

20 Trigonometrical Tables

20.1 TRIGONOMETRICAL TABLES

The approximate values correct upto four decimal places of *sine*, *cosine* and *tangent* of all angles lying between 0° and 90° can be found from the tables of *natural sines*, *natural cosines* and *natural tangents* given at the end of the book. These tables are called **trigonometrical tables**.

Trigonometrical tables consist of three parts :

- (i) a column on the extreme left containing degrees from 0 to 90.
- (ii) ten columns (at the intervals of $6'$) headed by $0'$, $6'$, $12'$, $18'$, $24'$, $30'$, $36'$, $42'$, $48'$ and $54'$.
- (iii) five columns (called mean difference columns) for an increase of $1'$, $2'$, $3'$, $4'$ and $5'$ in the angle.

20.2 USE OF TRIGONOMETRICAL TABLES

We illustrate the method of using trigonometrical tables with the help of following examples :

ILLUSTRATIVE EXAMPLES

Example 1. Find the value of $\sin 53^\circ 34'$.

Solution. To find the value of $\sin 53^\circ 34'$, we read the table of natural sines in the horizontal line which begins with 53° and in the vertical column headed by $30'$ ($\because 34' = 30' + 4'$). The value that we find is 8039. Now read, in the same horizontal line, the value written in the mean difference column headed by $4'$; it is found to be 7. On adding these two numbers, we get $8039 + 7 = 8046$, and so $\sin 53^\circ 34' = .8046$.

Thus the value of $\sin 53^\circ 34'$ is obtained as under :

$\sin 53^\circ 30' = .8039$	(From tables)
Mean difference for $4' = 7$	(To be added)
$\therefore \sin 53^\circ 34' = .8046$.	

Example 2. Find the value of $\cos 49^\circ 21'$.

Solution. We know that as θ increases, the value of $\cos \theta$ decreases, therefore, the numbers in the mean difference columns are to be subtracted.

The value of $\cos 49^\circ 21'$ is obtained as under :

$$\begin{aligned} \text{Since} \quad \cos 49^\circ 21' &= \cos (49^\circ 18' + 3') \\ \cos 49^\circ 18' &= \cdot 6521 && \text{(From tables)} \\ \text{Mean difference for } 3' &= 7 && \text{(To be subtracted)} \\ \therefore \quad \cos 49^\circ 21' &= \cdot 6514. \end{aligned}$$

Example 3. Find the value of $\tan 65^\circ 41'$.

Solution. Since $\tan 65^\circ 41' = \tan (65^\circ 36' + 5')$

$$\begin{aligned} \tan 65^\circ 36' &= 2.2045 && \text{(From tables)} \\ \text{Mean difference for } 5' &= 85 && \text{(To be added)} \\ \therefore \quad \tan 65^\circ 41' &= 2.2130. \end{aligned}$$

Note

By using the trigonometrical tables of natural sines, natural cosines and natural tangents, we can find the angle whose sine, cosine or tangent is given. We illustrate this with the help of following examples :

Example 4. Using trigonometric tables, find the measure of the angle θ when $\sin \theta = 0.2826$.

Solution. In the table of natural sines, look for a value (≤ 0.2826) which is sufficiently close to 0.2826 . We find that the value 0.2823 occurs in the horizontal line beginning with 16° and in the column headed by $24'$. Then, we look for the number $3 (= 2826 - 2823)$ in the same horizontal line and in the mean differences column, we find the number 3 in the column headed by $1'$, so we get $\theta = 16^\circ 24' + 1' = 16^\circ 25'$.

Thus the value of θ is obtained as under :

$$\begin{aligned} \text{Given} \quad \sin \theta &= 0.2826 \\ \sin 16^\circ 24' &= 0.2823 && \text{(From tables)} \\ \therefore \quad \text{Difference} &= 0.0003 \\ \text{Mean difference for } 1' &= 0.0003 && \text{(From tables)} \\ \therefore \quad \theta &= 16^\circ 24' + 1' = 16^\circ 25'. \end{aligned}$$

Example 5. Find the acute angle θ when $\cos \theta = 0.8637$.

Solution. Given $\cos \theta = 0.8637$

$$\begin{aligned} \cos 30^\circ 18' &= 0.8634 && \text{(From tables)} \\ \therefore \quad \text{Difference} &= 0.0003 \\ \text{Mean difference for } 2' &= 0.0003 && \text{(From tables)} \\ \therefore \quad \theta &= 30^\circ 18' - 2' = 30^\circ 16'. \end{aligned}$$

(\because greater is the value of $\cos \theta$, smaller is θ)

Example 6. Using tables, find the value of $2 \sin \theta - \cos \theta$ when $\tan \theta = 0.3726$.

Solution. Given $\tan \theta = 0.3726$

$$\begin{aligned} \tan 20^\circ 24' &= 0.3719 && \text{(From tables)} \\ \therefore \quad \text{Difference} &= 0.0007 \end{aligned}$$

Mean difference for $2' = .0007$ (From tables)

$$\therefore \theta = 20^\circ 24' + 2' = 20^\circ 26'$$

Thus to find the value of $2 \sin \theta - \cos \theta$, we have to find the values of $\sin 20^\circ 26'$ and $\cos 20^\circ 26'$.

$\sin 20^\circ 24' = .3486$ (From tables)

Mean difference for $2' = 5$ (To be added)

$$\therefore \sin 20^\circ 26' = .3491$$

$\cos 20^\circ 24' = .9373$ (From tables)

Mean difference for $2' = 2$ (To be subtracted)

$$\therefore \cos 20^\circ 26' = .9371$$

$$\begin{aligned} 2 \sin \theta - \cos \theta &= 2 \sin 20^\circ 26' - \cos 20^\circ 26' \\ &= 2 \times .3491 - .9371 \\ &= .6982 - .9371 = -.2389. \end{aligned}$$

Exercise 20

1. Find the value of the following :

(i) $\sin 35^\circ 22'$

(ii) $\sin 71^\circ 31'$

(iii) $\sin 65^\circ 20'$

(iv) $\sin 23^\circ 56'$

2. Find the value of the following :

(i) $\cos 62^\circ 27'$

(ii) $\cos 3^\circ 11'$

(iii) $\cos 86^\circ 40'$

(iv) $\cos 45^\circ 58'$

3. Find the value of the following :

(i) $\tan 15^\circ 2'$

(ii) $\tan 53^\circ 14'$

(iii) $\tan 82^\circ 18'$

(iv) $\tan 6^\circ 9'$

4. Use tables to find the acute angle θ , given that

(i) $\sin \theta = .5789$

(ii) $\sin \theta = .9484$

(iii) $\sin \theta = .2357$

(iv) $\sin \theta = .6371$

5. Use tables to find the acute angle θ , given that

(i) $\cos \theta = .4625$

(ii) $\cos \theta = .9906$

(iii) $\cos \theta = .6951$

(iv) $\cos \theta = .3412$

6. Use tables to find the acute angle θ , given that

(i) $\tan \theta = .2685$

(ii) $\tan \theta = 1.7451$

(iii) $\tan \theta = 3.1749$

(iv) $\tan \theta = .9347$

7. Using trigonometric table, find the measure of the angle A when $\sin A = 0.1822$.

8. Using tables, find the value of $2 \sin \theta - \cos \theta$ when

(i) $\theta = 35^\circ$

(ii) $\tan \theta = .2679$

9. If $\sin x^\circ = 0.67$, find the value of

(i) $\cos x^\circ$

(ii) $\cos x^\circ + \tan x^\circ$

10. If θ is acute and $\cos \theta = .7258$, find the value of

(i) θ

(ii) $2 \tan \theta - \sin \theta$