consistent, then the lines represented by two equations are
A. intersecting
B. parallel
C. always coincident
D. intersecting or coincident

## Answer

A pair of linear equations is called inconsistent when the lines doesn't have any solution. It means both the lines are parallel to each other.

A pair of linear equations is called consistent when they have infinite number of solutions or they have a unique solution.
An intersecting line will always have a unique solution.
A coincident line will have infinite number of solutions.
So the line represented by a pair of linear equations in two variables is always intersecting or coincident if the system of equation is consistent.

Let $a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ be two lines where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$ $\qquad$
The system of linear equations will have unique solution if
$\frac{a_{1}}{a_{2}} \neq \frac{b_{1}}{b_{2}}$. $\qquad$
For the system of linear equations to be consistent either condition (i) or (ii) must be satisfied.
If the equations are consistent then they are either intersecting or coincident

## 12. Question

The area of the triangle formed by the line $\frac{x}{a}+\frac{y}{b}=1$ with the coordinate axes is
A. $a b$
B. $2 a b$
C. $\frac{1}{2} a b$
D. $\frac{1}{4} \mathrm{ab}$

## Answer

Given:
$\frac{x}{a}+\frac{y}{b}=1$
The given linear equation is in the slope intercept form. Intercept means the distance at which the given equation cuts or meets the coordinate axis. In this problem $a \& b$ are the intercepts on the $x$ and $y$ axis respectively.

The triangle formed by a straight line with the coordinate axis is a right angled triangle where the angle subtended at origin is $90^{\circ}$. So the length of the x intercepts becomes the perpendicular and y intercept becomes the base of the triangle.

We know Area Of a triangle $=\frac{1}{2} *$ (perpendicular length) $*$ (base length)
So Area of the triangle becomes $\frac{1}{2}$ ab
The Area of the triangle is $\frac{1}{2} \mathrm{ab}$

## 13. Question

The area of the triangle formed by the lines $y=x, x=6$ and $y=0$ is
A. 36 sq. units
B. 18 sq. units
C. 9 sq. units
D. 72 sq. units

Answer


Given:

Equation 1: $y=x$ Equation 2: $x=6$ Equation 3: $y=0$
According to the given question Equation $1,2 \& 3$ cuts each other at three different points creating a triangle and we need to calculate the area of this triangle formed by these lines.

Now Equation 2 is a line parallel to $Y$ axis at a distance of 6 units. Equation 3 is the equation of the $x$ axis.
So we can say that equation $2 \& 3$ are mutually perpendicular to each other and the triangle formed by these 3 equations is a right angled triangle .

We solve equation $1 \& 2$ by substitution method
After solving we get $x=6 \& y=6$
So the perpendicular height of the triangle turns out to be 6 units.
Since Equation 2 is at a distance of 6 units from the origin so the length of the base turns out to be 6 units.
Perpendicular height $=6$ units
Base Length $=6$ units.
Area of the Triangle $=\frac{1}{2} *($ perpendicular length $) *$ (base length $)$
Area of the triangle becomes $=\frac{1}{2} * 6 * 6=18$ sq.units
The Area of the triangle is 18 sq. units

## 14. Question

If the system of equations $2 x+3 y=5,4 x+k y=10$ has infinitely many solutions, then $k=$
A. 1
B. $1 / 2$
C. 3
D. 6

Answer
Given:
Equation 1: $2 x+3 y=5$
Equation 2: $4 x+k y=10$
Both the equations are in the form of ;
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have infinitely many solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}}=\frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$a_{1}=2$
$a_{2}=4$
$\mathrm{b}_{1}=3$
$b_{2}=k$
$c_{1}=5$
$c_{2}=10$
Putting the above values in equation (i) and solving the extreme left and extreme right portion of the equality we get the value of a
$\frac{2}{4}=\frac{3}{k}$
$\Rightarrow 2 \mathrm{k}=12 \Rightarrow \mathrm{k}=6$
The value of $k$ for which the system of equations has infinitely many solution is $k=6$

## 15. Question

If the system of equations $k x-5 y=2,6 x+2 y=7$ has no solution, then $k=$
A. -10
B. -5
C. -6
D. -15

## Answer

Given:
Equation 1: kx - $5 y=2$
Equation 2: $6 x+2 y=7$
Both the equations are in the form of :
$a_{1} x+b_{1} y=c_{1} \& a_{2} x+b_{2} y=c_{2}$ where
$a_{1} \& a_{2}$ are the coefficients of $x$
$b_{1} \& b_{2}$ are the coefficients of $y$
$c_{1} \& c_{2}$ are the constants
For the system of linear equations to have no solutions we must have
$\frac{\mathrm{a}_{1}}{\mathrm{a}_{2}}=\frac{\mathrm{b}_{1}}{\mathrm{~b}_{2}} \neq \frac{\mathrm{c}_{1}}{\mathrm{c}_{2}}$
According to the problem:
$\mathrm{a}_{1}=\mathrm{k}$
$a_{2}=6$
$\mathrm{b}_{1}=-5$
$b_{2}=2$
$c_{1}=2$
$c_{2}=7$
Putting the above values in equation (i) and solving we get:
$\frac{k}{6}=\frac{-5}{2}$
$\Rightarrow k=\frac{-5 * 6}{2} \Rightarrow k=-15$
Also we find $\frac{-15}{6}=\frac{-5}{2} \neq \frac{2}{7}$
The value of $k$ for which the system of equations has no solution is $k=-15$

## 16. Question

The area of the triangle formed by the lines $x=3, y=4$ and $x=y$ is
A. $1 / 2$ sq. unit
B. 1 sq. unit
C. 2 sq. unit
D. None of these

## Answer

Given :
Equation 1: $x=3$
Equation 2: $y=4$
Equation 3: $\mathrm{x}=\mathrm{y}$


Equation 1 is a line parallel to $y$ axis
Equation 2 is a line parallel to $x$ axis
So Equation $1 \& 2$ are mutually perpendicular to each other.
Hence the triangle formed is a right angled triangle.
First we solve the three lines simultaneously by method of substitution and get the three points of intersection or three coordinates of the triangle.

Solving Equation $1 \& 2$ we get the coordinate ( 3,4 ). Let this Coordinate name be $\mathrm{P}_{1}$
Solving Equation $2 \& 3$ we get the coordinate ( 4,4 ). Let this Coordinate name be $P_{2}$
Solving Equation $3 \& 1$ we get the coordinate ( 3,3 ). Let this Coordinate name be $P_{3}$
We now use the formula for Area of a triangle through 3 given points
Area $=\frac{1}{2} *\left|x_{1} *\left(y_{2}-y_{3}\right)+x_{2} *\left(y_{3}-y_{1}\right)+x_{3} *\left(y_{1}-y_{2}\right)\right|$

Where $x_{1}, y_{1}$ are the coordinates of $P_{1}$
$x_{2}, y_{2}$ are the coordinates of $P_{2}$
$x_{3}, y_{3}$ are the coordinates of $P_{3}$
Area of the Given Triangle $=\frac{1}{2} *|3 *(4-3)+4 *(3-4)+3 *(4-4)|$
Area $=\frac{1}{2} *\left|3^{*}(1)+4 *(-1)+3^{*}(0)\right|$
Area $=\frac{1}{2} *|3-4| \Rightarrow$ Area $=\frac{1}{2}$ sq. units
The Area of the triangle is $\frac{1}{2}$ sq. units

## 17. Question

The area of the triangle formed by the lines $2 x+3 y=12, x-y-1=0$ and $x=0$ (as shown in Fig. 3.23), is


Fig. 3.23
A. 7 sq. units
B. 7.5 sq. units
C. 6.5 sq. units
D. 6 sq. units

## Answer

Given
Equation 1: $2 x+3 y=12$ Equation 2: $x-y=1$ Equation $3: x=0$
To calculate the Area at first we solve the Equation $1 \& 2$ Simultaneously by method of substitution.
We substitute the value of $x$ from Equation 2 in Equation 1 to get the value of $y$
Equation 2: $x-y=1 \Rightarrow x=y+1$
Equation 1: $2 x+3 y=12$
Substituting the value from equation 2 we get
$2(y+1)+3 y=12 \Rightarrow 2 y+2+3 y=12 \Rightarrow 5 y=10 \Rightarrow y=2$

Putting the value in Equation 1 we get
$x=2+1 \Rightarrow x=3$
So both this lines passes through $(3,2)$ Let this Coordinate name be $P_{1}$
Equation 3 is the equation for $y$ axis
Equation 1 meets $Y$ axis at $(0,4)$ which is calculated by substituting $x=0$ in Equation 1. Let this Coordinate name be $P_{2}$
Equation 2 meets $Y$ axis at $(0,-1)$ which is calculated by substituting $x=0$ in Equation 2. Let this Coordinate name be $P_{3}$
So Area of the triangle $=\frac{1}{2} *\left|x_{1} *\left(y_{2}-y_{3}\right)+x_{2} *\left(y_{3}-y_{1}\right)+x_{3} *\left(y_{1}-y_{2}\right)\right|$
Where $\mathrm{x}_{1}, \mathrm{y}_{1}$ are the coordinates of $\mathrm{P}_{1}$
$x_{2}, y_{2}$ are the coordinates of $P_{2}$
$x_{3}, y_{3}$ are the coordinates of $P_{3}$
$\Rightarrow$ Area of the Given Triangle $=\frac{1}{2} *\left|3^{*}(4+1)+0 *(-1-2)+0 *(2-4)\right|$
$\Rightarrow$ Area of the Given Triangle $=\frac{1}{2} *|3 * 5|$
$\Rightarrow$ Area $=\frac{15}{2} \Rightarrow$ Area $=$ 7.5 Sq. Units
Area of the triangle is 7.5 sq. Units

