## 14. Quadratic Equations

## Exercise 14.1

## 1. Question

Solve the following quadratic equations by factorization method $x^{2}+1=0$

## Answer

Given $x^{2}+1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$\mathrm{x}^{2}-\mathrm{i}^{2}=0$
$\Rightarrow(x+i)(x-i)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}+\mathrm{i}=0$ or $\mathrm{x}-\mathrm{i}=0$
$\Rightarrow \mathrm{x}=-\mathrm{i}$ or $\mathrm{x}=\mathrm{i}$
$\therefore \mathrm{x}= \pm \mathrm{i}$
Thus, the roots of the given equation are $\pm \mathrm{i}$.

## 2. Question

Solve the following quadratic equations by factorization method
$9 x^{2}+4=0$

## Answer

Given $9 x^{2}+4=0$
$\Rightarrow 9 x^{2}+4 \times 1=0$
We have $\mathrm{i}^{2}=-1 \Rightarrow 1=-\mathrm{i}^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$9 x^{2}+4\left(-i^{2}\right)=0$
$\Rightarrow 9 x^{2}-4 i^{2}=0$
$\Rightarrow(3 \mathrm{x})^{2}-(2 \mathrm{i})^{2}=0$
$\Rightarrow(3 x+2 i)(3 x-2 i)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow 3 \mathrm{x}+2 \mathrm{i}=0$ or $3 \mathrm{x}-2 \mathrm{i}=0$
$\Rightarrow 3 \mathrm{x}=-2 \mathrm{i}$ or $3 \mathrm{x}=2 \mathrm{i}$
$\Rightarrow \mathrm{x}=-\frac{2}{3} \mathrm{i}$ or $\frac{2}{3} \mathrm{i}$
$\therefore \mathrm{x}= \pm \frac{2}{3} \mathrm{i}$
Thus, the roots of the given equation are $\pm \frac{2}{3} \mathrm{i}$.

## 3. Question

Solve the following quadratic equations by factorization method
$x^{2}+2 x+5=0$

## Answer

Given $x^{2}+2 x+5=0$
$\Rightarrow \mathrm{x}^{2}+2 \mathrm{x}+1+4=0$
$\Rightarrow x^{2}+2(x)(1)+1^{2}+4=0$
$\Rightarrow(x+1)^{2}+4=0\left[\because(a+b)^{2}=a^{2}+2 a b+b^{2}\right]$
$\Rightarrow(x+1)^{2}+4 \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$(x+1)^{2}+4\left(-i^{2}\right)=0$
$\Rightarrow(x+1)^{2}-4 i^{2}=0$
$\Rightarrow(\mathrm{x}+1)^{2}-(2 \mathrm{i})^{2}=0$
$\Rightarrow(x+1+2 i)(x+1-2 i)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}+1+2 \mathrm{i}=0$ or $\mathrm{x}+1-2 \mathrm{i}=0$
$\Rightarrow \mathrm{x}=-1-2 \mathrm{i}$ or $\mathrm{x}=-1+2 \mathrm{i}$
$\therefore \mathrm{x}=-1 \pm 2 \mathrm{i}$
Thus, the roots of the given equation are $-1 \pm 2 \mathrm{i}$.

## 4. Question

Solve the following quadratic equations by factorization method
$4 x^{2}-12 x+25=0$

## Answer

Given $4 x^{2}-12 x+25=0$
$\Rightarrow 4 x^{2}-12 x+9+16=0$
$\Rightarrow(2 x)^{2}-2(2 x)(3)+3^{2}+16=0$
$\Rightarrow(2 x-3)^{2}+16=0\left[\because(a+b)^{2}=a^{2}+2 a b+b^{2}\right]$
$\Rightarrow(2 x-3)^{2}+16 \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$(2 x-3)^{2}+16\left(-i^{2}\right)=0$
$\Rightarrow(2 \mathrm{x}-3)^{2}-16 \mathrm{i}^{2}=0$
$\Rightarrow(2 x-3)^{2}-(4 i)^{2}=0$
Since $a^{2}-b^{2}=(a+b)(a-b)$, we get
$(2 x-3+4 i)(2 x-3-4 i)=0$
$\Rightarrow 2 \mathrm{x}-3+4 \mathrm{i}=0$ or $2 \mathrm{x}-3-4 \mathrm{i}=0$
$\Rightarrow 2 x=3-4 i$ or $2 x=3+4 i$
$\Rightarrow x=\frac{3-4 i}{2}$ or $\frac{3+4 i}{2}$
$\Rightarrow x=\frac{3}{2}-2 i$ or $\frac{3}{2}+2 i$
$\therefore \mathrm{x}=\frac{3}{2} \pm 2 \mathrm{i}$
Thus, the roots of the given equation $\operatorname{are} \frac{3}{2} \pm 2 \mathrm{i}$.

## 5. Question

Solve the following quadratic equations by factorization method
$x^{2}+x+1=0$

## Answer

Given $x^{2}+x+1=0$
$\Rightarrow x^{2}+x+\frac{1}{4}+\frac{3}{4}=0$
$\Rightarrow x^{2}+2(x)\left(\frac{1}{2}\right)+\left(\frac{1}{2}\right)^{2}+\frac{3}{4}=0$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4}=0\left[\because(a+b)^{2}=a^{2}+2 a b+b^{2}\right]$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4} \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4}\left(-i^{2}\right)=0$
$\Rightarrow\left(\mathrm{x}+\frac{1}{2}\right)^{2}-\frac{3}{4} \mathrm{i}^{2}=0$
$\Rightarrow\left(\mathrm{x}+\frac{1}{2}\right)^{2}-\left(\frac{\sqrt{3}}{2} \mathrm{i}\right)^{2}=0$
$\Rightarrow\left(x+\frac{1}{2}+\frac{\sqrt{3}}{2} i\right)\left(x+\frac{1}{2}-\frac{\sqrt{3}}{2} i\right)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}+\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}=0$ or $\mathrm{x}+\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}=-\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}=0$ or $\mathrm{x}=-\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}$
$\therefore \mathrm{x}=-\frac{1}{2} \pm \frac{\sqrt{3}}{2} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{1}{2} \pm \frac{\sqrt{3}}{2} \mathrm{i}$.

## 6. Question

Solve the following quadratics
$4 x^{2}+1=0$

Given $4 x^{2}+1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$4 \mathrm{x}^{2}-\mathrm{i}^{2}=0$
$\Rightarrow(2 x)^{2}-\mathrm{i}^{2}=0$
$\Rightarrow(2 x+i)(2 x-i)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow 2 \mathrm{x}+\mathrm{i}=0$ or $2 \mathrm{x}-\mathrm{i}=0$
$\Rightarrow 2 \mathrm{x}=-\mathrm{i}$ or $2 \mathrm{x}=\mathrm{i}$
$\Rightarrow \mathrm{x}=-\frac{1}{2} \mathrm{i}$ or $\frac{1}{2} \mathrm{i}$
$\therefore \mathrm{x}= \pm \frac{1}{2} \mathrm{i}$
Thus, the roots of the given equation are $\pm \frac{1}{2} \mathrm{i}$.

## 7. Question

Solve the following quadratics
$x^{2}-4 x+7=0$

## Answer

Given $x^{2}-4 x+7=0$
$\Rightarrow x^{2}-4 x+4+3=0$
$\Rightarrow x^{2}-2(x)(2)+2^{2}+3=0$
$\Rightarrow(x-2)^{2}+3=0\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
$\Rightarrow(x-2)^{2}+3 \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$(x-2)^{2}+3\left(-i^{2}\right)=0$
$\Rightarrow(\mathrm{x}-2)^{2}-3 \mathrm{i}^{2}=0$
$\Rightarrow(x-2)^{2}-(\sqrt{3} i)^{2}=0$
Since $a^{2}-b^{2}=(a+b)(a-b)$, we get
$(x-2+\sqrt{3} i)(x-2-\sqrt{3} i)=0$
$\Rightarrow \mathrm{x}-2+\sqrt{3} \mathrm{i}=0$ or $\mathrm{x}-2-\sqrt{3} \mathrm{i}=0$
$\Rightarrow \mathrm{x}=2-\sqrt{3} \mathrm{i}$ or $\mathrm{x}=2+\sqrt{3} \mathrm{i}$
$\therefore \mathrm{x}=2 \pm \sqrt{3} \mathrm{i}$
Thus, the roots of the given equation are $2 \pm \sqrt{3} \mathrm{i}$.

## 8. Question

Solve the following quadratics
$x^{2}+2 x+2=0$

## Answer

Given $x^{2}+2 x+2=0$
$\Rightarrow \mathrm{x}^{2}+2 \mathrm{x}+1+1=0$
$\Rightarrow x^{2}+2(x)(1)+1^{2}+1=0$
$\Rightarrow(x+1)^{2}+1=0\left[\because(a+b)^{2}=a^{2}+2 a b+b^{2}\right]$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$(x+1)^{2}+\left(-i^{2}\right)=0$
$\Rightarrow(\mathrm{x}+1)^{2}-\mathrm{i}^{2}=0$
$\Rightarrow(x+1)^{2}-(i)^{2}=0$
$\Rightarrow(x+1+i)(x+1-i)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}+1+\mathrm{i}=0$ or $\mathrm{x}+1-\mathrm{i}=0$
$\Rightarrow \mathrm{x}=-1-\mathrm{i}$ or $\mathrm{x}=-1+\mathrm{i}$
$\therefore \mathrm{x}=-1 \pm \mathrm{i}$
Thus, the roots of the given equation are $-1 \pm i$.

## 9. Question

Solve the following quadratics
$5 x^{2}-6 x+2=0$

## Answer

Given $5 x^{2}-6 x+2=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=5, b=-6$ and $c=2$
$\Rightarrow x=\frac{-(-6) \pm \sqrt{(-6)^{2}-4(5)(2)}}{2(5)}$
$\Rightarrow x=\frac{6 \pm \sqrt{36-40}}{10}$
$\Rightarrow x=\frac{6 \pm \sqrt{-4}}{10}$
$\Rightarrow \mathrm{x}=\frac{6 \pm \sqrt{4(-1)}}{10}$
We have $\mathrm{i}^{2}=-1$
By substituting -1 = $\mathrm{i}^{2}$ in the above equation, we get
$x=\frac{6 \pm \sqrt{4 \mathrm{i}^{2}}}{10}$
$\Rightarrow \mathrm{x}=\frac{6 \pm \sqrt{(2 \mathrm{i})^{2}}}{10}$
$\Rightarrow x=\frac{6 \pm 2 i}{10}$
$\Rightarrow x=\frac{2(3 \pm i)}{10}$
$\Rightarrow \mathrm{x}=\frac{3 \pm \mathrm{i}}{5}$
$\therefore \mathrm{x}=\frac{3}{5} \pm \frac{1}{5} \mathrm{i}$
Thus, the roots of the given equation $\operatorname{are} \frac{3}{5} \pm \frac{1}{5} \mathrm{i}$.

## 10. Question

Solve the following quadratics
$21 x^{2}+9 x+1=0$

## Answer

Given $21 x^{2}+9 x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=21, b=9$ and $c=1$
$\Rightarrow \mathrm{x}=\frac{-9 \pm \sqrt{9^{2}-4(21)(1)}}{2(21)}$
$\Rightarrow x=\frac{-9 \pm \sqrt{81-84}}{42}$
$\Rightarrow \mathrm{x}=\frac{-9 \pm \sqrt{-3}}{42}$
$\Rightarrow \mathrm{x}=\frac{-9 \pm \sqrt{3(-1)}}{42}$
We have $\mathrm{i}^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$x=\frac{-9 \pm \sqrt{3 \mathrm{i}^{2}}}{42}$
$\Rightarrow x=\frac{-9 \pm \sqrt{(\sqrt{3} \mathrm{i})^{2}}}{42}$
$\Rightarrow x=\frac{-9 \pm \sqrt{3} i}{42}$
$\Rightarrow \mathrm{x}=-\frac{9}{42} \pm \frac{\sqrt{3}}{42} \mathrm{i}$
$\therefore \mathrm{x}=-\frac{3}{14} \pm \frac{\sqrt{3}}{42} \mathrm{i}$

Thus, the roots of the given equation are $-\frac{3}{14} \pm \frac{\sqrt{3}}{42} \mathrm{i}$.

## 11. Question

Solve the following quadratics
$x^{2}-x+1=0$

## Answer

Given $x^{2}-x+1=0$
$\Rightarrow \mathrm{x}^{2}-\mathrm{x}+\frac{1}{4}+\frac{3}{4}=0$
$\Rightarrow x^{2}-2(x)\left(\frac{1}{2}\right)+\left(\frac{1}{2}\right)^{2}+\frac{3}{4}=0$
$\Rightarrow\left(x-\frac{1}{2}\right)^{2}+\frac{3}{4}=0\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
$\Rightarrow\left(x-\frac{1}{2}\right)^{2}+\frac{3}{4} \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$\left(x-\frac{1}{2}\right)^{2}+\frac{3}{4}\left(-i^{2}\right)=0$
$\Rightarrow\left(\mathrm{x}-\frac{1}{2}\right)^{2}-\frac{3}{4} \mathrm{i}^{2}=0$
$\Rightarrow\left(x-\frac{1}{2}\right)^{2}-\left(\frac{\sqrt{3}}{2} \mathrm{i}\right)^{2}=0$
$\Rightarrow\left(x-\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}\right)\left(\mathrm{x}-\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}\right)=0\left[\because \mathrm{a}^{2}-\mathrm{b}^{2}=(\mathrm{a}+\mathrm{b})(\mathrm{a}-\mathrm{b})\right]$
$\Rightarrow \mathrm{x}-\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}=0$ or $\mathrm{x}-\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}=\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}=0$ or $\mathrm{x}=\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}$
$\therefore \mathrm{x}=\frac{1}{2} \pm \frac{\sqrt{3}}{2} \mathrm{i}$
Thus, the roots of the given equation are $\frac{1}{2} \pm \frac{\sqrt{3}}{2} \mathrm{i}$.

## 12. Question

Solve the following quadratics
$x^{2}+x+1=0$

## Answer

Given $x^{2}+x+1=0$
$\Rightarrow x^{2}+x+\frac{1}{4}+\frac{3}{4}=0$
$\Rightarrow x^{2}+2(x)\left(\frac{1}{2}\right)+\left(\frac{1}{2}\right)^{2}+\frac{3}{4}=0$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4}=0\left[\because(a+b)^{2}=a^{2}+2 a b+b^{2}\right]$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4} \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$\left(x+\frac{1}{2}\right)^{2}+\frac{3}{4}\left(-i^{2}\right)=0$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}-\frac{3}{4} \mathrm{i}^{2}=0$
$\Rightarrow\left(x+\frac{1}{2}\right)^{2}-\left(\frac{\sqrt{3}}{2} \mathrm{i}\right)^{2}=0$
$\Rightarrow\left(x+\frac{1}{2}+\frac{\sqrt{3}}{2} i\right)\left(x+\frac{1}{2}-\frac{\sqrt{3}}{2} i\right)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow x+\frac{1}{2}+\frac{\sqrt{3}}{2} i=0$ or $x+\frac{1}{2}-\frac{\sqrt{3}}{2} i=0$
$\Rightarrow x=-\frac{1}{2}-\frac{\sqrt{3}}{2} \mathrm{i}=0$ or $\mathrm{x}=-\frac{1}{2}+\frac{\sqrt{3}}{2} \mathrm{i}$
$\therefore x=-\frac{1}{2} \pm \frac{\sqrt{3}}{2} i$
Thus, the roots of the given equation are $-\frac{1}{2} \pm \frac{\sqrt{3}}{2} \mathrm{i}$.

## 13. Question

Solve the following quadratics
$17 x^{2}-8 x+1=0$

## Answer

Given $17 x^{2}-8 x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=17, b=-8$ and $c=1$
$\Rightarrow x=\frac{-(-8) \pm \sqrt{(-8)^{2}-4(17)(1)}}{2(17)}$
$\Rightarrow \mathrm{X}=\frac{8 \pm \sqrt{64-68}}{34}$
$\Rightarrow \mathrm{x}=\frac{8 \pm \sqrt{-4}}{34}$
$\Rightarrow \mathrm{x}=\frac{8 \pm \sqrt{4(-1)}}{34}$
We have $\mathrm{i}^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{8 \pm \sqrt{4 \mathrm{i}^{2}}}{34}$
$\Rightarrow \mathrm{x}=\frac{8 \pm \sqrt{(2 \mathrm{i})^{2}}}{34}$
$\Rightarrow \mathrm{x}=\frac{8 \pm 2 \mathrm{i}}{34}$
$\Rightarrow x=\frac{2(4 \pm i)}{34}$
$\Rightarrow x=\frac{4 \pm i}{17}$
$\therefore x=\frac{4}{17} \pm \frac{1}{17} \mathrm{i}$
Thus, the roots of the given equation are $\frac{4}{17} \pm \frac{1}{17} \mathrm{i}$.

## 14. Question

Solve the following quadratics
$27 x^{2}-10 x+1=0$

## Answer

Given $27 x^{2}-10 x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=27, b=-10$ and $c=1$
$\Rightarrow x=\frac{-(-10) \pm \sqrt{(-10)^{2}-4(27)(1)}}{2(27)}$
$\Rightarrow x=\frac{10 \pm \sqrt{100-108}}{54}$
$\Rightarrow x=\frac{10 \pm \sqrt{-8}}{54}$
$\Rightarrow \mathrm{x}=\frac{10 \pm \sqrt{8(-1)}}{54}$
We have $i^{2}=-1$
By substituting -1 $=\mathrm{i}^{2}$ in the above equation, we get
$\mathrm{x}=\frac{10 \pm \sqrt{8 \mathrm{i}^{2}}}{54}$
$\Rightarrow \mathrm{x}=\frac{10 \pm \sqrt{(2 \sqrt{2} \mathrm{i})^{2}}}{54}$
$\Rightarrow \mathrm{x}=\frac{10 \pm 2 \sqrt{2} \mathrm{i}}{54}$
$\Rightarrow x=\frac{2(5 \pm \sqrt{2} i)}{54}$
$\Rightarrow \mathrm{x}=\frac{5 \pm \sqrt{2} \mathrm{i}}{27}$
$\therefore x=\frac{5}{27} \pm \frac{\sqrt{2}}{27} i$
Thus, the roots of the given equation are $\frac{5}{27} \pm \frac{\sqrt{2}}{27} \mathrm{i}$.
15. Question

Solve the following quadratics
$17 x^{2}+28 x+12=0$

## Answer

Given $17 x^{2}+28 x+12=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=17, b=28$ and $c=12$
$\Rightarrow \mathrm{x}=\frac{-28 \pm \sqrt{28^{2}-4(17)(12)}}{2(17)}$
$\Rightarrow x=\frac{-28 \pm \sqrt{784-816}}{34}$
$\Rightarrow x=\frac{-28 \pm \sqrt{-32}}{34}$
$\Rightarrow x=\frac{-28 \pm \sqrt{32(-1)}}{34}$
We have $\mathrm{i}^{2}=-1$
By substituting -1 $=\mathrm{i}^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-28 \pm \sqrt{32 \mathrm{i}^{2}}}{34}$
$\Rightarrow x=\frac{-28 \pm \sqrt{(4 \sqrt{2} i)^{2}}}{34}$
$\Rightarrow x=\frac{-28 \pm 4 \sqrt{2} i}{34}$
$\Rightarrow \mathrm{x}=\frac{2(-14 \pm 2 \sqrt{2} \mathrm{i})}{34}$
$\Rightarrow x=\frac{-14 \pm 2 \sqrt{2} i}{17}$
$\therefore x=-\frac{14}{17} \pm \frac{2 \sqrt{2}}{17} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{14}{17} \pm \frac{2 \sqrt{2}}{17} \mathrm{i}$.

## 16. Question

Solve the following quadratics
$21 x^{2}-28 x+10=0$

## Answer

Given $21 x^{2}-28 x+10=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 \mathbf{a c}}}{2 \mathbf{a}}$
Here, $a=21, b=-28$ and $c=10$
$\Rightarrow x=\frac{-(-28) \pm \sqrt{(-28)^{2}-4(21)(10)}}{2(21)}$
$\Rightarrow \mathrm{x}=\frac{28 \pm \sqrt{784-840}}{42}$
$\Rightarrow \mathrm{x}=\frac{28 \pm \sqrt{-56}}{42}$
$\Rightarrow \mathrm{x}=\frac{28 \pm \sqrt{56(-1)}}{42}$
We have $\mathrm{i}^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{28 \pm \sqrt{56 \mathrm{i}^{2}}}{42}$
$\Rightarrow x=\frac{28 \pm \sqrt{(2 \sqrt{14} i)^{2}}}{42}$
$\Rightarrow \mathrm{x}=\frac{28 \pm 2 \sqrt{14} \mathrm{i}}{42}$
$\Rightarrow x=\frac{2(14 \pm \sqrt{14} \mathrm{i})}{42}$
$\Rightarrow \mathrm{x}=\frac{14 \pm \sqrt{14} \mathrm{i}}{21}$
$\Rightarrow x=\frac{14}{21} \pm \frac{\sqrt{14}}{21} \mathrm{i}$
$\therefore \mathrm{X}=\frac{2}{3} \pm \frac{\sqrt{14}}{21} \mathrm{i}$
Thus, the roots of the given equation $\operatorname{are} \frac{2}{3} \pm \frac{\sqrt{14}}{21} \mathrm{i}$.

## 17. Question

Solve the following quadratics
$8 x^{2}-9 x+3=0$

## Answer

Given $8 x^{2}-9 x+3=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$\mathbf{x}=\frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^{2}-4 \mathbf{a c}}}{2 \mathbf{a}}$
Here, $a=8, b=-9$ and $c=1$
$\Rightarrow x=\frac{-(-9) \pm \sqrt{(-9)^{2}-4(8)(3)}}{2(8)}$
$\Rightarrow x=\frac{9 \pm \sqrt{81-96}}{16}$
$\Rightarrow x=\frac{9 \pm \sqrt{-15}}{16}$
$\Rightarrow x=\frac{9 \pm \sqrt{15(-1)}}{16}$
We have $\mathrm{i}^{2}=-1$
By substituting -1 $=\mathrm{i}^{2}$ in the above equation, we get
$x=\frac{9 \pm \sqrt{15 \mathrm{i}^{2}}}{16}$
$\Rightarrow x=\frac{9 \pm \sqrt{(\sqrt{15} i)^{2}}}{16}$
$\Rightarrow x=\frac{9 \pm \sqrt{15} i}{16}$
$\therefore x=\frac{9}{16} \pm \frac{\sqrt{15}}{16} i$
Thus, the roots of the given equation are $\frac{9}{16} \pm \frac{\sqrt{15}}{16} \mathrm{i}$.

## 18. Question

Solve the following quadratics
$13 x^{2}+7 x+1=0$

## Answer

Given $13 x^{2}+7 x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=13, b=7$ and $c=1$
$\Rightarrow \mathrm{x}=\frac{-7 \pm \sqrt{7^{2}-4(13)(1)}}{2(13)}$
$\Rightarrow x=\frac{-7 \pm \sqrt{49-52}}{26}$
$\Rightarrow x=\frac{-7 \pm \sqrt{-3}}{26}$
$\Rightarrow x=\frac{-7 \pm \sqrt{3(-1)}}{26}$

We have $i^{2}=-1$
By substituting -1 $=i^{2}$ in the above equation, we get
$x=\frac{-7 \pm \sqrt{3 \mathrm{i}^{2}}}{26}$
$\Rightarrow x=\frac{-7 \pm \sqrt{(\sqrt{3} \mathrm{i})^{2}}}{26}$
$\Rightarrow x=\frac{-7 \pm \sqrt{3} \mathrm{i}}{26}$
$\therefore x=-\frac{7}{26} \pm \frac{\sqrt{3}}{26} i$
Thus, the roots of the given equation are $-\frac{7}{26} \pm \frac{\sqrt{3}}{26} \mathrm{i}$.
19. Question
$2 x^{2}+x+1=0$

## Answer

Given $2 x^{2}+x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=2, b=1$ and $c=1$
$\Rightarrow x=\frac{-1 \pm \sqrt{1^{2}-4(2)(1)}}{2(2)}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1-8}}{4}$
$\Rightarrow x=\frac{-1 \pm \sqrt{-7}}{4}$
$\Rightarrow x=\frac{-1 \pm \sqrt{7(-1)}}{4}$
We have $\mathrm{i}^{2}=-1$
By substituting -1 $=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-1 \pm \sqrt{7 \mathrm{i}^{2}}}{4}$
$\Rightarrow x=\frac{-1 \pm \sqrt{(\sqrt{7} \mathrm{i})^{2}}}{4}$
$\Rightarrow x=\frac{-1 \pm \sqrt{7} i}{4}$
$\therefore x=-\frac{1}{4} \pm \frac{\sqrt{7}}{4} i$
Thus, the roots of the given equation are $-\frac{1}{4} \pm \frac{\sqrt{7}}{4} \mathrm{i}$.

## 20. Question

Prove: $\sqrt{3} x^{2}-\sqrt{2} x+3 \sqrt{3}=0$

## Answer

Given $\sqrt{3} \mathrm{x}^{2}-\sqrt{2} \mathrm{x}+3 \sqrt{3}=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

Here, $\mathrm{a}=\sqrt{3}, \mathrm{~b}=-\sqrt{2}$ and $\mathrm{c}=3 \sqrt{3}$
$\Rightarrow \mathrm{x}=\frac{-(-\sqrt{2}) \pm \sqrt{(-\sqrt{2})^{2}-4(\sqrt{3})(3 \sqrt{3})}}{2(\sqrt{3})}$
$\Rightarrow \mathrm{x}=\frac{\sqrt{2} \pm \sqrt{2-36}}{2 \sqrt{3}}$
$\Rightarrow x=\frac{\sqrt{2} \pm \sqrt{-34}}{2 \sqrt{3}}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{34(-1)}}{2 \sqrt{3}}$
We have $\mathrm{i}^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{34 \mathrm{i}^{2}}}{2 \sqrt{3}}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{(\sqrt{34} \mathrm{i})^{2}}}{2 \sqrt{3}}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{34} \mathrm{i}}{2 \sqrt{3}}$
$\therefore \mathrm{x}=-\frac{\sqrt{2}}{2 \sqrt{3}} \pm \frac{\sqrt{34}}{2 \sqrt{3}} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{\sqrt{2}}{2 \sqrt{3}} \pm \frac{\sqrt{34}}{2 \sqrt{3}} \mathrm{i}$.

## 21. Question

Solve the following quadratics $\sqrt{2} x^{2}+x+\sqrt{2}=0$

## Answer

Given $\sqrt{2} \mathrm{x}^{2}+\mathrm{x}+\sqrt{2}=0$
Recall that the roots of quadratic equation $a x^{\mathbf{2}}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $\mathrm{a}=\sqrt{2}, \mathrm{~b}=1$ and $\mathrm{c}=\sqrt{2}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1^{2}-4(\sqrt{2})(\sqrt{2})}}{2(\sqrt{2})}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1-8}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{-7}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{7(-1)}}{2 \sqrt{2}}$
We have $i^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$x=\frac{-1 \pm \sqrt{7 i^{2}}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{(\sqrt{7} \mathrm{i})^{2}}}{2 \sqrt{2}}$
$\Rightarrow x=\frac{-1 \pm \sqrt{7} i}{2 \sqrt{2}}$
$\therefore \mathrm{x}=-\frac{1}{2 \sqrt{2}} \pm \frac{\sqrt{7}}{2 \sqrt{2}} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{1}{2 \sqrt{2}} \pm \frac{\sqrt{7}}{2 \sqrt{2}}$ i.

## 22. Question

Solve the following quadratics $x^{2}+x+\frac{1}{\sqrt{2}}=0$

## Answer

Given $\mathrm{x}^{2}+\mathrm{x}+\frac{1}{\sqrt{2}}=0$
$\Rightarrow\left(\mathrm{x}^{2}+\mathrm{x}+\frac{1}{\sqrt{2}}\right) \times \sqrt{2}=0 \times \sqrt{2}$
$\Rightarrow \sqrt{2} x^{2}+\sqrt{2} x+1=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $\mathrm{a}=\sqrt{2}, \mathrm{~b}=\sqrt{2}$ and $\mathrm{c}=1$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{(\sqrt{2})^{2}-4(\sqrt{2})(1)}}{2(\sqrt{2})}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{2-4 \sqrt{2}}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{2(1-2 \sqrt{2})}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{2} \pm \sqrt{2} \times \sqrt{1-2 \sqrt{2}}}{2 \sqrt{2}}$
$\Rightarrow x=\frac{\sqrt{2}(-1 \pm \sqrt{1-2 \sqrt{2}})}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1-2 \sqrt{2}}}{2}$
$\Rightarrow x=\frac{-1 \pm \sqrt{(2 \sqrt{2}-1)(-1)}}{2}$
We have $i^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-1 \pm \sqrt{(2 \sqrt{2}-1) \mathrm{i}^{2}}}{2}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{(\sqrt{2 \sqrt{2}-1 \mathrm{i}})^{2}}}{2}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{2 \sqrt{2}-1} \mathrm{i}}{2}$
$\therefore \mathrm{x}=-\frac{1}{2} \pm \frac{\sqrt{2 \sqrt{2}-1}}{2} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{1}{2} \pm \frac{\sqrt{2 \sqrt{2}-1}}{2}$.

## 23. Question

Solve: $x^{2}+\frac{x}{\sqrt{2}}+1=0$

## Answer

Given $\mathrm{x}^{2}+\frac{\mathrm{x}}{\sqrt{2}}+1=0$
$\Rightarrow\left(\mathrm{x}^{2}+\frac{\mathrm{x}}{\sqrt{2}}+1\right) \times \sqrt{2}=0 \times \sqrt{2}$
$\Rightarrow \sqrt{2} x^{2}+x+\sqrt{2}=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$\mathbf{x}=\frac{-\mathbf{b} \pm \sqrt{\mathbf{b}^{2}-4 \mathbf{a c}}}{2 \mathbf{a}}$
Here, $\mathrm{a}=\sqrt{2}, \mathrm{~b}=1$ and $\mathrm{c}=\sqrt{2}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1^{2}-4(\sqrt{2})(\sqrt{2})}}{2(\sqrt{2})}$
$\Rightarrow x=\frac{-1 \pm \sqrt{1-8}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{-7}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{7(-1)}}{2 \sqrt{2}}$
We have $\mathrm{i}^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-1 \pm \sqrt{7 \mathrm{i}^{2}}}{2 \sqrt{2}}$
$\Rightarrow x=\frac{-1 \pm \sqrt{(\sqrt{7} \mathrm{i})^{2}}}{2 \sqrt{2}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{7} \mathrm{i}}{2 \sqrt{2}}$
$\therefore \mathrm{x}=-\frac{1}{2 \sqrt{2}} \pm \frac{\sqrt{7}}{2 \sqrt{2}} \mathrm{i}$
Thus, the roots of the given equation are $-\frac{1}{2 \sqrt{2}} \pm \frac{\sqrt{7}}{2 \sqrt{2}} \mathrm{i}$.

## 24. Question

Solve the following quadratics $\sqrt{5} \mathrm{x}^{2}+\mathrm{x}+\sqrt{5}=0$

## Answer

Given $\sqrt{5} x^{2}+x+\sqrt{5}=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=\sqrt{5}, b=1$ and $c=\sqrt{5}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1^{2}-4(\sqrt{5})(\sqrt{5})}}{2(\sqrt{5})}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{1-20}}{2 \sqrt{5}}$
$\Rightarrow x=\frac{-1 \pm \sqrt{-19}}{2 \sqrt{5}}$
$\Rightarrow x=\frac{-1 \pm \sqrt{19(-1)}}{2 \sqrt{5}}$
We have $\mathrm{i}^{2}=-1$
By substituting -1 $=i^{2}$ in the above equation, we get
$x=\frac{-1 \pm \sqrt{19 \mathrm{i}^{2}}}{2 \sqrt{5}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{(\sqrt{19} \mathrm{i})^{2}}}{2 \sqrt{5}}$
$\Rightarrow \mathrm{x}=\frac{-1 \pm \sqrt{19} \mathrm{i}}{2 \sqrt{5}}$
$\therefore \mathrm{x}=-\frac{1}{2 \sqrt{5}} \pm \frac{\sqrt{19}}{2 \sqrt{5}} \mathrm{i}_{\mathrm{i}}$
Thus, the roots of the given equation are $-\frac{1}{2 \sqrt{5}} \pm \frac{\sqrt{19}}{2 \sqrt{5}} \mathrm{i}$.

## 25. Question

$-x^{2}+x-2=0$

## Answer

Given $-x^{2}+x-2=0$
$\Rightarrow x^{2}-x+2=0$
$\Rightarrow \mathrm{x}^{2}-\mathrm{x}+\frac{1}{4}+\frac{7}{4}=0$
$\Rightarrow \mathrm{x}^{2}-2(\mathrm{x})\left(\frac{1}{2}\right)+\left(\frac{1}{2}\right)^{2}+\frac{7}{4}=0$
$\Rightarrow\left(x-\frac{1}{2}\right)^{2}+\frac{7}{4}=0\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
$\Rightarrow\left(\mathrm{x}-\frac{1}{2}\right)^{2}+\frac{7}{4} \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$\left(x-\frac{1}{2}\right)^{2}+\frac{7}{4}\left(-i^{2}\right)=0$
$\Rightarrow\left(\mathrm{x}-\frac{1}{2}\right)^{2}-\frac{7}{4} \mathrm{i}^{2}=0$
$\Rightarrow\left(x-\frac{1}{2}\right)^{2}-\left(\frac{\sqrt{7}}{2} i\right)^{2}=0$
$\Rightarrow\left(x-\frac{1}{2}+\frac{\sqrt{7}}{2} i\right)\left(x-\frac{1}{2}-\frac{\sqrt{7}}{2} i\right)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}-\frac{1}{2}+\frac{\sqrt{7}}{2} \mathrm{i}=0$ or $\mathrm{x}-\frac{1}{2}-\frac{\sqrt{7}}{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}=\frac{1}{2}-\frac{\sqrt{7}}{2} \mathrm{i}=0$ or $\mathrm{x}=\frac{1}{2}+\frac{\sqrt{7}}{2} \mathrm{i}$
$\therefore \mathrm{X}=\frac{1}{2} \pm \frac{\sqrt{7}}{2} \mathrm{i}$
Thus, the roots of the given equation are $\frac{1}{2} \pm \frac{\sqrt{7}}{2} \mathrm{i}$.

## 26. Question

Solve: $x^{2}-2 x+\frac{3}{2}=0$

## Answer

Given $\mathrm{x}^{2}-2 \mathrm{x}+\frac{3}{2}=0$
$\Rightarrow x^{2}-2 x+1+\frac{1}{2}=0$
$\Rightarrow x^{2}-2(x)\left(\frac{1}{2}\right)+1^{2}+\frac{1}{2}=0$
$\Rightarrow(x-1)^{2}+\frac{1}{2}=0\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
$\Rightarrow(x-1)^{2}+\frac{1}{2} \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$(x-1)^{2}+\frac{1}{2}\left(-i^{2}\right)=0$
$\Rightarrow(x-1)^{2}-\frac{1}{2} i^{2}=0$
$\Rightarrow(\mathrm{x}-1)^{2}-\left(\frac{1}{\sqrt{2}} \mathrm{i}\right)^{2}=0$
$\Rightarrow\left(x-1+\frac{1}{\sqrt{2}} i\right)\left(x-1-\frac{1}{\sqrt{2}} i\right)=0\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow \mathrm{x}-1+\frac{1}{\sqrt{2}} \mathrm{i}=0$ or $\mathrm{x}-1-\frac{1}{\sqrt{2}} \mathrm{i}=0$
$\Rightarrow \mathrm{x}=1-\frac{1}{\sqrt{2}} \mathrm{i}=0$ or $\mathrm{x}=1+\frac{1}{\sqrt{2}} \mathrm{i}$
$\therefore \mathrm{x}=1 \pm \frac{1}{\sqrt{2}} \mathrm{i}$
Thus, the roots of the given equation are $1 \pm \frac{1}{\sqrt{2}} \mathrm{i}$.

## 27. Question

Solve the following quadratics $3 x^{2}-4 x+\frac{20}{3}=0$

## Answer

Given $3 \mathrm{x}^{2}-4 \mathrm{x}+\frac{20}{3}=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=3, b=-4$ and $c=\frac{20}{3}$
$\Rightarrow \mathrm{x}=\frac{-(-4) \pm \sqrt{(-4)^{2}-4(3)\left(\frac{20}{3}\right)}}{2(3)}$
$\Rightarrow \mathrm{x}=\frac{4 \pm \sqrt{16-80}}{6}$
$\Rightarrow x=\frac{4 \pm \sqrt{-64}}{6}$
$\Rightarrow \mathrm{x}=\frac{4 \pm \sqrt{64(-1)}}{6}$
We have $i^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$x=\frac{4 \pm \sqrt{64 i^{2}}}{6}$
$\Rightarrow \mathrm{x}=\frac{4 \pm \sqrt{(8 \mathrm{i})^{2}}}{6}$
$\Rightarrow x=\frac{4 \pm 8 i}{6}$
$\Rightarrow x=\frac{2(2 \pm 4 i)}{6}$
$\Rightarrow \mathrm{x}=\frac{2 \pm 4 \mathrm{i}}{3}$
$\therefore \mathrm{x}=\frac{2}{3} \pm \frac{4}{3} \mathrm{i}$
Thus, the roots of the given equation $\operatorname{are} \frac{2}{3} \pm \frac{4}{3} \mathrm{i}$.

## Exercise 14.2

## 1 A. Question

Solve the following quadratic equations by factorization method:
$x^{2}+10 i x-21=0$

## Answer

$x^{2}+10 i x-21=0$
Given $x^{2}+10 i x-21=0$
$\Rightarrow x^{2}+10 i x-21 \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$x^{2}+10 i x-21\left(-i^{2}\right)=0$
$\Rightarrow x^{2}+10 i x+21 i^{2}=0$
$\Rightarrow x^{2}+3 i x+7 i x+21 i^{2}=0$
$\Rightarrow x(x+3 i)+7 i(x+3 i)=0$
$\Rightarrow(\mathrm{x}+3 \mathrm{i})(\mathrm{x}+7 \mathrm{i})=0$
$\Rightarrow x+3 i=0$ or $x+7 i=0$
$\therefore \mathrm{x}=-3 \mathrm{i}$ or -7 i
Thus, the roots of the given equation are $-3 i$ and $-7 i$.

## 1 B. Question

Solve the following quadratic equations by factorization method:
$x^{2}+(1-2 i) x-2 i=0$

## Answer

$x^{2}+(1-2 i) x-2 i=0$
Given $x^{2}+(1-2 i) x-2 i=0$
$\Rightarrow \mathrm{x}^{2}+\mathrm{x}-2 \mathrm{ix}-2 \mathrm{i}=0$
$\Rightarrow x(x+1)-2 i(x+1)=0$
$\Rightarrow(\mathrm{x}+1)(\mathrm{x}-2 \mathrm{i})=0$
$\Rightarrow \mathrm{x}+1=0$ or $\mathrm{x}-2 \mathrm{i}=0$
$\therefore \mathrm{x}=-1$ or 2 i
Thus, the roots of the given equation are -1 and 2 i .

## 1 C. Question

Solve the following quadratic equations by factorization method:
$x^{2}-(2 \sqrt{3}+3 i) x+6 \sqrt{3} i=0$

## Answer

$x^{2}-(2 \sqrt{3}+3 i) x+6 \sqrt{3} i=0$
Given $\mathrm{x}^{2}-(2 \sqrt{3}+3 \mathrm{i}) \mathrm{x}+6 \sqrt{3} \mathrm{i}=0$
$\Rightarrow \mathrm{x}^{2}-(2 \sqrt{3} \mathrm{x}+3 \mathrm{ix})+6 \sqrt{3} \mathrm{i}=0$
$\Rightarrow \mathrm{x}^{2}-2 \sqrt{3} \mathrm{x}-3 \mathrm{ix}+6 \sqrt{3} \mathrm{i}=0$
$\Rightarrow \mathrm{x}(\mathrm{x}-2 \sqrt{3})-3 \mathrm{i}(\mathrm{x}-2 \sqrt{3})=0$
$\Rightarrow(\mathrm{x}-2 \sqrt{3})(\mathrm{x}-3 \mathrm{i})=0$
$\Rightarrow \mathrm{x}-2 \sqrt{3}=0$ or $\mathrm{x}-3 \mathrm{i}=0$
$\therefore \mathrm{x}=2 \sqrt{3}$ or 3 i
Thus, the roots of the given equation are $2 \sqrt{3}$ and $3 i$.

## 1 D. Question

Solve the following quadratic equations by factorization method:
$6 x^{2}-17 i x-12=0$

## Answer

$6 x^{2}-17 i x-12=0$
Given $6 x^{2}-17 i x-12=0$
$\Rightarrow 6 x^{2}-17 i x-12 \times 1=0$
We have $i^{2}=-1 \Rightarrow 1=-i^{2}$
By substituting $1=-i^{2}$ in the above equation, we get
$6 x^{2}-17 i x-12\left(-i^{2}\right)=0$
$\Rightarrow 6 x^{2}-17 i x+12 i^{2}=0$
$\Rightarrow 6 x^{2}-9 i x-8 i x+12 i^{2}=0$
$\Rightarrow 3 \mathrm{x}(2 \mathrm{x}-3 \mathrm{i})-4 \mathrm{i}(2 \mathrm{x}-3 \mathrm{i})=0$
$\Rightarrow(2 \mathrm{x}-3 \mathrm{i})(3 \mathrm{x}-4 \mathrm{i})=0$
$\Rightarrow 2 \mathrm{x}-3 \mathrm{i}=0$ or $3 \mathrm{x}-4 \mathrm{i}=0$
$\Rightarrow 2 \mathrm{x}=3 \mathrm{i}$ or $3 \mathrm{x}=4 \mathrm{i}$
$\therefore x=\frac{3}{2}$ i or $\frac{4}{3} \mathrm{i}$
Thus, the roots of the given equation are $\frac{3}{2} \mathrm{i}$ and $\frac{4}{3} \mathrm{i}$.

## 2 A. Question

Solve the following quadratic equations:
$x^{2}-(3 \sqrt{2}+2 i) x+6 \sqrt{2} i=0$

## Answer

$x^{2}-(3 \sqrt{2}+2 i) x+6 \sqrt{2} i=0$
Given $\mathrm{x}^{2}-(3 \sqrt{2}+2 \mathrm{i}) \mathrm{x}+6 \sqrt{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}^{2}-(3 \sqrt{2} \mathrm{x}+2 \mathrm{ix})+6 \sqrt{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}^{2}-3 \sqrt{2} \mathrm{x}-2 \mathrm{ix}+6 \sqrt{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}(\mathrm{x}-3 \sqrt{2})-2 \mathrm{i}(\mathrm{x}-3 \sqrt{2})=0$
$\Rightarrow(\mathrm{x}-3 \sqrt{2})(\mathrm{x}-2 \mathrm{i})=0$
$\Rightarrow \mathrm{x}-3 \sqrt{2}=0$ or $\mathrm{x}-2 \mathrm{i}=0$
$\therefore \mathrm{x}=3 \sqrt{2}$ or 2 i
Thus, the roots of the given equation are $3 \sqrt{2}$ and 2 i .

## 2 B. Question

Solve the following quadratic equations:
$x^{2}-(5-i) x+(18+i)=0$

## Answer

$x^{2}-(5-i) x+(18+i)=0$
Given $x^{2}-(5-i) x+(18+i)=0$
Recall that the roots of quadratic equation $a x^{\mathbf{2}}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

Here, $a=1, b=-(5-i)$ and $c=(18+i)$
$\Rightarrow x=\frac{-(-(5-i)) \pm \sqrt{(-(5-i))^{2}-4(1)(18+i)}}{2(1)}$
$\Rightarrow x=\frac{(5-i) \pm \sqrt{(5-i)^{2}-4(18+i)}}{2}$
$\Rightarrow x=\frac{(5-\mathrm{i}) \pm \sqrt{25-10 \mathrm{i}+\mathrm{i}^{2}-72-4 \mathrm{i}}}{2}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{-47-14 \mathrm{i}+\mathrm{i}^{2}}}{2}$
By substituting $i^{2}=-1$ in the above equation, we get
$x=\frac{(5-i) \pm \sqrt{-47-14 i+(-1)}}{2}$
$\Rightarrow x=\frac{(5-\mathrm{i}) \pm \sqrt{-48-14 \mathrm{i}}}{2}$
$\Rightarrow x=\frac{(5-\mathrm{i}) \pm \sqrt{(-1)(48+14 \mathrm{i})}}{2}$
By substituting $-1=i^{2}$ in the above equation, we get
$x=\frac{(5-i) \pm \sqrt{i^{2}(48+14 i)}}{2}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \mathrm{i} \sqrt{48+14 \mathrm{i}}}{2}$
We can write $48+14 i=49-1+14 i$
$\Rightarrow 48+14 i=49+i^{2}+14 i\left[\because i^{2}=-1\right]$
$\Rightarrow 48+14 i=7^{2}+i^{2}+2(7)(i)$
$\Rightarrow 48+14 i=(7+i)^{2}\left[\because(a+b)^{2}=a^{2}+b^{2}+2 a b\right]$
By using the result $48+14 i=(7+i)^{2}$, we get
$x=\frac{(5-i) \pm i \sqrt{(7+i)^{2}}}{2}$
$\Rightarrow x=\frac{(5-i) \pm i(7+i)}{2}$
$\Rightarrow x=\frac{(5-i)+i(7+i)}{2}$ or $\frac{(5-i)-i(7+i)}{2}$
$\Rightarrow \mathrm{x}=\frac{5-\mathrm{i}+7 \mathrm{i}+\mathrm{i}^{2}}{2}$ or $\frac{5-\mathrm{i}-7 \mathrm{i}-\mathrm{i}^{2}}{2}$
$\Rightarrow \mathrm{x}=\frac{5+6 \mathrm{i}+(-1)}{2}$ or $\frac{5-8 \mathrm{i}-(-1)}{2}\left[\because \mathrm{i}^{2}=-1\right]$
$\Rightarrow x=\frac{5+6 i-1}{2}$ or $\frac{5-8 i+1}{2}$
$\Rightarrow x=\frac{4+6 i}{2}$ or $\frac{6-8 i}{2}$
$\Rightarrow \mathrm{x}=\frac{2(2+3 \mathrm{i})}{2}$ or $\frac{2(3-4 \mathrm{i})}{2}$
$\therefore \mathrm{x}=2+3 \mathrm{i}$ or $3-4 \mathrm{i}$
Thus, the roots of the given equation are $2+3 i$ and $3-4 i$.

## 2 C. Question

Solve the following quadratic equations:
$(2+i) x^{2}-(5-i) x+2(1-i)=0$

## Answer

$(2+i) x^{2}-(5-i) x+2(1-i)=0$
Given $(2+i) x^{2}-(5-i) x+2(1-i)=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $\mathrm{a}=(2+\mathrm{i}), \mathrm{b}=-(5-\mathrm{i})$ and $\mathrm{c}=2(1-\mathrm{i})$
$\Rightarrow \mathrm{x}=\frac{-(-(5-\mathrm{i})) \pm \sqrt{(-(5-\mathrm{i}))^{2}-4(2+\mathrm{i})(2(1-\mathrm{i}))}}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{(5-\mathrm{i})^{2}-8(2+\mathrm{i})(1-\mathrm{i})}}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{25-10 \mathrm{i}+\mathrm{i}^{2}-8\left(2-2 \mathrm{i}+\mathrm{i}-\mathrm{i}^{2}\right)}}{2(2+\mathrm{i})}$
By substituting $i^{2}=-1$ in the above equation, we get
$x=\frac{(5-i) \pm \sqrt{25-10 i+(-1)-8(2-i-(-1))}}{2(2+i)}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{24-10 \mathrm{i}-8(3-\mathrm{i})}}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{24-10 \mathrm{i}-24+8 \mathrm{i}}}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm \sqrt{-2 \mathrm{i}}}{2(2+\mathrm{i})}$
We can write $-2 i=-2 i+1-1$
$\Rightarrow-2 i=-2 i+1+i^{2}\left[\because i^{2}=-1\right]$
$\Rightarrow-2 i=1-2 i+i^{2}$
$\Rightarrow-2 i=1^{2}-2(1)(i)+i^{2}$
$\Rightarrow-2 i=(1-i)^{2}\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
By using the result $-2 \mathrm{i}=(1-\mathrm{i})^{2}$, we get
$x=\frac{(5-i) \pm \sqrt{(1-i)^{2}}}{2(2+i)}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i}) \pm(1-\mathrm{i})}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{(5-\mathrm{i})+(1-\mathrm{i})}{2(2+\mathrm{i})}$ or $\frac{(5-\mathrm{i})-(1-\mathrm{i})}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{5-\mathrm{i}+1-\mathrm{i}}{2(2+\mathrm{i})}$ or $\frac{5-\mathrm{i}-1+\mathrm{i}}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{6-2 \mathrm{i}}{2(2+\mathrm{i})}$ or $\frac{4}{2(2+\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{3-\mathrm{i}}{2+\mathrm{i}}$ or $\frac{2}{2+\mathrm{i}}$
$\Rightarrow \mathrm{x}=\frac{3-\mathrm{i}}{2+\mathrm{i}} \times \frac{2-\mathrm{i}}{2-\mathrm{i}}$ or $\frac{2}{2+\mathrm{i}} \times \frac{2-\mathrm{i}}{2-\mathrm{i}}$
$\Rightarrow \mathrm{x}=\frac{(3-\mathrm{i})(2-\mathrm{i})}{(2+\mathrm{i})(2-\mathrm{i})}$ or $\frac{2(2-\mathrm{i})}{(2+\mathrm{i})(2-\mathrm{i})}$
$\Rightarrow \mathrm{x}=\frac{6-3 \mathrm{i}-2 \mathrm{i}+\mathrm{i}^{2}}{2^{2}-\mathrm{i}^{2}}$ or $\frac{4-2 \mathrm{i}}{2^{2}-\mathrm{i}^{2}}$
$\Rightarrow x=\frac{6-5 i+(-1)}{4-(-1)}$ or $\frac{4-2 i}{4-(-1)}\left[\because i^{2}=-1\right]$
$\Rightarrow \mathrm{x}=\frac{5-5 \mathrm{i}}{4+1}$ or $\frac{4-2 \mathrm{i}}{4+1}$
$\Rightarrow x=\frac{5(1-i)}{5}$ or $\frac{4-2 i}{5}$
$\therefore \mathrm{x}=1-\mathrm{i}$ or $\frac{4}{5}-\frac{2}{5} \mathrm{i}$
Thus, the roots of the given equation are $1-i$ and ${ }^{4}-{ }^{2}$

## 2 D. Question

Solve the following quadratic equations:
$x^{2}-(2+i) x-(1-7 i)=0$

## Answer

$x^{2}-(2+i) x-(1-7 i)=0$
Given $\mathrm{x}^{2}-(2+\mathrm{i}) \mathrm{x}-(1-7 \mathrm{i})=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $\mathrm{a}=1, \mathrm{~b}=-(2+\mathrm{i})$ and $\mathrm{c}=-(1-7 \mathrm{i})$
$\Rightarrow \mathrm{x}=\frac{-(-(2+\mathrm{i})) \pm \sqrt{(-(2+\mathrm{i}))^{2}-4(1)(-(1-7 \mathrm{i}))}}{2(1)}$
$\Rightarrow \mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{(2+\mathrm{i})^{2}+4(1-7 \mathrm{i})}}{2}$
$\Rightarrow \mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{4+4 \mathrm{i}+\mathrm{i}^{2}+4-28 \mathrm{i}}}{2}$
$\Rightarrow \mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{8-24 \mathrm{i}+\mathrm{i}^{2}}}{2}$
By substituting $\mathrm{i}^{2}=-1$ in the above equation, we get
$\mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{8-24 \mathrm{i}+(-1)}}{2}$
$\Rightarrow \mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{7-24 \mathrm{i}}}{2}$
We can write $7-24 i=16-9-24 i$
$\Rightarrow 7-24 i=16+9(-1)-24 i$
$\Rightarrow 7-24 i=16+9 i^{2}-24 i\left[\because i^{2}=-1\right]$
$\Rightarrow 7-24 i=4^{2}+(3 i)^{2}-2(4)(3 i)$
$\Rightarrow 7-24 i=(4-3 i)^{2}\left[\because(a-b)^{2}=a^{2}-b^{2}+2 a b\right]$
By using the result $7-24 i=(4-3 i)^{2}$, we get
$\mathrm{x}=\frac{(2+\mathrm{i}) \pm \sqrt{(4-3 \mathrm{i})^{2}}}{2}$
$\Rightarrow \mathrm{x}=\frac{(2+\mathrm{i}) \pm(4-3 \mathrm{i})}{2}$
$\Rightarrow x=\frac{(2+i)+(4-3 i)}{2}$ or $\frac{(2+i)-(4-3 i)}{2}$
$\Rightarrow \mathrm{x}=\frac{2+\mathrm{i}+4-3 \mathrm{i}}{2}$ or $\frac{2+\mathrm{i}-4+3 \mathrm{i}}{2}$
$\Rightarrow x=\frac{6-2 i}{2}$ or $\frac{-2+4 i}{2}$
$\Rightarrow \mathrm{x}=\frac{2(3-\mathrm{i})}{2}$ or $\frac{2(-1+2 \mathrm{i})}{2}$
$\therefore \mathrm{x}=3-\mathrm{i}$ or $-1+2 \mathrm{i}$
Thus, the roots of the given equation are $3-\mathrm{i}$ and $-1+2 \mathrm{i}$.

## 2 E. Question

Solve the following quadratic equations:
$i x^{2}-4 x-4 i=0$

## Answer

$i x^{2}-4 x-4 i=0$
Given $\mathrm{ix}^{2}-4 \mathrm{x}-4 \mathrm{i}=0$
$\Rightarrow \mathrm{ix}^{2}+4 \mathrm{x}(-1)-4 \mathrm{i}=0$
We have $i^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$i x^{2}+4 x i^{2}-4 i=0$
$\Rightarrow \mathrm{i}\left(\mathrm{x}^{2}+4 \mathrm{ix}-4\right)=0$
$\Rightarrow x^{2}+4 i x-4=0$
$\Rightarrow x^{2}+4 i x+4(-1)=0$
$\Rightarrow x^{2}+4 i x+4 i^{2}=0\left[\because i^{2}=-1\right]$
$\Rightarrow \mathrm{x}^{2}+2 \mathrm{ix}+2 \mathrm{ix}+4 \mathrm{i}^{2}=0$
$\Rightarrow \mathrm{x}(\mathrm{x}+2 \mathrm{i})+2 \mathrm{i}(\mathrm{x}+2 \mathrm{i})=0$
$\Rightarrow(x+2 i)(x+2 i)=0$
$\Rightarrow(x+2 i)^{2}=0$
$\Rightarrow \mathrm{x}+2 \mathrm{i}=0$
$\therefore x=-2 i$ (double root)
Thus, the roots of the given equation are $-2 i$ and $-2 i$.

## 2 F. Question

Solve the following quadratic equations:
$x^{2}+4 i x-4=0$

## Answer

$x^{2}+4 i x-4=0$
Given $x^{2}+4 i x-4=0$
$\Rightarrow x^{2}+4 i x+4(-1)=0$
We have $i^{2}=-1$
By substituting -1 = $\mathrm{i}^{2}$ in the above equation, we get
$\Rightarrow \mathrm{x}^{2}+4 \mathrm{ix}+4 \mathrm{i}^{2}=0$
$\Rightarrow x^{2}+2 i x+2 i x+4 i^{2}=0$
$\Rightarrow \mathrm{x}(\mathrm{x}+2 \mathrm{i})+2 \mathrm{i}(\mathrm{x}+2 \mathrm{i})=0$
$\Rightarrow(\mathrm{x}+2 \mathrm{i})(\mathrm{x}+2 \mathrm{i})=0$
$\Rightarrow(x+2 i)^{2}=0$
$\Rightarrow \mathrm{x}+2 \mathrm{i}=0$
$\therefore \mathrm{x}=-2 \mathrm{i}$ (double root)
Thus, the roots of the given equation are $-2 i$ and $-2 i$.

## 2 G. Question

Solve the following quadratic equations:
$2 \mathrm{x}^{2}+\sqrt{15} \mathrm{i} x-\mathrm{i}=0$

## Answer

$2 \mathrm{x}^{2}+\sqrt{15} \mathrm{ix}-\mathrm{i}=0$
Given $2 \mathrm{x}^{2}+\sqrt{15} \mathrm{ix}-\mathrm{i}=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $\mathrm{a}=2, \mathrm{~b}=\sqrt{15} \mathrm{i}$ and $\mathrm{c}=-\mathrm{i}$
$\Rightarrow \mathrm{x}=\frac{-(\sqrt{15 \mathrm{i}}) \pm \sqrt{(\sqrt{15 i})^{2}-4(2)(-\mathrm{i})}}{2(2)}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{i}} \pm \sqrt{15 \mathrm{i}^{2}+8 \mathrm{i}}}{4}$
By substituting $i^{2}=-1$ in the above equation, we get
$x=\frac{-\sqrt{15} i \pm \sqrt{15(-1)+8 i}}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{j}} \mathrm{i} \pm \sqrt{8 \mathrm{i}-15}}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{i}} \pm \sqrt{(-1)(15-8 \mathrm{i})}}{4}$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{-\sqrt{15 \mathrm{i}} \mathrm{i} \pm \sqrt{\mathrm{i}^{2}(15-8 \mathrm{i})}}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{i}} \mathrm{i} \pm \mathrm{i} \sqrt{15-8 \mathrm{i}}}{4}$
We can write $15-8 \mathrm{i}=16-1-8 \mathrm{i}$
$\Rightarrow 15-8 i=16+(-1)-8 i$
$\Rightarrow 15-8 i=16+i^{2}-8 i\left[\because i^{2}=-1\right]$
$\Rightarrow 15-8 \mathrm{i}=4^{2}+(\mathrm{i})^{2}-2(4)(\mathrm{i})$
$\Rightarrow 15-8 i=(4-i)^{2}\left[\because(a-b)^{2}=a^{2}-b^{2}+2 a b\right]$
By using the result $15-8 \mathrm{i}=(4-\mathrm{i})^{2}$, we get
$x=\frac{-\sqrt{15 i} i \pm i \sqrt{(4-i)^{2}}}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{i}} \pm \mathrm{i}(4-\mathrm{i})}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15} \mathrm{i}+\mathrm{i}(4-\mathrm{i})}{4}$ or $\frac{-\sqrt{15 \mathrm{i}} \mathrm{i}-\mathrm{i}(4-\mathrm{i})}{4}$
$\Rightarrow x=\frac{-\sqrt{15} i+4 i-i^{2}}{4}$ or $\frac{-\sqrt{15} i-4 i+i^{2}}{4}$
$\Rightarrow \mathrm{x}=\frac{-\sqrt{15 \mathrm{i}}+4 \mathrm{i}-(-1)}{4}$ or $\frac{-\sqrt{15 \mathrm{i}}-4 \mathrm{i}+(-1)}{4}\left[\because \mathrm{i}^{2}=-1\right]$
$\Rightarrow x=\frac{-\sqrt{15} i+4 i+1}{4}$ or $\frac{-\sqrt{15 i} i-4 i-1}{4}$
$\Rightarrow \mathrm{x}=\frac{1+(4-\sqrt{15}) \mathrm{i}}{4}$ or $\frac{-1-(4+\sqrt{15}) \mathrm{i}}{4}$
$\therefore \mathrm{x}=\frac{1}{4}+\left(\frac{4-\sqrt{15}}{4}\right) \mathrm{i}$ or $-\frac{1}{4}-\left(\frac{4+\sqrt{15}}{4}\right) \mathrm{i}$
Thus, the roots of the given equation are $\frac{1}{4}+\left(\frac{4-\sqrt{15}}{4}\right) \mathrm{i}$ and $-\frac{1}{4}-\left(\frac{4+\sqrt{15}}{4}\right) \mathrm{i}$.

## 2 H. Question

Solve the following quadratic equations:
$x^{2}-x+(1+i)=0$

## Answer

$x^{2}-x+(1+i)=0$
Given $\mathrm{x}^{2}-\mathrm{x}+(1+\mathrm{i})=0$

## Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by

$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=1, b=-1$ and $c=(1+i)$
$\Rightarrow \mathrm{x}=\frac{-(-1) \pm \sqrt{(-1)^{2}-4(1)(1+\mathrm{i})}}{2(1)}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \sqrt{1-4(1+\mathrm{i})}}{2}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \sqrt{1-4-4 \mathrm{i}}}{2}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \sqrt{-3-4 \mathrm{i}}}{2}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \sqrt{(-1)(3+4 \mathrm{i})}}{2}$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{1 \pm \sqrt{\mathrm{i}^{2}(3+4 \mathrm{i})}}{2}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \mathrm{i} \sqrt{3+4 \mathrm{i}}}{2}$
We can write $3+4 i=4-1+4 i$
$\Rightarrow 3+4 i=4+i^{2}+4 i\left[\because i^{2}=-1\right]$
$\Rightarrow 3+4 i=2^{2}+i^{2}+2(2)(i)$
$\Rightarrow 3+4 i=(2+i)^{2}\left[\because(a+b)^{2}=a^{2}+b^{2}+2 a b\right]$
By using the result $3+4 i=(2+i)^{2}$, we get
$\mathrm{x}=\frac{1 \pm \mathrm{i} \sqrt{(2-\mathrm{i})^{2}}}{2}$
$\Rightarrow \mathrm{x}=\frac{1 \pm \mathrm{i}(2+\mathrm{i})}{2}$
$\Rightarrow \mathrm{x}=\frac{1+\mathrm{i}(2+\mathrm{i})}{2}$ or $\frac{1-\mathrm{i}(2+\mathrm{i})}{2}$
$\Rightarrow \mathrm{x}=\frac{1+2 \mathrm{i}+\mathrm{i}^{2}}{2}$ or $\frac{1-2 \mathrm{i}-\mathrm{i}^{2}}{2}$
$\Rightarrow \mathrm{x}=\frac{1+2 \mathrm{i}+(-1)}{2}$ or $\frac{1-2 \mathrm{i}-(-1)}{2}\left[\because \mathrm{i}^{2}=-1\right]$
$\Rightarrow \mathrm{x}=\frac{1+2 \mathrm{i}-1}{2}$ or $\frac{1-2 \mathrm{i}+1}{2}$
$\Rightarrow x=\frac{2 i}{2}$ or $\frac{2-2 i}{2}$
$\Rightarrow x=i$ or $\frac{2(1-i)}{2}$
$\therefore \mathrm{x}=\mathrm{i}$ or $1-\mathrm{i}$
Thus, the roots of the given equation are i and $1-\mathrm{i}$.

## 2 I. Question

Solve the following quadratic equations:
$i x^{2}-x+12 i=0$

## Answer

$i x^{2}-x+12 i=0$
Given $i x^{2}-x+12 i=0$
$\Rightarrow \mathrm{ix}^{2}+\mathrm{x}(-1)+12 \mathrm{i}=0$
We have $i^{2}=-1$
By substituting $-1=i^{2}$ in the above equation, we get
$i x^{2}+x i^{2}+12 i=0$
$\Rightarrow \mathrm{i}\left(\mathrm{x}^{2}+\mathrm{ix}+12\right)=0$
$\Rightarrow \mathrm{x}^{2}+\mathrm{ix}+12=0$
$\Rightarrow \mathrm{x}^{2}+\mathrm{ix}-12(-1)=0$
$\Rightarrow x^{2}+i x-12 i^{2}=0\left[\because i^{2}=-1\right]$
$\Rightarrow \mathrm{x}^{2}-3 \mathrm{ix}+4 \mathrm{ix}-12 \mathrm{i}^{2}=0$
$\Rightarrow x(x-3 i)+4 i(x-3 i)=0$
$\Rightarrow(x-3 i)(x+4 i)=0$
$\Rightarrow x-3 i=0$ or $x+4 i=0$
$\therefore \mathrm{x}=3 \mathrm{i}$ or -4 i
Thus, the roots of the given equation are 3 i and -4 i .

## 2 J. Question

Solve the following quadratic equations:
$x^{2}-(3 \sqrt{2}-2 i) x-\sqrt{2} i=0$

## Answer

$\mathrm{x}^{2}-(3 \sqrt{2}-2 \mathrm{i}) \mathrm{x}-\sqrt{2} \mathrm{i}=0$
Given $\mathrm{x}^{2}-(3 \sqrt{2}-2 \mathrm{i}) \mathrm{x}-\sqrt{2} \mathrm{i}=0=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

Here, $\mathrm{a}=1, \mathrm{~b}=-(3 \sqrt{2}-2 \mathrm{i})$ and $\mathrm{c}=-\sqrt{2} \mathrm{i}$
$\Rightarrow \mathrm{x}=\frac{-(-(3 \sqrt{2}-2 \mathrm{i})) \pm \sqrt{(-(3 \sqrt{2}-2 \mathrm{i}))^{2}-4(1)(-\sqrt{2} \mathrm{i})}}{2(1)}$
$\Rightarrow x=\frac{(3 \sqrt{2}-2 i) \pm \sqrt{(3 \sqrt{2}-2 i)^{2}+4 \sqrt{2} i}}{2}$
$\Rightarrow x=\frac{(3 \sqrt{2}-2 i) \pm \sqrt{18-12 \sqrt{2} i+4 i^{2}+4 \sqrt{2}} \mathrm{i}}{2}$
$\Rightarrow \mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i}) \pm \sqrt{18-8 \sqrt{2} \mathrm{i}+4 \mathrm{i}^{2}}}{2}$
By substituting $\mathrm{i}^{2}=-1$ in the above equation, we get
$x=\frac{(3 \sqrt{2}-2 i) \pm \sqrt{18-8 \sqrt{2} i+4(-1)}}{2}$
$\Rightarrow \mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i}) \pm \sqrt{18-8 \sqrt{2} \mathrm{i}-4}}{2}$
$\Rightarrow \mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i}) \pm \sqrt{14-8 \sqrt{2}} \mathrm{i}}{2}$
We can write $14-8 \sqrt{2} i=16-2-8 \sqrt{2} i$
$\Rightarrow 14-8 \sqrt{2} \mathrm{i}=16+2(-1)-8 \sqrt{2} \mathrm{i}$
$\Rightarrow 14-8 \sqrt{2} \mathrm{i}=16+2 \mathrm{i}^{2}-8 \sqrt{2} \mathrm{i}\left[\because \mathrm{i}^{2}=-1\right]$
$\Rightarrow 14-8 \sqrt{2} \mathrm{i}=4^{2}+(\sqrt{2} \mathrm{i})^{2}-2(4)(\sqrt{2} \mathrm{i})$
$\Rightarrow 14-8 \sqrt{2} \mathrm{i}=(4-\sqrt{2} \mathrm{i})^{2}\left[\because(a-b)^{2}=a^{2}-2 a b+b^{2}\right]$
By using the result $14-8 \sqrt{2} \mathrm{i}=(4-\sqrt{2} \mathrm{i})^{2}$, we get
$\mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i}) \pm \sqrt{(4-\sqrt{2} \mathrm{i})^{2}}}{2}$
$\Rightarrow \mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i}) \pm(4-\sqrt{2} \mathrm{i})}{2}$
$\Rightarrow \mathrm{x}=\frac{(3 \sqrt{2}-2 \mathrm{i})+(4-\sqrt{2} \mathrm{i})}{2}$ or $\frac{(3 \sqrt{2}-2 \mathrm{i})-(4-\sqrt{2} \mathrm{i})}{2}$
$\Rightarrow \mathrm{x}=\frac{3 \sqrt{2}-2 \mathrm{i}+4-\sqrt{2} \mathrm{i}}{2}$ or $\frac{3 \sqrt{2}-2 \mathrm{i}-4+\sqrt{2} \mathrm{i}}{2}$
$\Rightarrow \mathrm{x}=\frac{3 \sqrt{2}+4-(2+\sqrt{2}) \mathrm{i}}{2}$ or $\frac{3 \sqrt{2}-4-(2-\sqrt{2}) \mathrm{i}}{2}\left[\because i^{2}=-1\right]$
$\therefore \mathrm{x}=\frac{3 \sqrt{2}+4}{2}-\left(\frac{2+\sqrt{2}}{2}\right) \mathrm{i}$ or $\frac{3 \sqrt{2}-4}{2}-\left(\frac{2-\sqrt{2}}{2}\right) \mathrm{i}$
Thus, the roots of the given equation are $\frac{3 \sqrt{2}+4}{2}-\left(\frac{2+\sqrt{2}}{2}\right) \mathrm{i}$ and $\frac{3 \sqrt{2}-4}{2}-\left(\frac{2-\sqrt{2}}{2}\right) \mathrm{i}$.
2 K. Question

Solve the following quadratic equations:
$x^{2}-(\sqrt{2}+i) x+\sqrt{2} i=0$

## Answer

xi. $x^{2}-(\sqrt{2}+i) x+\sqrt{2} i=0$

Given $\mathrm{x}^{2}-(\sqrt{2}+\mathrm{i}) \mathrm{x}+\sqrt{2} \mathrm{i}=0$
$\Rightarrow x^{2}-(\sqrt{2} x+i x)+\sqrt{2} i=0$
$\Rightarrow \mathrm{x}^{2}-\sqrt{2} \mathrm{x}-\mathrm{ix}+\sqrt{2} \mathrm{i}=0$
$\Rightarrow \mathrm{x}(\mathrm{x}-\sqrt{2})-\mathrm{i}(\mathrm{x}-\sqrt{2})=0$
$\Rightarrow(\mathrm{x}-\sqrt{2})(\mathrm{x}-\mathrm{i})=0$
$\Rightarrow \mathrm{x}-\sqrt{2}=0$ or $\mathrm{x}-\mathrm{i}=0$
$\therefore \mathrm{X}=\sqrt{2}$ or i
Thus, the roots of the given equation are $\sqrt{2}$ and $i$.

## 2 L. Question

Solve the following quadratic equations:
$2 x^{2}-(3+7 i) x+(9 i-3)=0$

## Answer

$2 x^{2}-(3+7 i) x+(9 i-3)=0$
Given $2 x^{2}-(3+7 i) x+(9 i-3)=0$
Recall that the roots of quadratic equation $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Here, $a=2, b=-(3+7 i)$ and $c=(9 i-3)$
$\Rightarrow x=\frac{-(-(3+7 i)) \pm \sqrt{(-(3+7 i))^{2}-4(2)(9 i-3)}}{2(2)}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \sqrt{(3+7 \mathrm{i})^{2}-8(9 \mathrm{i}-3)}}{4}$
$\Rightarrow x=\frac{(3+7 i) \pm \sqrt{9+42 i+49 i^{2}-72 i+24}}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \sqrt{33-30 \mathrm{i}+49 \mathrm{i}^{2}}}{4}$
By substituting $\mathrm{i}^{2}=-1$ in the above equation, we get
$x=\frac{(3+7 i) \pm \sqrt{33-30 i+49(-1)}}{4}$
$\Rightarrow x=\frac{(3+7 i) \pm \sqrt{33-30 i-49}}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \sqrt{-16-30 \mathrm{i}}}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \sqrt{(-1)(16+30 \mathrm{i})}}{4}$
By substituting $-1=i^{2}$ in the above equation, we get
$\mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \sqrt{\mathrm{i}^{2}(16+30 \mathrm{i})}}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \mathrm{i} \sqrt{16+30 \mathrm{i}}}{4}$
We can write $16+30 i=25-9+30 i$
$\Rightarrow 16+30 \mathrm{i}=25+9(-1)+30 \mathrm{i}$
$\Rightarrow 16+30 i=25+9 i^{2}+30 i\left[\because i^{2}=-1\right]$
$\Rightarrow 16+30 i=5^{2}+(3 i)^{2}+2(5)(3 i)$
$\Rightarrow 16+30 i=(5+3 i)^{2}\left[\because(a+b)^{2}=a^{2}+b^{2}+2 a b\right]$
By using the result $16+30 i=(5+3 i)^{2}$, we get
$x=\frac{(3+7 i) \pm i \sqrt{(5+3 i)^{2}}}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i}) \pm \mathrm{i}(5+3 \mathrm{i})}{4}$
$\Rightarrow \mathrm{x}=\frac{(3+7 \mathrm{i})+\mathrm{i}(5+3 \mathrm{i})}{4}$ or $\frac{(3+7 \mathrm{i})-\mathrm{i}(5+3 \mathrm{i})}{4}$
$\Rightarrow \mathrm{x}=\frac{3+7 \mathrm{i}+5 \mathrm{i}+3 \mathrm{i}^{2}}{4}$ or $\frac{3+7 \mathrm{i}-5 \mathrm{i}-3 \mathrm{i}^{2}}{4}$
$\Rightarrow \mathrm{x}=\frac{3+12 \mathrm{i}+3 \mathrm{i}^{2}}{4}$ or $\frac{3+2 \mathrm{i}-3 \mathrm{i}^{2}}{4}$
$\Rightarrow x=\frac{3+12 \mathrm{i}+3(-1)}{4}$ or $\frac{3+2 \mathrm{i}-3(-1)}{4}\left[\because \mathrm{i}^{2}=-1\right]$
$\Rightarrow x=\frac{3+12 i-3}{4}$ or $\frac{3+2 i+3}{4}$
$\Rightarrow x=\frac{12}{4} \mathrm{i}$ or $\frac{6+2 \mathrm{i}}{4}$
$\Rightarrow x=3 i$ or $\frac{6}{4}+\frac{2}{4} i$
$\therefore \mathrm{x}=3 \mathrm{i}$ or $\frac{3}{2}+\frac{1}{2} \mathrm{i}$
Thus, the roots of the given equation are 3 i and $\frac{3}{2}+\frac{1}{2} \mathrm{i}$.

## Very Short Answer

## 1. Question

Write the number of real roots of the equation $(x-1)^{2}+(x-2)^{2}+(x-3)^{2}=0$.

## Answer

given $(x-1)^{2}+(x-2)^{2}+(x-3)^{2}=0$
$x^{2}+1-2 x+x^{2}+4-4 x+x^{2}+9-6 x=0$
$3 x^{2}-12 x+14=0$
Comparing it with $a x^{2}+b x+c=0$ and substituting them in $b^{2}-4 a c$, we get
$=(-12)^{2}-4(3)(14)$
$=144-168$
$=-24<0$.
Hence the given equation do not have real roots. It has imaginary roots.

## 2. Question

If $a$ and $b$ are roots of the equation $x^{2}-p x+q=0$, then write the value of $\frac{1}{a}+\frac{1}{b}$.

## Answer

given $x^{2}-p x+q=0$
We know sum of the roots $=p$
Product of the roots $=\mathrm{q}$
As given that $a$ and $b$ are roots then,
$a+b=p$
$a b=q$
given $\frac{1}{a}+\frac{1}{b}$
$=\frac{a+b}{a b}$
$=\frac{\mathrm{p}}{\mathrm{q}}$.

## 3. Question

If roots $\alpha, \beta$ of equation $x^{2}-p x+16=0$ satisfy the relation $\alpha^{2}+\beta^{2}=9$, then write the value of $p$.

## Answer

given $\alpha^{2}+\beta^{2}=9$
$(\alpha+\beta)^{2}-2 \alpha \beta=9$
Given $x^{2}-p x+16=0$ and $\alpha, \beta$ are roots of the equation then
Sum of roots $\alpha+\beta=p$
Product of roots $\alpha \beta=16$
Substituting these in $(\alpha+\beta)^{2}-2 \alpha \beta=9$ we get,
$p^{2}-2(16)=9$
$p^{2}=41$
$P= \pm \sqrt{ } 41$

## 4. Question

If $2+\sqrt{3}$ is a root of the equation $\mathrm{x}^{2}+\mathrm{px}+\mathrm{q}=0$, then write the values of p and q .

## Answer

we know irrational roots always exists in pair hence if $2+\sqrt{3}$ is one root then $2-\sqrt{3}$ is another root.
Given $\mathrm{x}^{2}+\mathrm{px}+\mathrm{q}=0$
Sum of roots $=-p$
$2+\sqrt{ } 3+2-\sqrt{ } 3=-p$
$P=-4$
Product of roots $=q$
$(2+\sqrt{ } 3)(2-\sqrt{ } 3)=q$
$4-3=q$
$q=1$.

## 5. Question

If the difference between the roots of the equation $x^{2}+a x+8=0$ is 2 write the values of $a$.

## Answer

given $x^{2}+a x+8=0$ and $\alpha-\beta=2$
Also from given equation $\alpha \beta=8$
As $\alpha-\beta=2$
Then $\alpha-\frac{8}{\alpha}=2$
$\alpha^{2}-2 \alpha-8=0$
$(\alpha-4)(\alpha+2)=0$
$\alpha=4$ and $\alpha=-2$
if $\alpha=4$ then substituting it in $\alpha-\beta=2$ we get,
$\beta=2$
from the given equation,
sum of roots $=-a$
$\alpha+\beta=-a$
$-\mathrm{a}=4+2$
$a=-6$
if $\alpha=-2$ then substituting it in $\alpha-\beta=2$ we get,
$\beta=-4$
then sum of roots $\alpha+\beta=-a$
$a=6$
therefore $\mathrm{a}= \pm 6$.

## 6. Question

Write the roots of the equation $(a-b) x^{2}+(b-c) x+(c-a)=0$

## Answer

roots of a quadratic equation is $\mathrm{x}=\frac{-\mathrm{b} \pm \sqrt{\mathrm{b}^{2}-4 \mathrm{ac}}}{2 \mathrm{a}}$
From the given equation we get,
$x=\frac{-(b-c) \pm \sqrt{(b-c)^{2}-4(a-b)(c-a)}}{2(a-b)}$
$x=\frac{-(b-c) \pm \sqrt{b^{2}+c^{2}-2 b c-4 a c+4 a^{2}+4 b c-4 a b}}{2(a-b)}$
$x=\frac{-(b-c) \pm \sqrt{(-2 a+b+c)^{2}}}{2(a-b)}$
$=\frac{-\mathrm{b}+\mathrm{c}+(-2 \mathrm{a}+\mathrm{b}+\mathrm{c})}{2(\mathrm{a}-\mathrm{b})}$ and $\frac{-\mathrm{b}+\mathrm{c}-(-2 \mathrm{a}+\mathrm{b}+\mathrm{c})}{2(\mathrm{a}-\mathrm{b})}$
$=\frac{2(c-a)}{2(a-b)}$ and $\frac{2(a-b)}{2(a-b)}$
$=\frac{(c-a)}{(a-b)}$ and 1
Therefore $\mathrm{x}=1, \frac{(\mathrm{c}-\mathrm{a})}{(\mathrm{a}-\mathrm{b})}$.

## 7. Question

If $a$ and $b$ are roots of the equation $x^{2}-x+1=0$, then write the value of $a^{2}+b^{2}$.

## Answer

from the given equation sum of roots $a+b=1$
Product of roots $\mathrm{ab}=1$
Now $a^{2}+b^{2}=(a+b)^{2}-2 a b$
$=1-2$
$=-1$.

## 8. Question

Write the number of quadratic equations, with real roots, which do not change by squaring their roots.

## Answer

from the given condition roots remain unchanged only when they are equal to 1 and 0 .
Hence the roots may be $(0,1)$ or $(1,0)$ and $(1,1)$ and $(0,0)$.
Hence 3 equations can be formed by substituting these points in $(x-a)(x-b)=0$
Where $a, b$ are roots or points.

## 9. Question

If $\alpha, \beta$ are roots of the equation $x^{2}+\mathrm{lx}+\mathrm{m}=0$, write an equation whose roots are $-\frac{1}{\alpha}$ and $-\frac{1}{\beta}$.

## Answer

from the given equation sum of the roots $\alpha+\beta=-$ I
Product of roots $\alpha \beta=\mathrm{m}$
Formula to form a quadratic equation is $x^{2}-(\alpha+\beta) x+\alpha \beta=0$

Where $\alpha, \beta$ are roots of equation.
Given $\frac{-1}{\alpha}, \frac{-1}{\beta}$ are roots, then required quadratic equation is
$x^{2}-\left(\frac{-1}{\alpha}+\frac{-1}{\beta}\right) x+\frac{1}{\alpha \beta}=0$
$x^{2}+\left(\frac{\alpha+\beta}{\alpha \beta}\right) x+\frac{1}{\alpha \beta}=0$
$x^{2}+\left(\frac{-l}{m}\right) x+\frac{1}{m}=0$
$m x^{2}-\mid x+1=0$.

## 10. Question

If $\alpha, \beta$ are roots of the equation $x^{2}-a(x+1)-c=0$, then write the value of $(1+\alpha)(1+\beta)$.

## Answer

given $x^{2}-a(x+1)-c=0$
$x^{2}-a x-a-c=0$
$x^{2}-a x-(a+c)=0$
as $\alpha, \beta$ are roots of equation, we get
sum of the roots $\alpha+\beta=a$
Product of roots $\alpha \beta=-(a+c)$
Given $(1+\alpha)(1+\beta)$
$=1+(\alpha+\beta)+(\alpha \beta)$
$=1+a-a-c$
$=1-\mathrm{c}$.

## MCQ

## 1. Question

Mark the Correct alternative in the following:
The complete set of values of $k$, for which the quadratic equation $x^{2}-k x+k+2=0$ has equal rots, consists of
A. $2+\sqrt{12}$
B. $2 \pm \sqrt{12}$
C. $2-\sqrt{12}$
D. $-2-\sqrt{12}$

## Answer

Since roots are equal then $b^{2}-4 a c=0$
From the given equation we get,
$K^{2}-4(1)(K+2)=0$
$\mathrm{K}^{2}-4 \mathrm{k}-8=0$
$\mathrm{k}=\frac{4 \pm \sqrt{4^{2}-4(-8)}}{2}$
$=\frac{4 \pm \sqrt{16+32}}{2}$
$=\frac{4 \pm \sqrt{48}}{2}$
$=\frac{4 \pm 2 \sqrt{12}}{2}$
$=2 \pm \sqrt{ } 12$

## 2. Question

Mark the Correct alternative in the following:
For the equation $|\mathrm{x}|^{2}+|\mathrm{x}|-6=0$, the sum of the real roots is
A. 1
B. 0
C. 2
D. none of these

## Answer

given $|x|^{2}+|x|-6=0$
When $x>0$
It can be written as $x^{2}+x-6=0$
$(x+3)(x-2)=0$
$X=2$
When $\mathrm{x}<0$
It can be written as $x^{2}-x-6=0$
$(x-3)(x+2)=0$
$X=-2$
Therefore $x= \pm 2$
Hence sum of the roots $=0$.

## 3. Question

Mark the Correct alternative in the following:
If $a, b$ are the roots of the equation $x^{2}+x+1=0$, then $a^{2}+b^{2}=$
A. 1
B. 2
C. -1
D. 3

Answer
from the given equation sum of roots $a+b=-1$

Product of roots $\mathrm{ab}=1$
Given $a^{2}+b^{2}$
$(a+b)^{2}-2 a b$
$=1-2$
$=-1$.

## 4. Question

Mark the Correct alternative in the following:
If $\alpha, \beta$ are roots of the equation $4 x^{2}+3 x+7=0$, then $1 / \alpha+1 / \beta$ is equal to
A. $7 / 3$
B. $-7 / 3$
C. $3 / 7$
D. $-3 / 7$

## Answer

given $4 x^{2}+3 x+7=0$
We know sum of the roots $=\frac{-3}{4}$
Product of the roots $=\frac{7}{4}$
As given that $\alpha$ and $\beta$ are roots then,
$\alpha+\beta=\frac{-3}{4}$
$\alpha \beta=\frac{7}{4}$
given $\frac{1}{\alpha}+\frac{1}{\beta}$
$=\frac{\alpha+\beta}{\alpha \beta}$
$=\frac{-\frac{3}{4}}{\frac{7}{4}}$
$=\frac{-3}{7}$

## 5. Question

Mark the Correct alternative in the following:
The values of $x$ satisfying $\log _{3}\left(x^{2}+4 x+12\right)=2$ are
A. $2,-4$
B. $1,-3$
C. $-1,3$
D. $-1,-3$

Answer
given $\log _{3}\left(x^{2}+4 x+12\right)=2$
It can be written as
$\log _{3}\left(x^{2}+4 x+12\right)=2 \log _{3} 3$
$=\log _{3} 3^{2}$
$\log _{3}\left(x^{2}+4 x+12\right)=\log _{3} 9$
$x^{2}+4 x+12=9$
$x^{2}+4 x+3=0$
$(x+1)(x+3)=0$
$X=-1,-3$.

## 6. Question

Mark the Correct alternative in the following:
The number of real roots of the equation $\left(x^{2}+2 x\right)^{2}-(x+1)^{2}-55=0$ is
A. 2
B. 1
C. 4
D. none of these

## Answer

given $\left(x^{2}+2 x\right)^{2}-(x+1)^{2}-55=0$
$\left[\left(x^{2}+2 x+1\right)-1\right]^{2}-(x+1)^{2}-55=0$
$(x+1)^{4}-2(x+1)^{2}+1-(x+1)^{2}-55=0$
$(x+1)^{4}-3(x+1)^{2}-54=0$
let $(x+1)^{2}=r$
$r^{2}-3 r-54=0$
$r^{2}-9 r+6 r-54=0$
$r(r-9)+6(r-9)=0$
$r=-6,9$
but $(x+1)^{2} \geq 0$ so, $(x+1)^{2} \neq-6$
so, $(x+1)^{2}=9$
$x+1= \pm 3$
$x=-1 \pm 3$
$x=-4$, and 2 .

## 7. Question

Mark the Correct alternative in the following:
If $\alpha, \beta$ are the roots of the equation $a x^{2}+b x+c=0$, then $\frac{1}{a \alpha+b}+\frac{1}{a \beta+b}=$
A. $c / a b$
B. $a / b c$
C. b/ac
D. none of these

## Answer

given $\frac{1}{a \alpha+b}+\frac{1}{a \beta+b}$
$=\frac{\mathrm{a} \alpha+\mathrm{b}+\mathrm{a} \beta+\mathrm{b}}{(\mathrm{a} \alpha+\mathrm{b})(\mathrm{a} \beta+\mathrm{b})}$
$=\frac{a(\alpha+\beta)+2 b}{a^{2}(\alpha \beta)+a b(\alpha+\beta)+b^{2}}$
$=\frac{a\left(\frac{-b}{a}\right)+2 b}{a^{2}\left(\frac{c}{a}\right)+a b\left(\frac{-b}{a}\right)+b^{2}}$
$=\frac{b}{a c-b^{2}+b^{2}}$
$=\frac{\mathrm{b}}{\mathrm{ac}}$.

## 8. Question

Mark the Correct alternative in the following:
If $\alpha, \beta$ are the roots of the equation $x^{2}+p x+1=0 ; \gamma, \delta$ the roots of the equation $x^{2}+q x+1=0$, then $(\alpha-\gamma)(\alpha+\delta)(\beta-\gamma)(\beta+\delta)=$
A. $q^{2}-p^{2}$
B. $\mathrm{p}^{2}-\mathrm{q}^{2}$
C. $p^{2}+q^{2}$
D. none of these

## Answer

$\alpha^{2}+p \alpha+1=0, \beta^{2}+p \beta+1=0$
$\alpha+\beta=-p, \alpha \beta=1$
$\gamma^{2}+q Y+1=0, \delta^{2}+q \delta+1=0$
$\delta-\gamma=\sqrt{q^{2}-4}, \gamma \delta=1$
$(\alpha-\gamma)(\alpha+\delta)(\beta-\gamma)(\beta+\delta)$
$=\left(\alpha^{2}+\alpha(\delta-\gamma)-\gamma \delta\right)\left(\beta^{2}+\beta(\delta-\gamma)-\delta \gamma\right)$
$=\left(\alpha^{2}+\alpha \sqrt{q^{2}-4}-1\right)\left(\beta^{2}+\beta \sqrt{q^{2}-4}-1\right)$
$=\left(-2-p \alpha+\alpha \sqrt{q^{2}-4}\right)\left(-2-p \beta+\beta \sqrt{q^{2}-4}\right)$
$=4+2 p \beta-2 \beta \sqrt{q^{2}-4}+2 p \alpha+p^{2} \alpha \beta-p \alpha \beta \sqrt{q^{2}-4}-2 \alpha \sqrt{q^{2}-4}$
$-p \beta \alpha \sqrt{q^{2}-4}+\alpha^{2} \beta^{2}\left(q^{2}-4\right)$
$=4+2 p(\alpha+\beta)-2 \sqrt{q^{2}-4}(\alpha+\beta)+p^{2} \alpha \beta-2 p \alpha \beta \sqrt{q^{2}-4}$
$+\alpha^{2} \beta^{2}\left(q^{2}-4\right)$
$=4-2 p^{2}+2 p \sqrt{q^{2}-4}+p^{2}-2 p \sqrt{q^{2}-4}+\left(q^{2}-4\right)$
$=4-2 p^{2}+p^{2}+q^{2}-4$
$=q^{2}-p^{2}$

## 9. Question

Mark the Correct alternative in the following:
The number of real solutions of $\left|2 x-x^{2}-3\right|=1$ is
A. 0
B. 2
C. 3
D. 4

## Answer

given $\left|2 x-x^{2}-3\right|=1$
$2 x-x^{2}-3= \pm 1$
When $2 x-x^{2}-3=1$
$\Rightarrow 2 x-x^{2}-3-1=0$
$\Rightarrow 2 x-x^{2}-4=0$
$=x^{2}-2 x+4=0$
Discriminant, $\mathrm{D}=4-16$
$=-12<0$
Hence the roots are unreal.
When $2 x-x^{2}-3=-1$
$=x^{2}-2 x-2=0$
Discriminant, $D=4-8=-4<0$
Hence the roots are unreal.
Hence the given equation has no real roots.

## 10. Question

Mark the Correct alternative in the following:
The number of solutions of $\mathrm{x}^{2}+|\mathrm{x}-1|=1$ is
A. 0
B. 1
C. 2
D. 3

Answer
when $\mathrm{x}>0$
$x^{2}+x-1=1$
$x^{2}+x-2=0$
$(x-1)(x+2)=0$
$x=1,-2$
when $\mathrm{x}<0$
$x^{2}-x+1=1$
$x^{2}-x=0$
$x(x-1)=0$
$x=0,1$
hence the given equation has 3 solutions and they are $x=0,1,-1$.

## 11. Question

Mark the Correct alternative in the following:
If $x$ is real and $k=\frac{x^{2}-x+1}{x^{2}+x+1}$, then
A. $k \in[1 / 3,3]$
B. $k \geq 3$
C. $k \leq 1 / 3$
D. none of these

## Answer

$\left(x^{2}+x+1\right) k=\left(x^{2}-x+1\right)$
$(k-1) x^{2}+(k+1) x+(k-1)=0$
For roots of quadratic equation real
Case I: a $\neq 0$ and $\mathrm{D} \geq 0$
$k-1 \neq 0 \Rightarrow k \neq 1$
$\sqrt{(\mathrm{k}+1)^{2}-4(\mathrm{k}-1)(\mathrm{k}-1)} \geq 0$
$-3 k^{2}+10 k-3 \geq 0$
$3 \mathrm{k}^{2}-10 \mathrm{k}+3 \leq 0$
$3\left(k^{2}-\frac{10}{3} k+1\right) \leq 0$
$\mathrm{k}^{2}-2\left(\frac{5}{3}\right)(\mathrm{k})+\frac{25}{9}-\frac{25}{9}+1 \leq 0$
$\left(k-\frac{5}{3}\right)^{2} \leq \frac{16}{9}$
$\mathrm{k}-\frac{5}{3} \geq \frac{-4}{3}$ or $\mathrm{k}-\frac{5}{3} \leq \frac{4}{3}$
$\mathrm{k} \geq \frac{1}{3}$ or $\mathrm{k} \leq 3$

Case II : a = 0
$k-1=0 \Rightarrow k=1$
At $k=1,2 x=0 \Rightarrow x=0$ is real
So, $k=1$ is also count in answer.
Then, final answer is $k \in[1 / 3,3]$

## 12. Question

Mark the Correct alternative in the following:
If the roots of $x^{2}-b x+c=0$ are two consecutive integers, then $b^{2}-4 c$ is
A. 0
B. 1
C. 2
D. None of these

## Answer

given that roots are consecutive, let they be a, a+1
From the formula for quadratic equation,
$(x-a)(x-a-1)=x^{2}-(a+1) x-a x+a(a+1)=x^{2}-(2 a+1) x+a(a+1)$ thenb $b^{2}-4 c=(2 a+1)^{2}-4 a(a+1)=$ $4 a^{2}+1+4 a-4 a^{2}-4 a=1$.

## 13. Question

Mark the Correct alternative in the following:
The value of a such that $x^{2}-11 x+a=0$ and $x^{2}-14 x+2 a=0$ may have a common root is
A. 0
B. 12
C. 24
D. 32

## Answer

subtracting both the equations we get,
$x^{2}-11 x+a-x^{2}+14 x+2 a=0$
$3 \mathrm{x}-\mathrm{a}=0$
$\mathrm{x}=\frac{\mathrm{a}}{3}$
Substituting it in first equation we get,
$\left(\frac{a}{3}\right)^{2}-11 \frac{a}{3}+a=0$
$\frac{a^{2}}{9}-\frac{8 a}{3}=0$
$a^{2}-24 a=0$
$a=24$.
14. Question

Mark the Correct alternative in the following:
The values of k for which is quadratic equation $\mathrm{kx}^{2}+1=\mathrm{kx}+3 \mathrm{x}-11 \mathrm{x}^{2}$ has real and equal roots are
A. $-11,-3$
B. 5, 7
C. $5,-7$
D. None of these

## Answer

given $k x^{2}+1=k x+3 x-11 x^{2}$
$x^{2}(k+11)-x(k+3)+1=0$
as the roots are real and equal then the discriminant is equal to zero.
$D=b^{2}-4 a c=0$
$(k+3)^{2}-4(k+11)(1)=0$
$\mathrm{K}^{2}+9+6 \mathrm{k}-4 \mathrm{k}-44=0$
$\mathrm{K}^{2}+2 \mathrm{k}-35=0$
$(k-5)(k+7)=0$
$K=5,-7$.

## 15. Question

Mark the Correct alternative in the following:
If one root of the equation $x^{2}+p x+12=0$ is 4 , while the equation $x^{2}+p x+q=0$ has equal roots, the value of $q$ is
A. $46 / 4$
B. $4 / 49$
C. 4
D. none of these

Answer
multiplying first equation and subtracting both the equations we get,
$2 x^{2}+4 x+6 \lambda-2 x^{2}-3 x-5 \lambda=0$
$x+\lambda=0$
$x=-\lambda$
Substituting it in first equation we get,
$(-\lambda)^{2}+2(-\lambda)+3 \lambda=0$
$\lambda^{2}+\lambda=0$
$\lambda=-1$.

## 16. Question

Mark the Correct alternative in the following:
If one root of the equation $x^{2}+p x+12=0$ is 4 , while the equation $x^{2}+p x+q=0$ has equal roots, the
value of $q$ is
A. $46 / 4$
B. $4 / 49$
C. 4
D. none of these

## Answer

given 4 is the root of $x^{2}+p x+12=0$
$=16+4 p+12=0$
$4 p=-28$
$P=-7$
Given $x^{2}+p x+q=0$ has equal roots, then discriminant is 0.
$D=b^{2}-4 a c=0$
$p^{2}-4 q=0$
$4 q=49$
$\mathrm{q}=\frac{49}{4}$.

## 17. Question

Mark the Correct alternative in the following:
The value of $p$ and $q(p \neq 0, q \neq 0)$ for which $p, q$ are the roots of the equation $x^{2}+p x+q$ ab=0 are
A. $p=1, q=-2$
B. $p=-1, q=-2$
C. $p=-1, q=2$
D. $p=1, q=2$

## Answer

Sum of the roots $=\frac{-b}{a}=-p$
$\Rightarrow p+q=-p$
Product of the roots $=\frac{c}{a}=q$
$\Rightarrow p q=q$
$\Rightarrow p=1$
Put value of $p$ in eq.(1)
$\Rightarrow 1+q=-1$
$\Rightarrow q=-2$

## 18. Question

Mark the Correct alternative in the following:
The set of all vales of $m$ for which both the roots of the equation $x^{2}-(m+1) x+m+4=0$ are real and negative, is
A. $(-,-3][5, \infty)$
B. $[-3,5]$
C. $(-4,-3]$
D. $(-3,-1]$

## Answer

For roots to be real its $\mathrm{D} \geq 0$
$\sqrt{(m+1)^{2}-4(1)(m+4)} \geq 0$
$(m+1)^{2}-4(m+4) \geq 0$
$m^{2}-2 m-15 \geq 0$
$(m-1)^{2}-16 \geq 0$
$(m-1)^{2} \geq 16$
$m-1 \leq-4$ or $m-1 \geq 4$
$m \leq-3$ or $m \geq 5$
For both roots to be negative product of roots should be positive and sum of roots should be negative.

Product of roots $=m+4>0 \Rightarrow m>-4$
Sum of roots $=m+1<0 \Rightarrow m<-1$
After taking intersection of $\mathrm{D} \geq 0$, Product of roots $>0$ and sum of roots $<0$. We can say that the final answer is
$m \in(-4,-3]$
19. Question

Mark the Correct alternative in the following:
The number of roots of the equation $\frac{(x+2)(x-5)}{(x-3)(x+6)}=\frac{x-2}{x+4}$ is
A. 0
B. 1
C. 2
D. 3

## Answer

given $\frac{(x+2)(x-5)}{(x-3)(x+6)}=\frac{x-2}{x+4}$
$(x+2)(x-5)(x+4)=(x-2)(x-3)(x+6)$
$x^{3}+4 x^{2}-5 x^{2}-20 x+2 x^{2}+8 x-10 x-40=x^{3}+6 x^{2}-3 x^{2}-18 x-2 x^{2}-12 x+6 x+36$
$x^{2}-22 x-40=x^{2}-24 x+36$
$4 x=76$
$x=19$
hence the given equation has only one solution.
20. Question

Mark the Correct alternative in the following:
If $\alpha$ and $\beta$ are the roots of $4 x^{2}+3 x+7=0$, then the value of $\frac{1}{\alpha}+\frac{1}{\beta}$ is
A. $\frac{4}{7}$
B. $-\frac{3}{7}$
C. $\frac{3}{7}$
D. $-\frac{3}{4}$

## Answer

given $4 x^{2}+3 x+7=0$
We know sum of the roots $=\frac{-3}{4}$
Product of the roots $=\frac{7}{4}$
As given that $\alpha$ and $\beta$ are roots then,
$\alpha+\beta=\frac{-3}{4}$
$\alpha \beta=\frac{7}{4}$
given $\frac{1}{\alpha}+\frac{1}{\beta}$
$=\frac{\alpha+\beta}{\alpha \beta}$
$=\frac{-\frac{3}{4}}{\frac{7}{4}}$
$=\frac{-3}{7}$

## 21. Question

Mark the Correct alternative in the following:
If $\alpha, \beta$ are the roots of the equation $\mathrm{x}^{2}+\mathrm{px}+\mathrm{q}=0$, then $-\frac{1}{\alpha},-\frac{1}{\beta}$ are the roots of the equation
A. $x^{2}-p x+q=0$
B. $x^{2}+p x+q=0$
C. $\mathrm{qx}^{2}+\mathrm{px}+1=0$
D. $q x^{2}-\mathrm{px}+1=0$

## Answer

from the given equation sum of the roots $\alpha+\beta=-p$
Product of roots $\alpha \beta=q$
Formula to form a quadratic equation is $x^{2}-(\alpha+\beta) x+\alpha \beta=0$
Where $\alpha, \beta$ are roots of equation.
Given $\frac{-1}{\alpha}, \frac{-1}{\beta}$ are roots, then required quadratic equation is
$x^{2}-\left(\frac{-1}{\alpha}+\frac{-1}{\beta}\right) x+\frac{1}{\alpha \beta}=0$
$x^{2}+\left(\frac{\alpha+\beta}{\alpha \beta}\right) x+\frac{1}{\alpha \beta}=0$
$x^{2}+\left(\frac{-p}{q}\right) x+\frac{1}{q}=0$
$q x^{2}-p x+1=0$

## 22. Question

Mark the Correct alternative in the following:
If the difference of the roots of $x^{2}-p x+q=0$ is unity, then
A. $p^{2}+4 q=1$
B. $p^{2}-4 q=1$
C. $p^{2}+4 q^{2}=(1+2 q)^{2}$
D. $4 p^{2}+q^{2}=(1+2 p)^{2}$

## Answer

Difference of the roots $=\frac{\sqrt{D}}{|a|}$
$1=\frac{\sqrt{b^{2}-4 a c}}{|a|}$
$1=\frac{\sqrt{(-p)^{2}-4(1)(q)}}{|1|}$
$p^{2}-4 q=1$
$p^{2}-4 q+4 q^{2}-4 q^{2}=1$
$p^{2}+4 q^{2}=1+2(2)(q)+(2 q)^{2}$
$p^{2}+4 q^{2}=(1+2 q)^{2}$

## 23. Question

Mark the Correct alternative in the following:
If $\alpha, \beta$ are the roots of the equation $x^{2}-p(x+1)-c=0$, then $(\alpha+1)(\beta+1)=$
A. C
B. $c-1$
C. $1-\mathrm{c}$
D. none of these

## Answer

given $x^{2}-p(x+1)-c=0$
$x^{2}-p x-p-c=0$
$x^{2}-p x-(p+c)=0$
as $\alpha, \beta$ are roots of equation, we get
sum of the roots $\alpha+\beta=p$
Product of roots $\alpha \beta=-(p+c)$
Given $(1+\alpha)(1+\beta)$
$=1+(\alpha+\beta)+(\alpha \beta)$
$=1+p-p-c$
$=1-\mathrm{c}$.

## 24. Question

Mark the Correct alternative in the following:
The least value of $k$ which makes the roots of the equation $x^{2}+5 x+k=0$ imaginary is
A. 4
B. 5
C. 6
D. 7

## Answer

given that the equation has imaginary roots, hence the discriminant is less than 0 .
$=25-4 \mathrm{k}<0$
When we submit 7 in $k$ the condition above will be satisfied and when we replace 6 the condition will be false.
So the least value of $k$ is 7 .

## 25. Question

Mark the Correct alternative in the following:
The equation of the smallest degree with real coefficients having $1+i$ as one of the roots is
A. $x^{2}+x+1=0$
B. $x^{2}-2 x+2=0$
C. $x^{2}+2 x+2=0$
D. $x^{2}+2 x-2=0$

## Answer

for the complex roots it will exists in pair.
Hence the roots are $1+i$ and 1-i
Formula for quadratic equation is $(x-a)(x-b)=0$
$(x-1-\mathrm{i})(\mathrm{x}-1+\mathrm{i})=0$
$x^{2}-x+i x-x+1-i-i x+i-i^{2}=0$
$x^{2}-2 x+2=0$.

